A visualization of the cosmic web, showing a complex network of filaments and nodes of matter. The filaments are colored in shades of blue, green, and yellow, while the nodes are bright orange and red. The background is dark, with small white dots representing individual galaxies.

# Getting bored with CDM? — structure formation & dark matter

Ken Nagamine  
Osaka U. / UNLV

# Contents

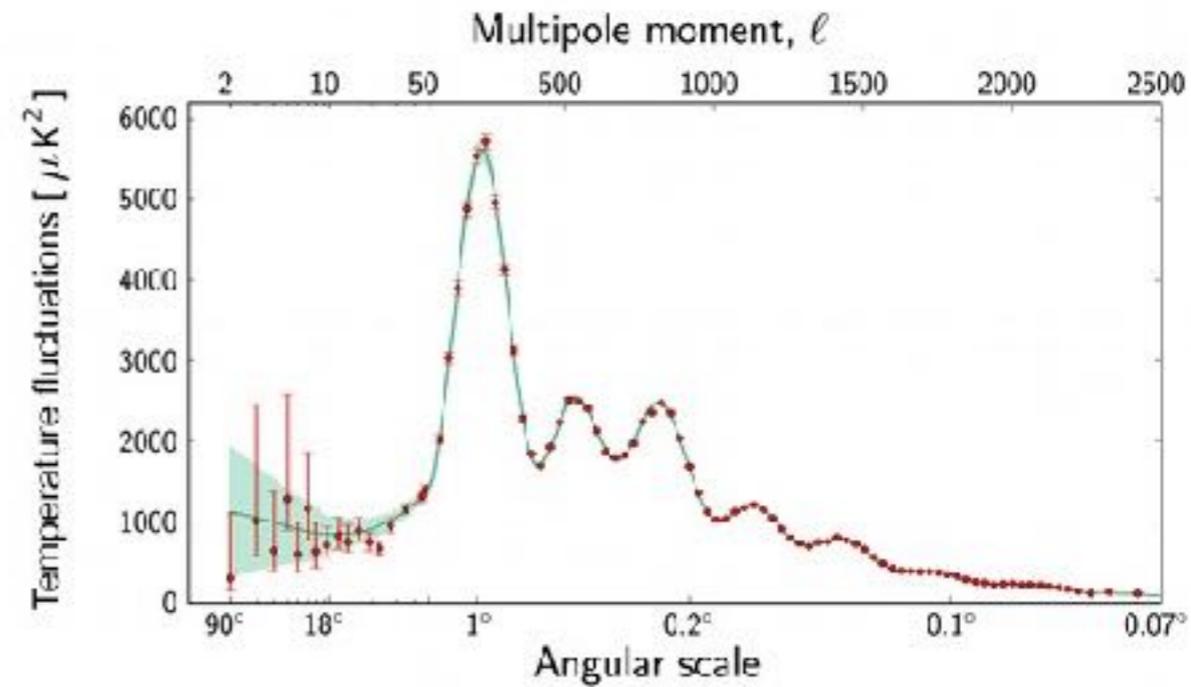
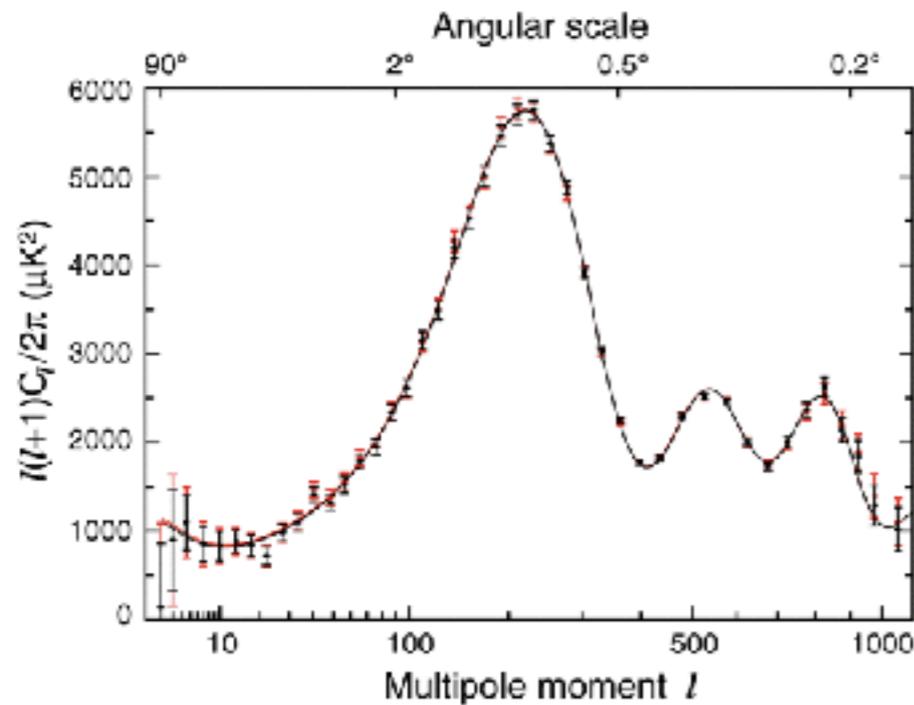
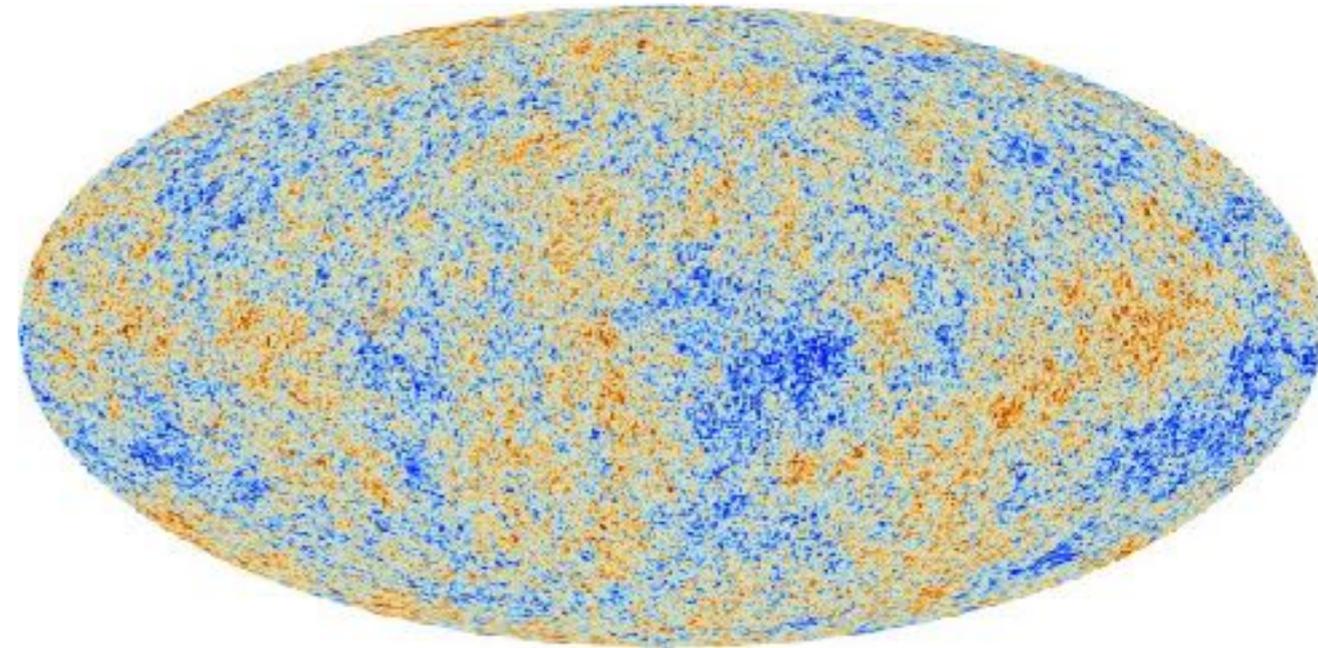
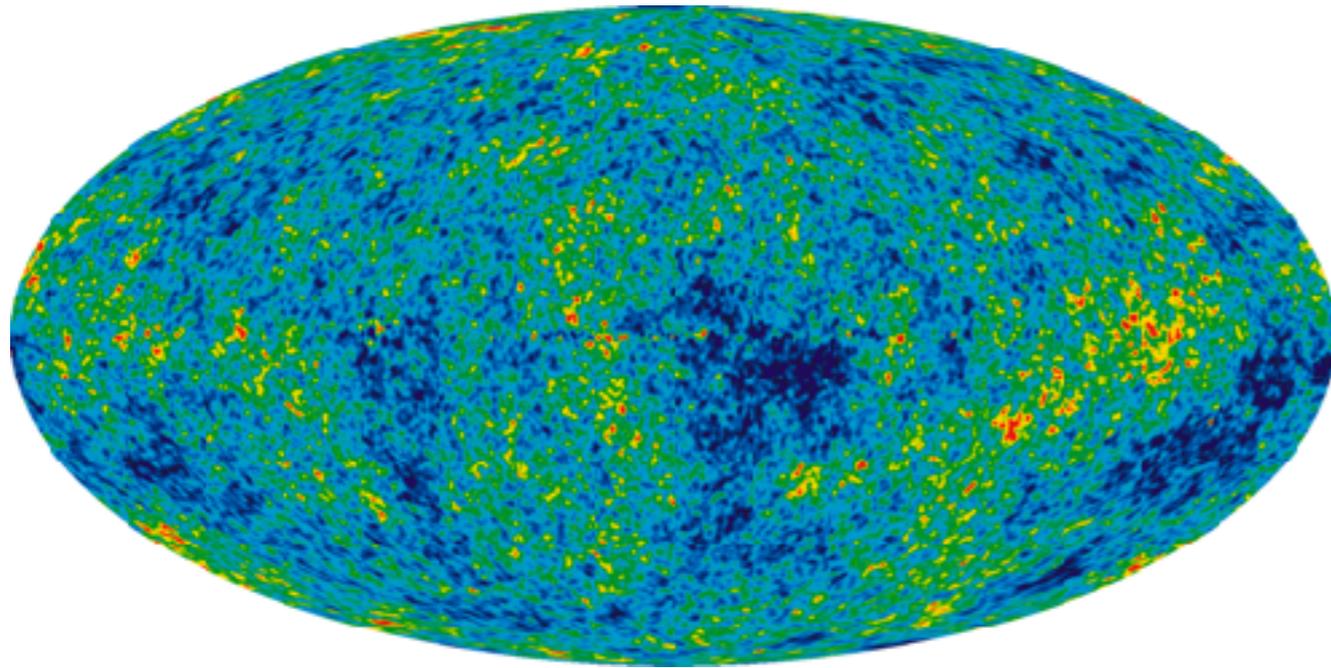
- Successful  **$\Lambda$ CDM** model on **large-scales**
- What about  $\lesssim 10$  kpc? — “**small scale problem**”
- **Alternative models: e.g., WDM, SIDM, FDM, ...**
- Complication of **baryonic physics** — do we really need alternative DM ?

# Evidence of Dark Matter

## and its success on large scales

- **Galaxy clusters** — ~80% of mass is dark (Zwicky '33)
- **Galaxy rotation curves** (Rubin & Ford '70)
- **CMB** (angular power spectrum)
- **Structure formation** —  $P(k)$ , galaxy clustering, Ly- $\alpha$  forest
- **Gravitational lensing** (strong & weak)
- **Bullet Cluster** (Markevich+'02; Clowe+'06)
- .....

# WMAP & Planck CMB results

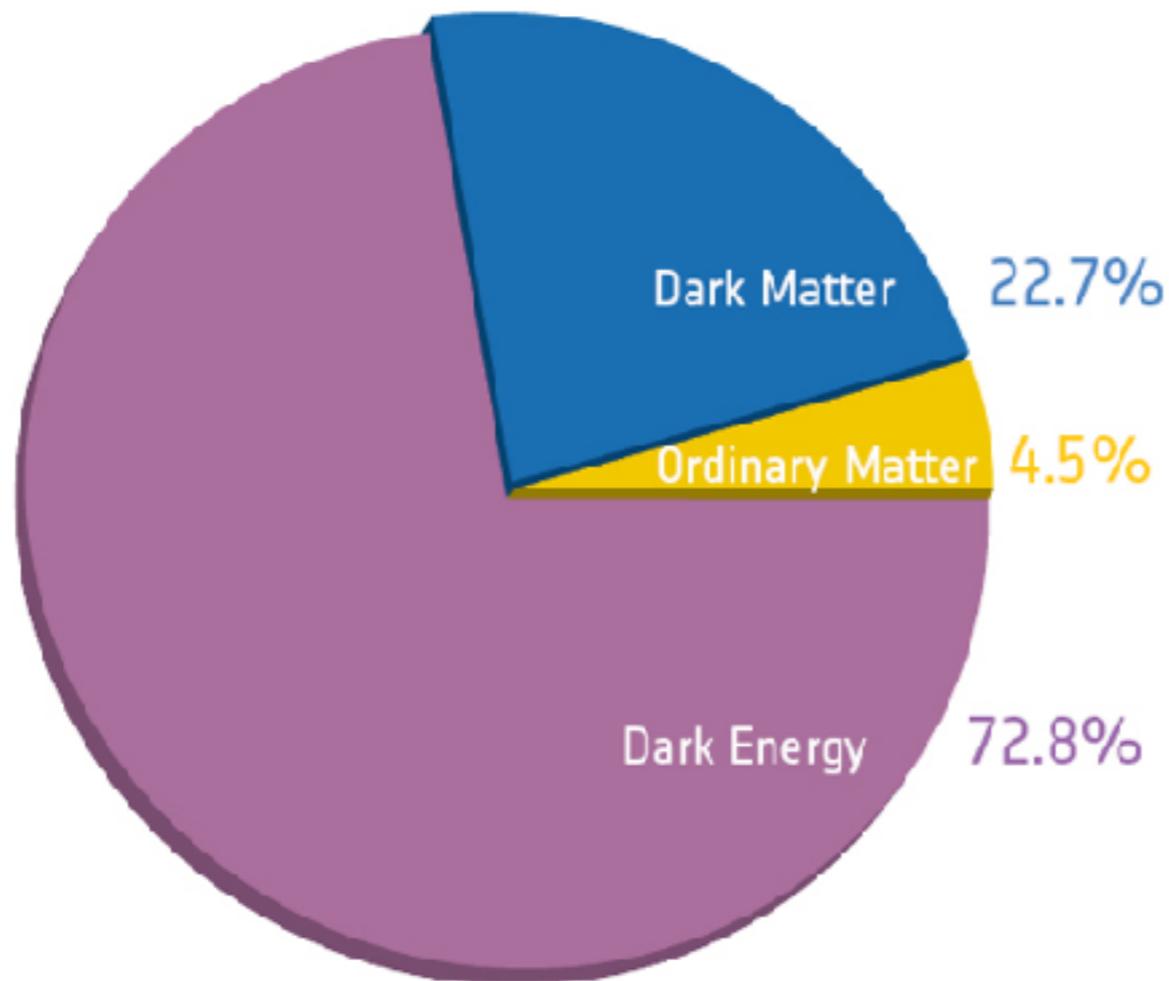


WMAP9; Hinshaw+ '13

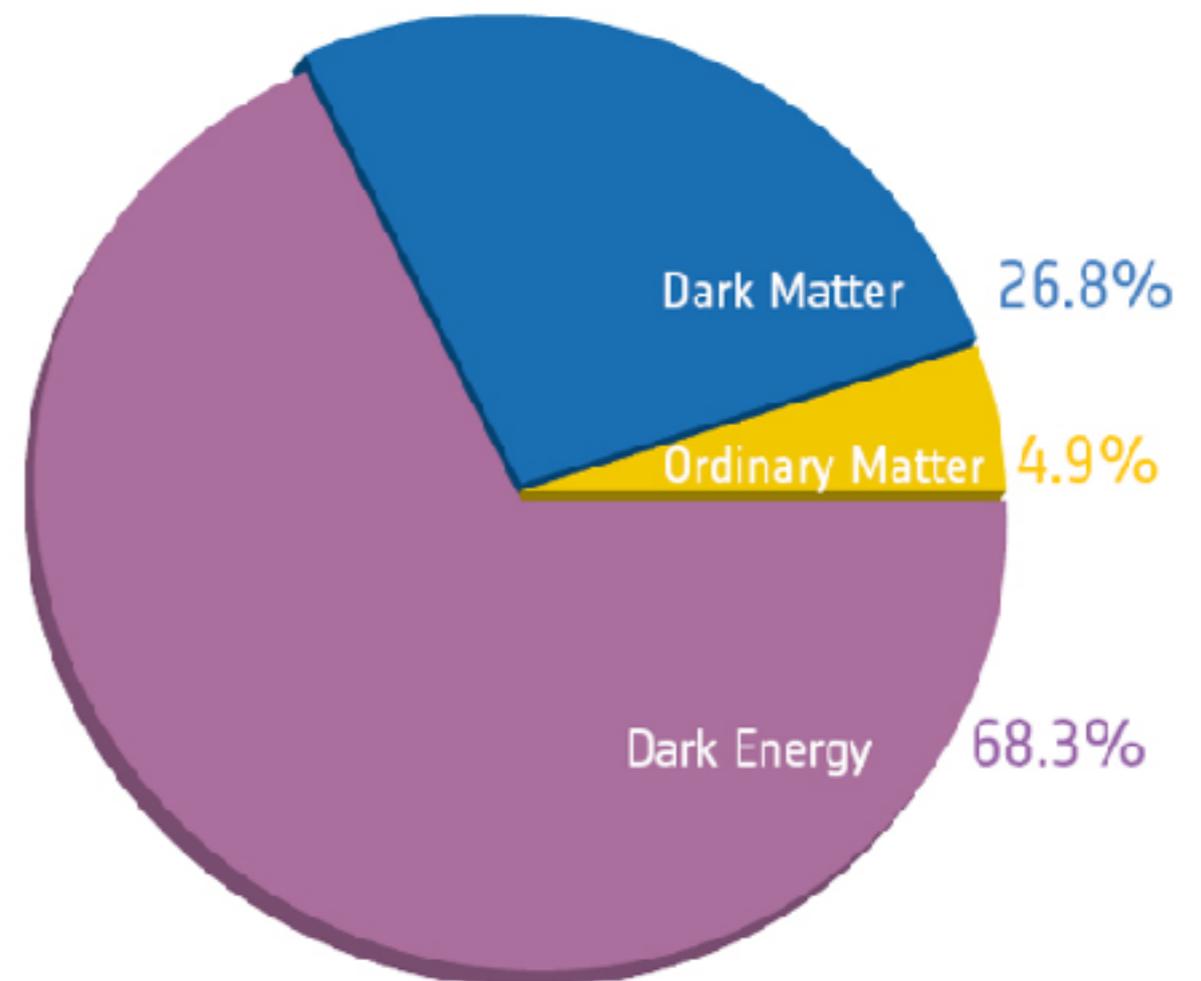
(ESA March 2013)

**$T \sim 2.73\text{K}$  black body with  $\sim 10^{-5}$  fluctuations**

# Cosmic Energy Budget

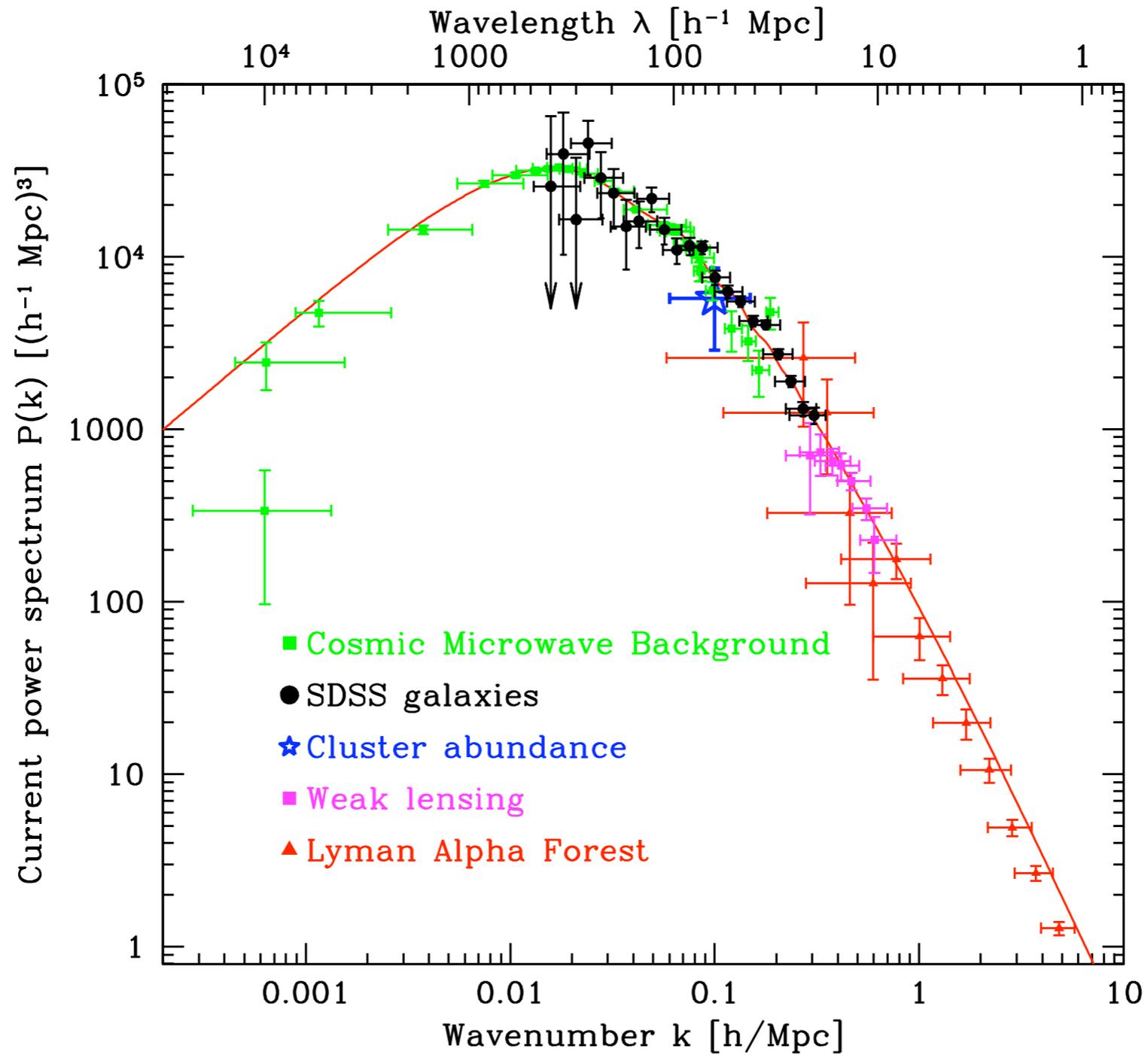


Before Planck

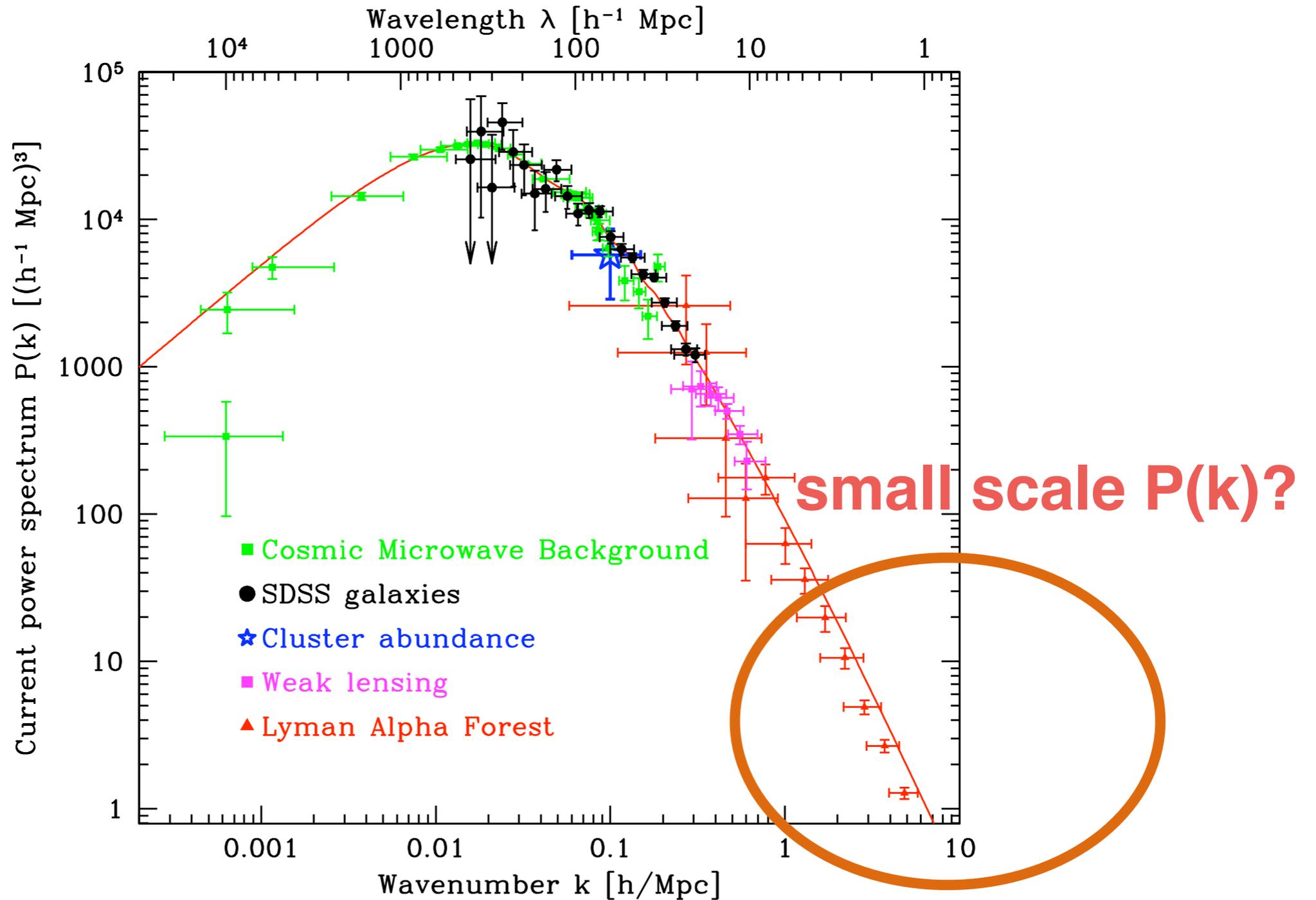


After Planck

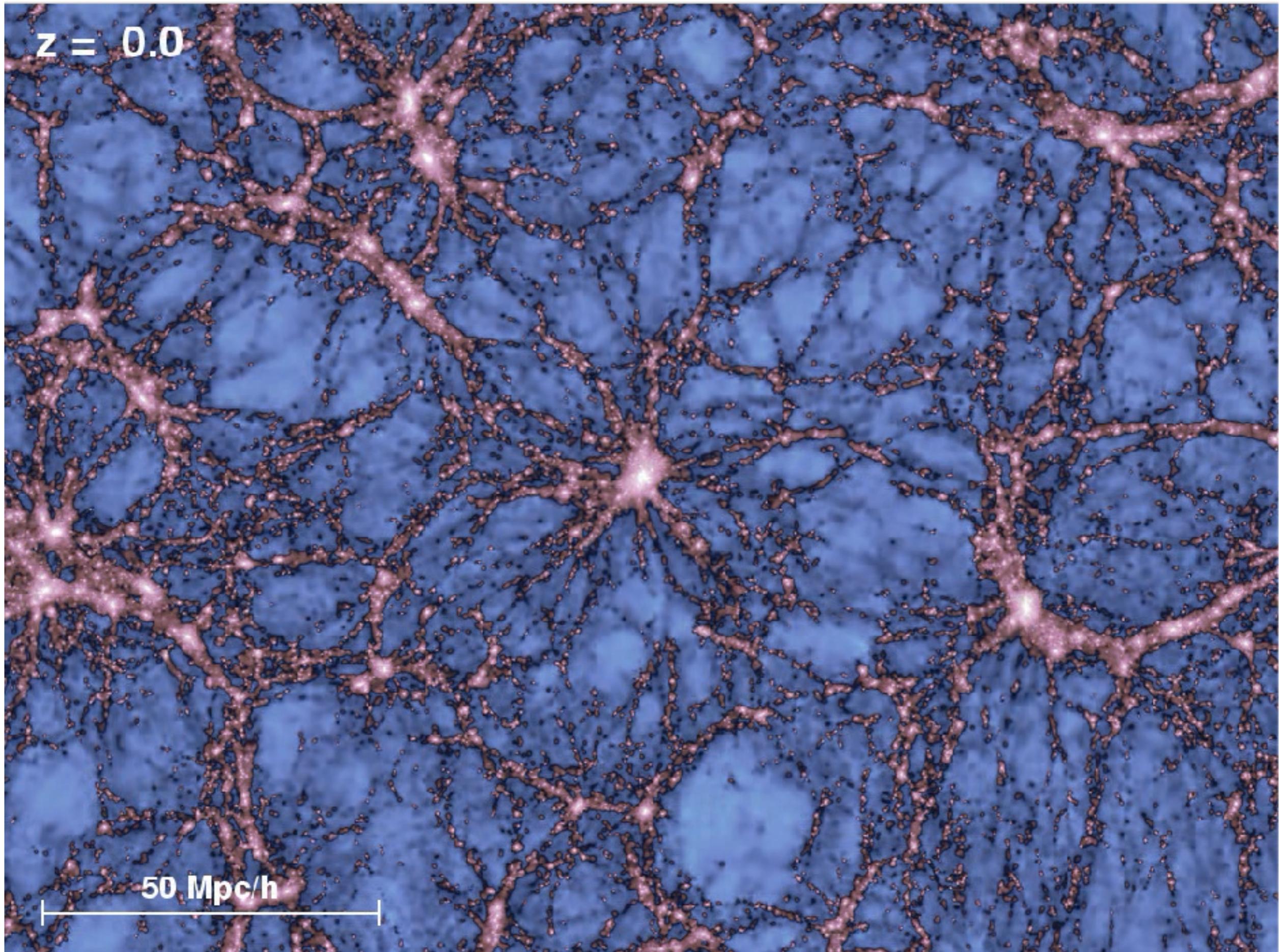
# Matter Power Spectrum



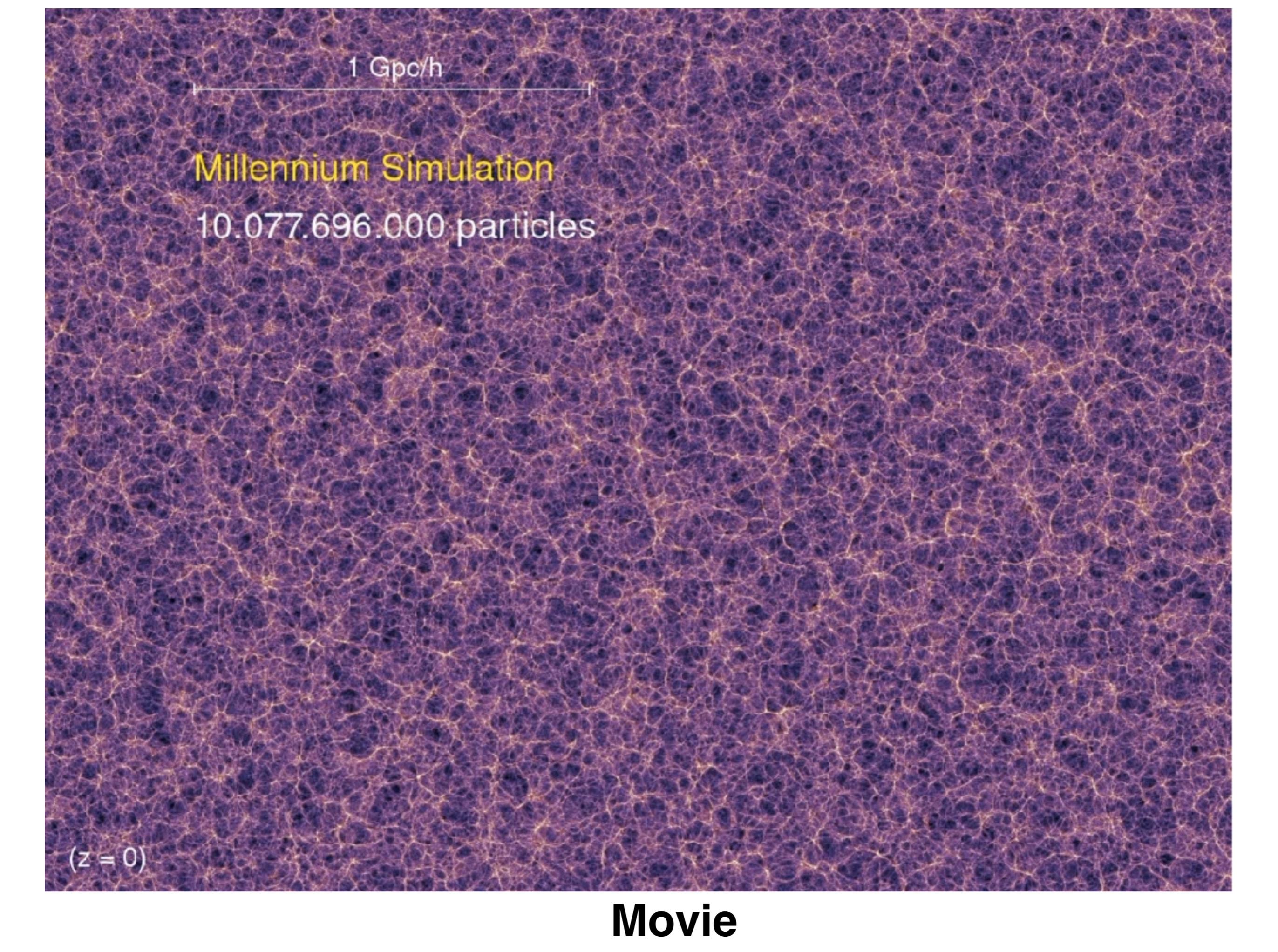
# Matter Power Spectrum



Tegmark 2004



**Movie**

A visualization of the Millennium Simulation, showing a dense network of particles in a dark purple and blue color scheme. The particles are arranged in a complex, interconnected pattern, representing the large-scale structure of the universe. A scale bar at the top indicates 1 Gpc/h. The text 'Millennium Simulation' and '10,077,696,000 particles' is overlaid on the image. The redshift value '(z = 0)' is shown in the bottom left corner.

1 Gpc/h

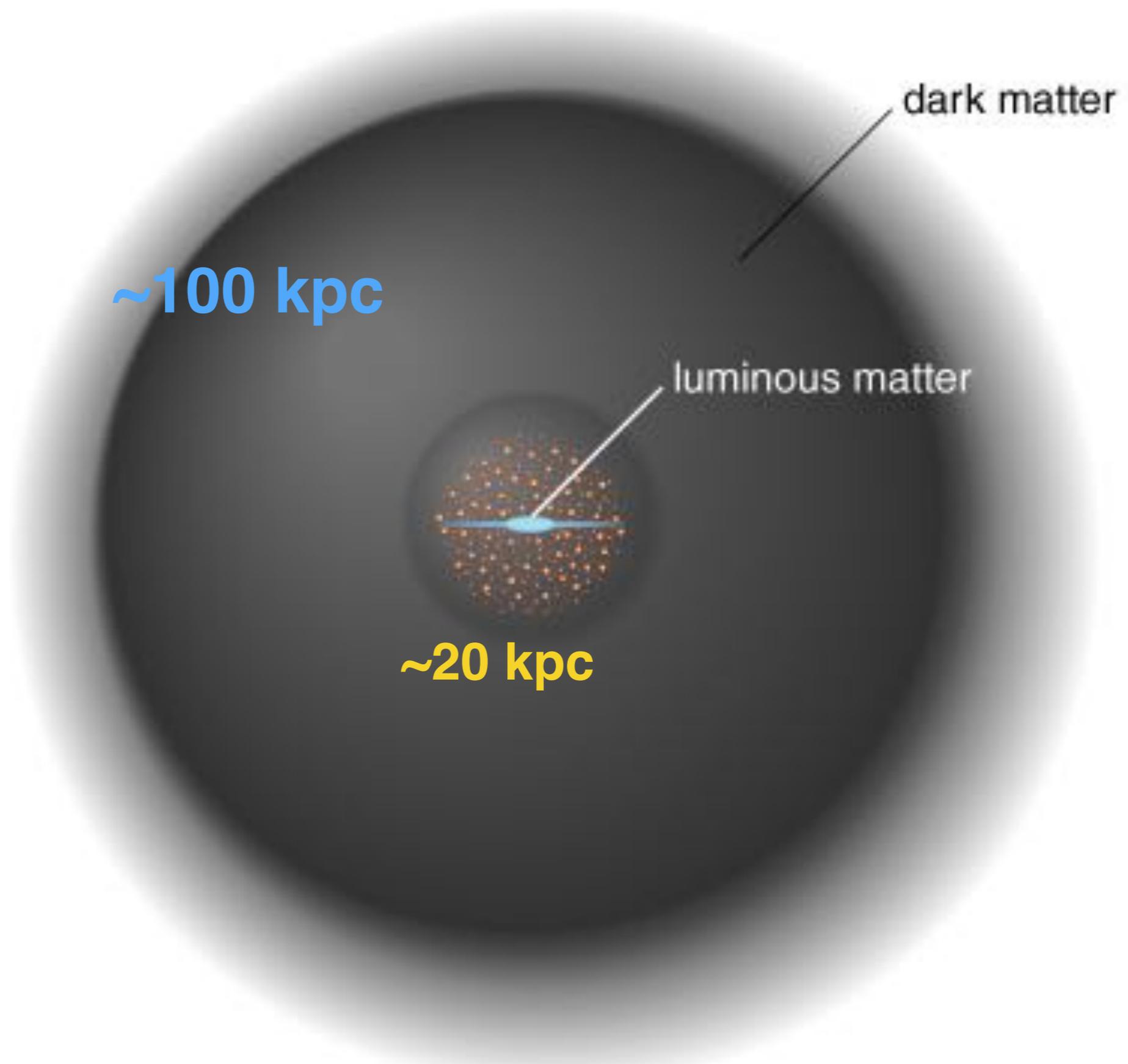
Millennium Simulation

10,077,696,000 particles

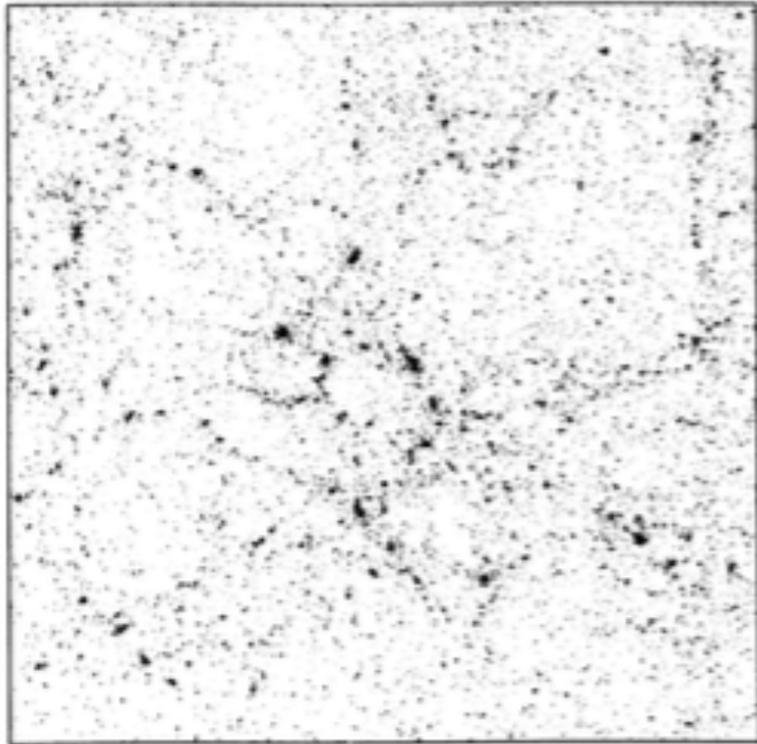
( $z = 0$ )

**Movie**

# Current simple picture of DM halo & galaxy

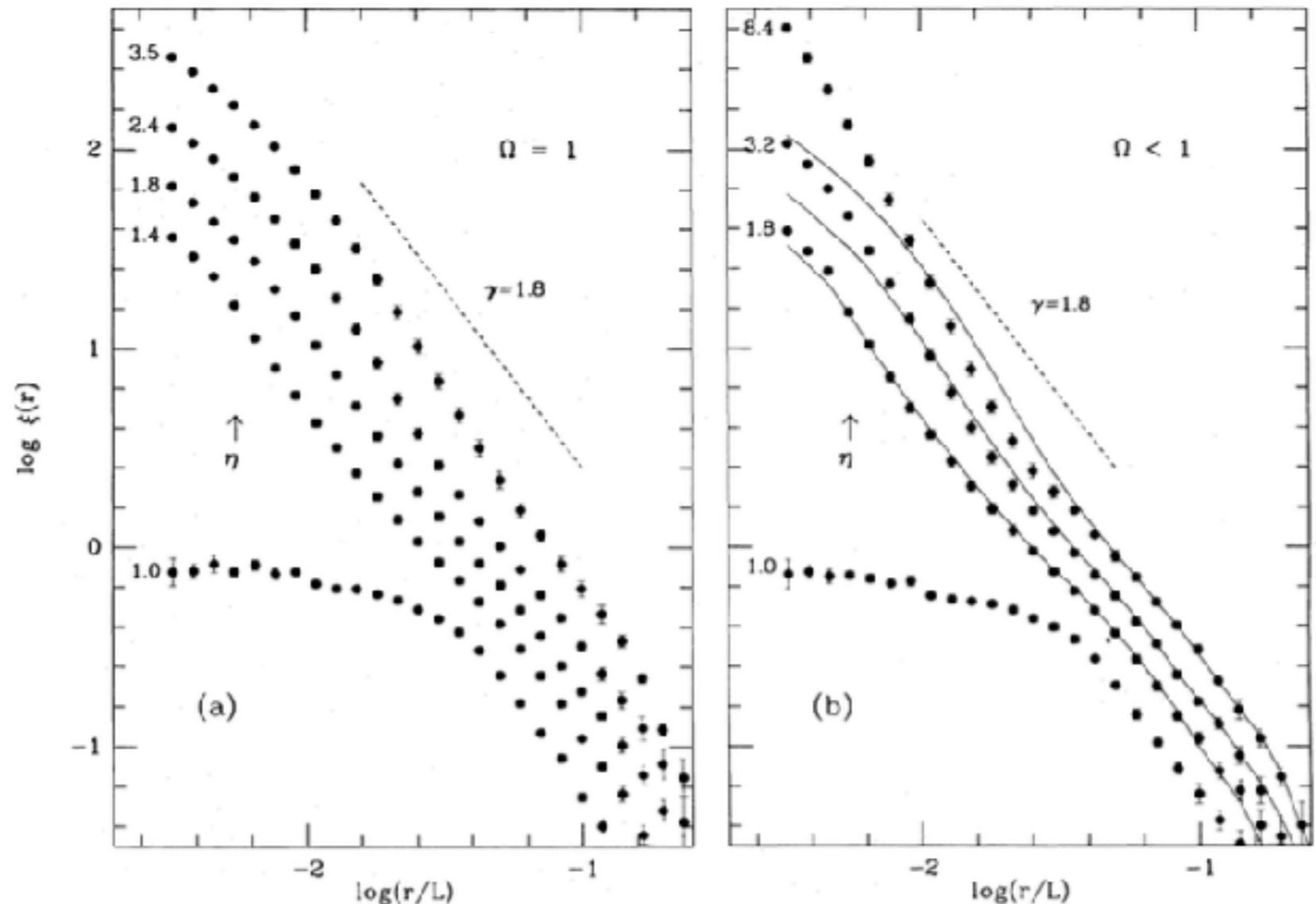


# Galaxy Correlation Function & Bias



Davis+'85

only  $32^3$  ptcl !!  
(N-body)



CDM simulation can explain galaxy clustering  
w/ the idea of “**bias**”

(Some possible)

## small-scale problems of $\Lambda$ CDM

- **Cusp-Core problem:** simulations predicting too steep inner halo profile
- **Missing satellites problem:** too much substructure?
- **Too-big-to-fail problem:** over-abundance of massive substructures that could host gals after reionization (but not observed in MW-satellites)
- **Void phenomenon:** gals in voids are too normal?
- **Satellites plane problem:** satellites aligned in a plane for both MW and Andromeda
- ....

# Dark matter halo cusp

Navarro-Frenk-White (NFW) profile

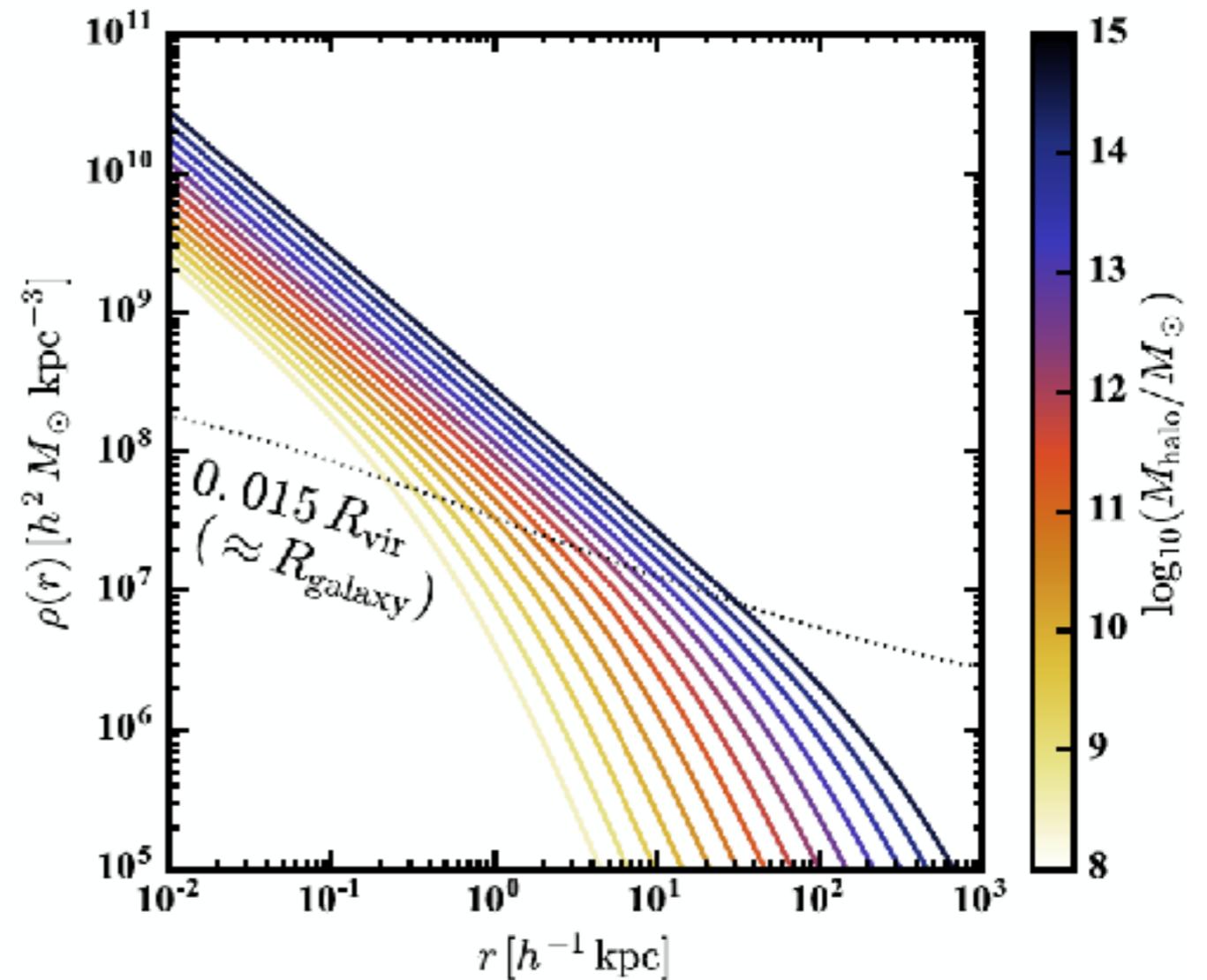
(NFW '96)

$$\rho(r) = \frac{4\rho_{-2}}{(r/r_{-2})(1+r/r_{-2})^2}$$

$$c = R_{\text{vir}}/r_{-2}$$

$$c \propto M_{\text{vir}}^{-a} (1+z)^{-1}$$

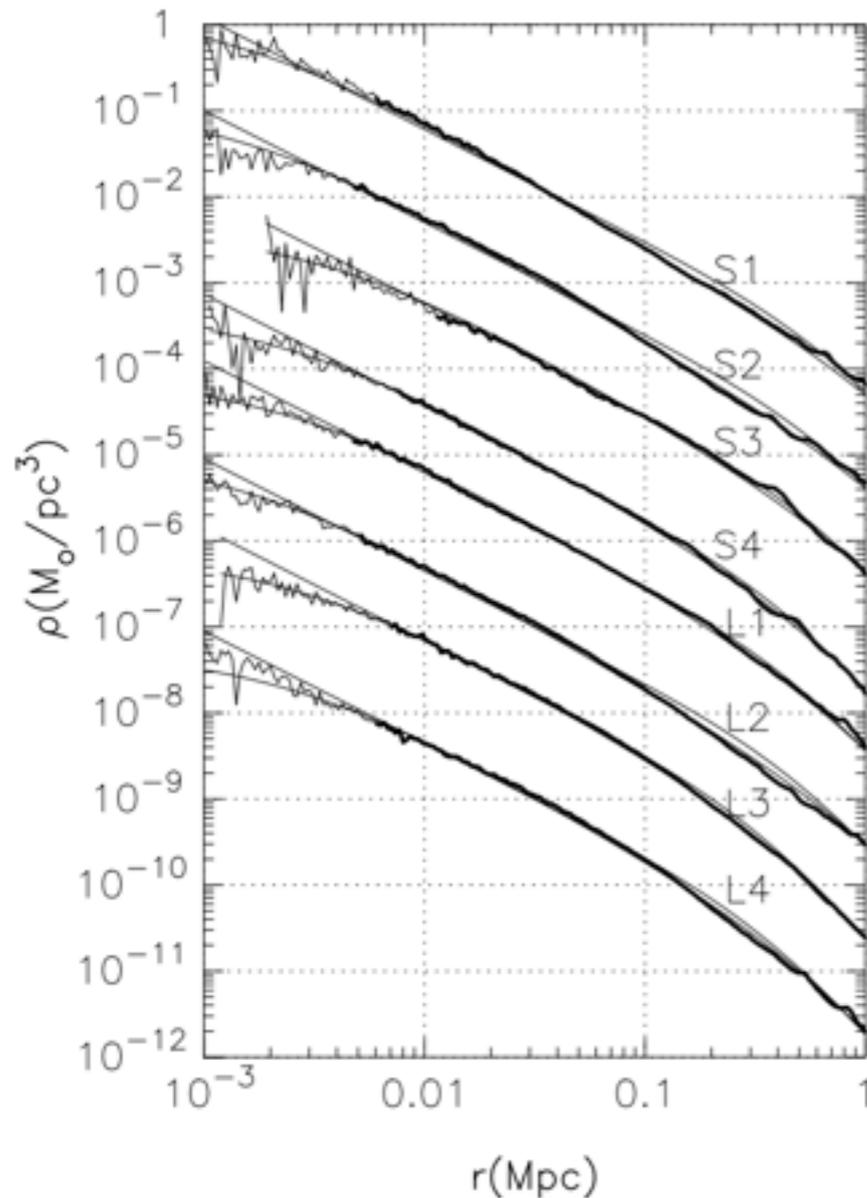
$$a \approx 0.1 \quad (\text{Bullock+'01})$$



Bullock & Boylan-Kolchin '17

But observed dwarf gals tend to have flat cores.

# Cuspy profile not universal?



**Fukushige+'14**

## Universal Profile:

NFW: MNRAS 275, 720 (1995): proposed NFW profile for x-ray clusters  
NFW: ApJ 462, 563 (1996)  
NFW: ApJ 490, 493 (1997): Appendix has useful formulae

## Papers supporting NFW profile:

Cole & Lacey, MNRAS 281, 716 (1996)  
Tormen, Bouchet, & White MNRAS 286, 865 (1997)  
Kravtsov, Klypin, & Khokhlov ApJS, 111, 73 (1997) (Code paper)  
Power et al., MNRAS 338, 14 (2003)

## Papers finding steeper profiles:

Fukushige & Makino, ApJ 447, J9 (1997)  
Moore et al., ApJ 499, L5 (1998)  
Moore et al., MNRAS 310, 1147 (1999)  
Ghigna et al., ApJ 544, 616 (2000)  
Klypin et al., ApJ 554, 903 (2001)  
Fukushige & Makino, ApJ 557, 533 (2001)

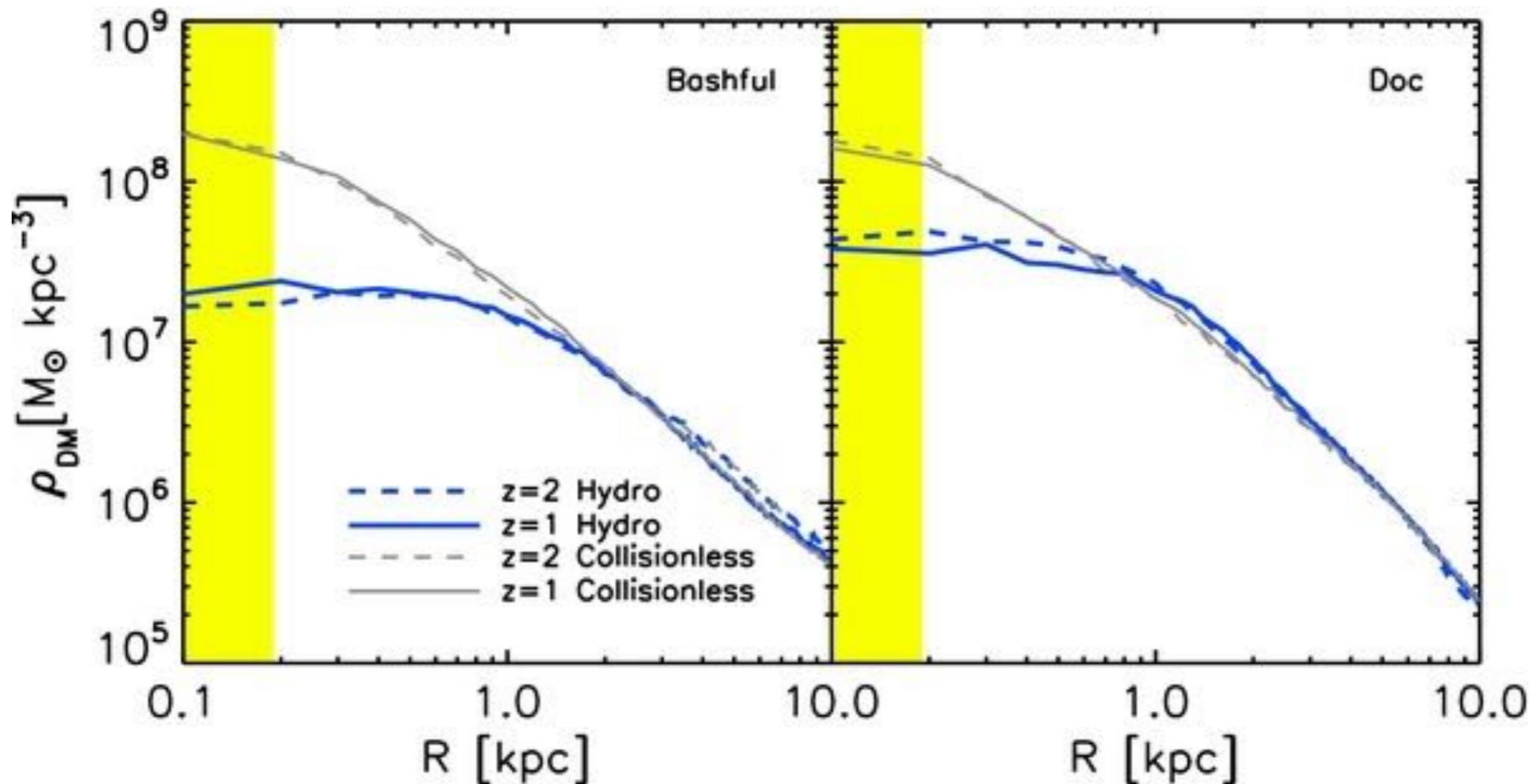
## Papers finding shallower profiles:

Kravtsov et al., ApJ 502, 48 (1998) (but later "retracted" by Klypin et al 2001)

## Papers finding not-so-universal profiles:

Jing & Suto ApJ 529, L69 (2000)  
Jing, ApJ 535, 30 (2000)  
Fukushige, Kawai, & Makino, astro-ph/0306203 (2003)  
Hayashi et al., astro-ph/0310576 (2003)

# Supernova-driven gas outflows can remove DM cusps and create kpc-size cores



(Results of zoom-in hydro sim.)

So, is CDM just fine?

Madau+'14

# Substructure problem?

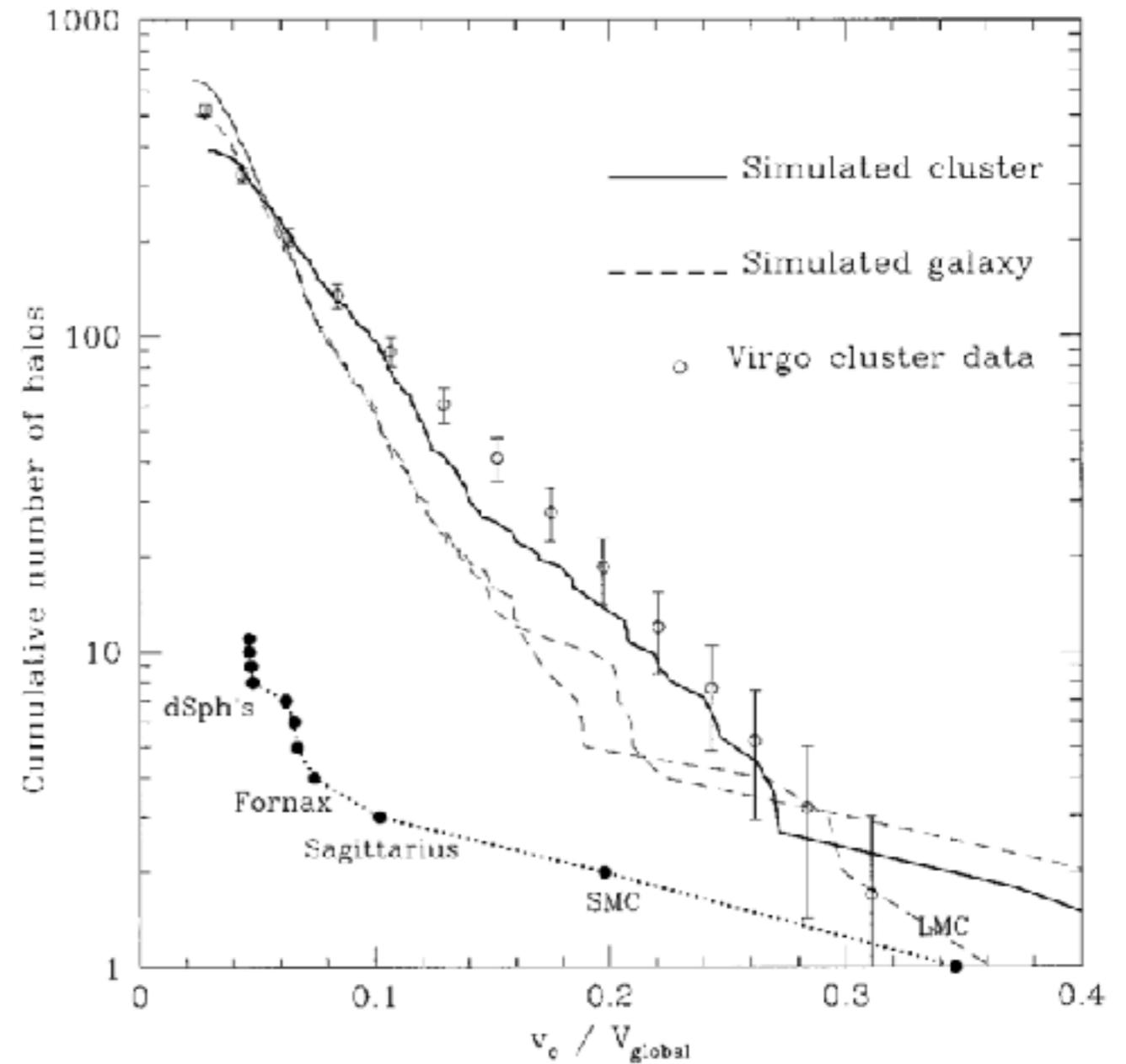
**$z=11.9$**

**800 x 600 physical kpc**

**Diemand, Kuhlen, Madau 2006**

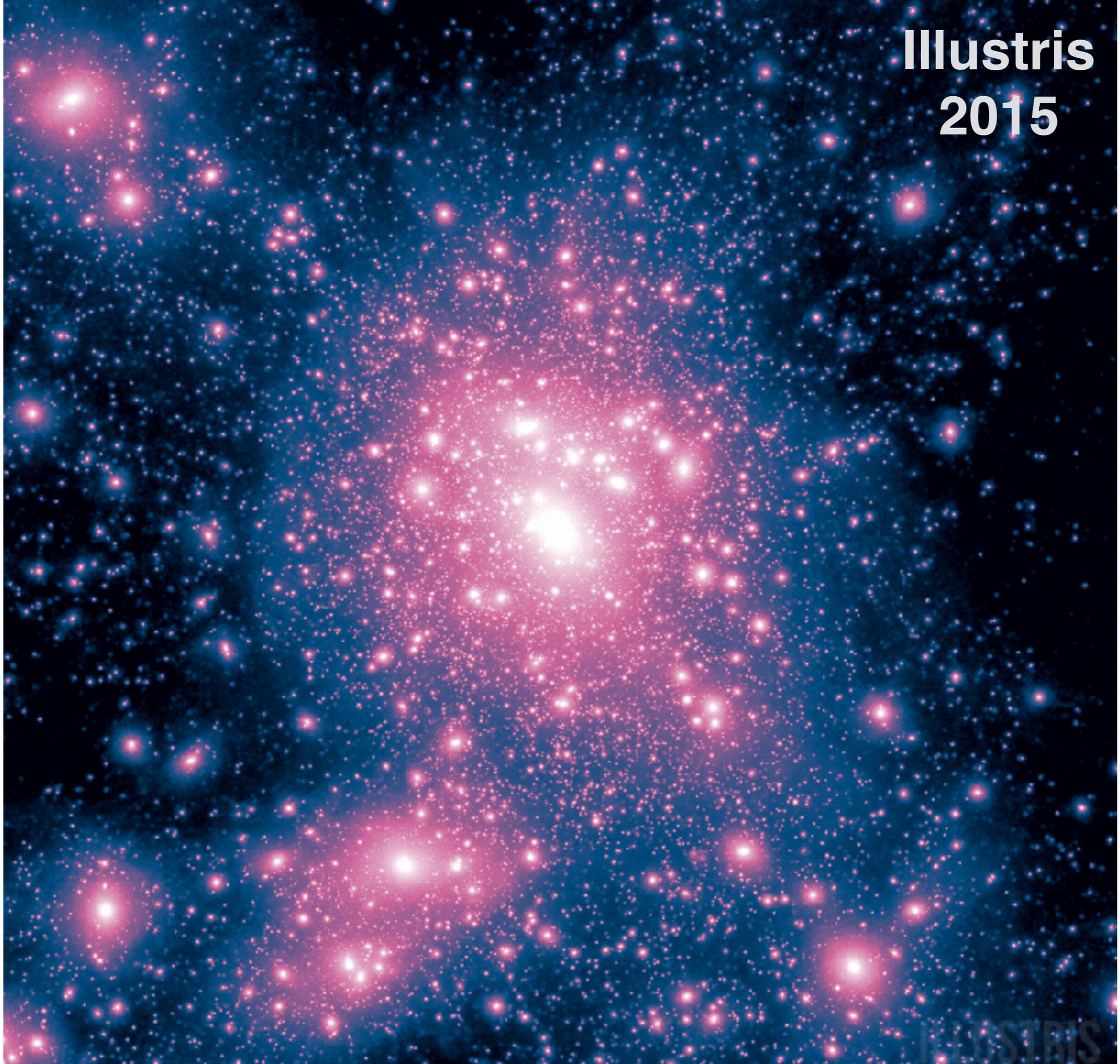
**Movie**

# Original Substructure Problem



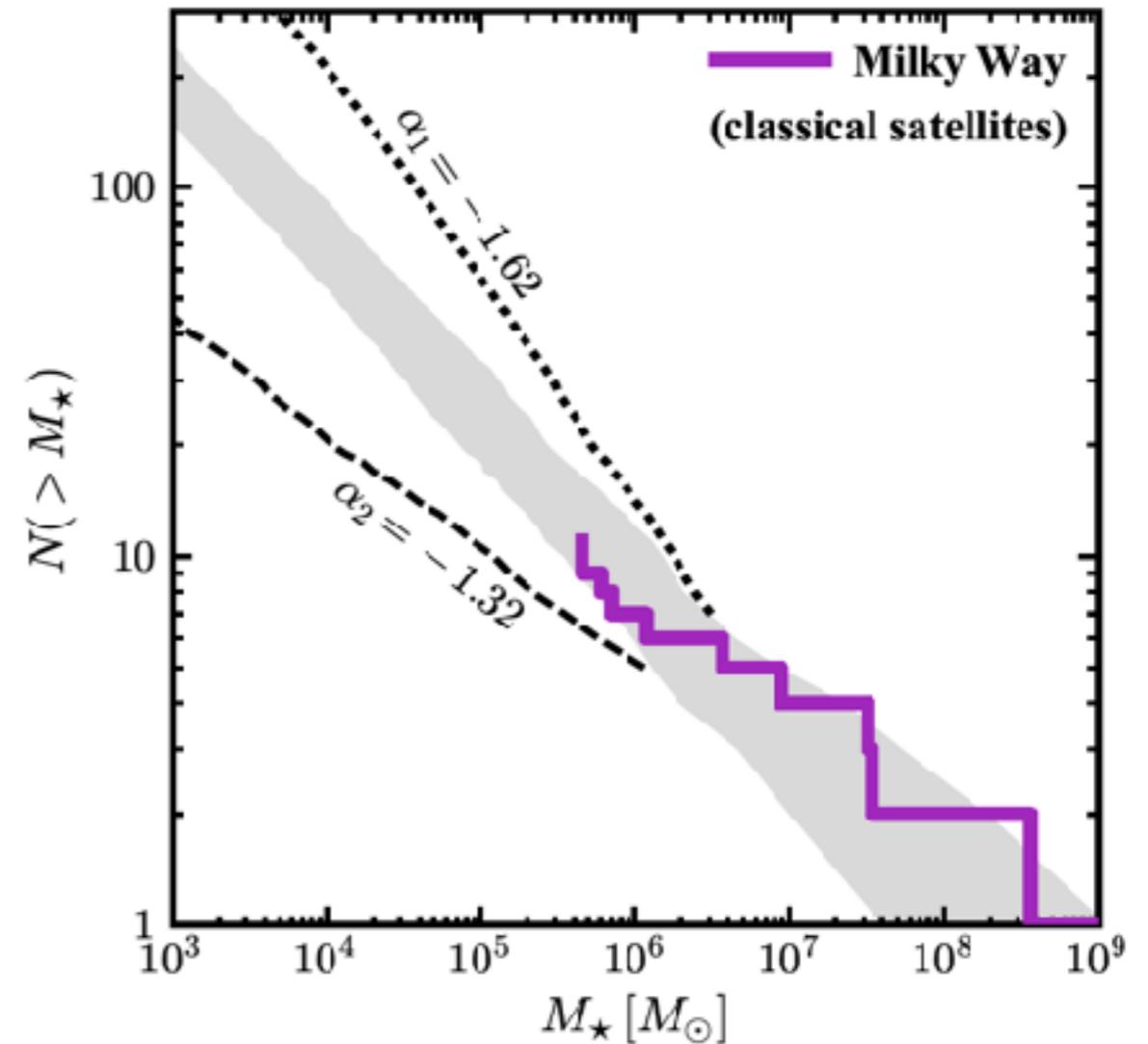
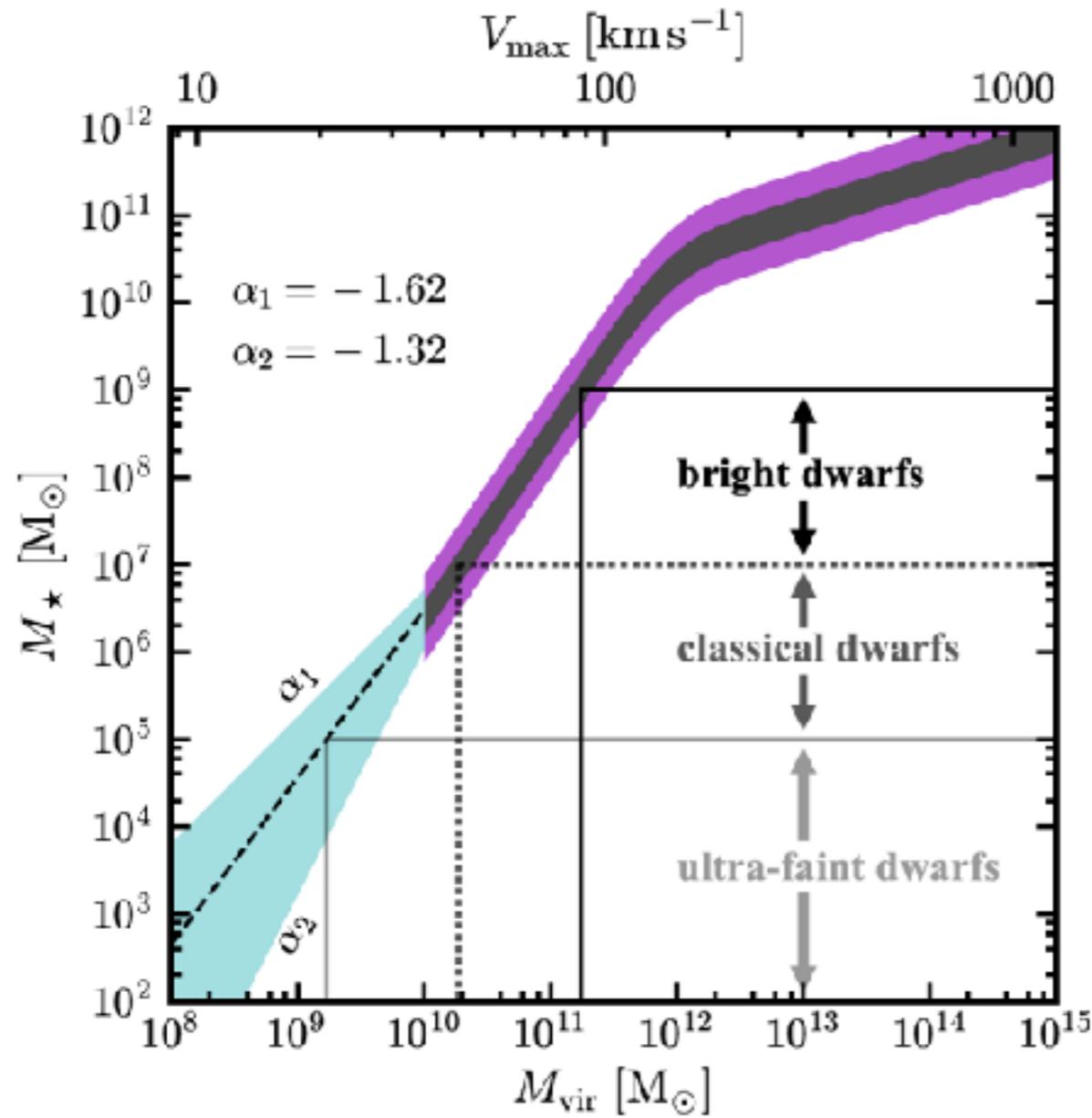
Klypin+'99; Moore+'99

# Illustris 2015



ILLUSTRIS

# Substructure Problem Solved?



Garrison-Kimmel+'17

Bullock & Boylan-Kolchin '17

# No Missing Satellite Problem?

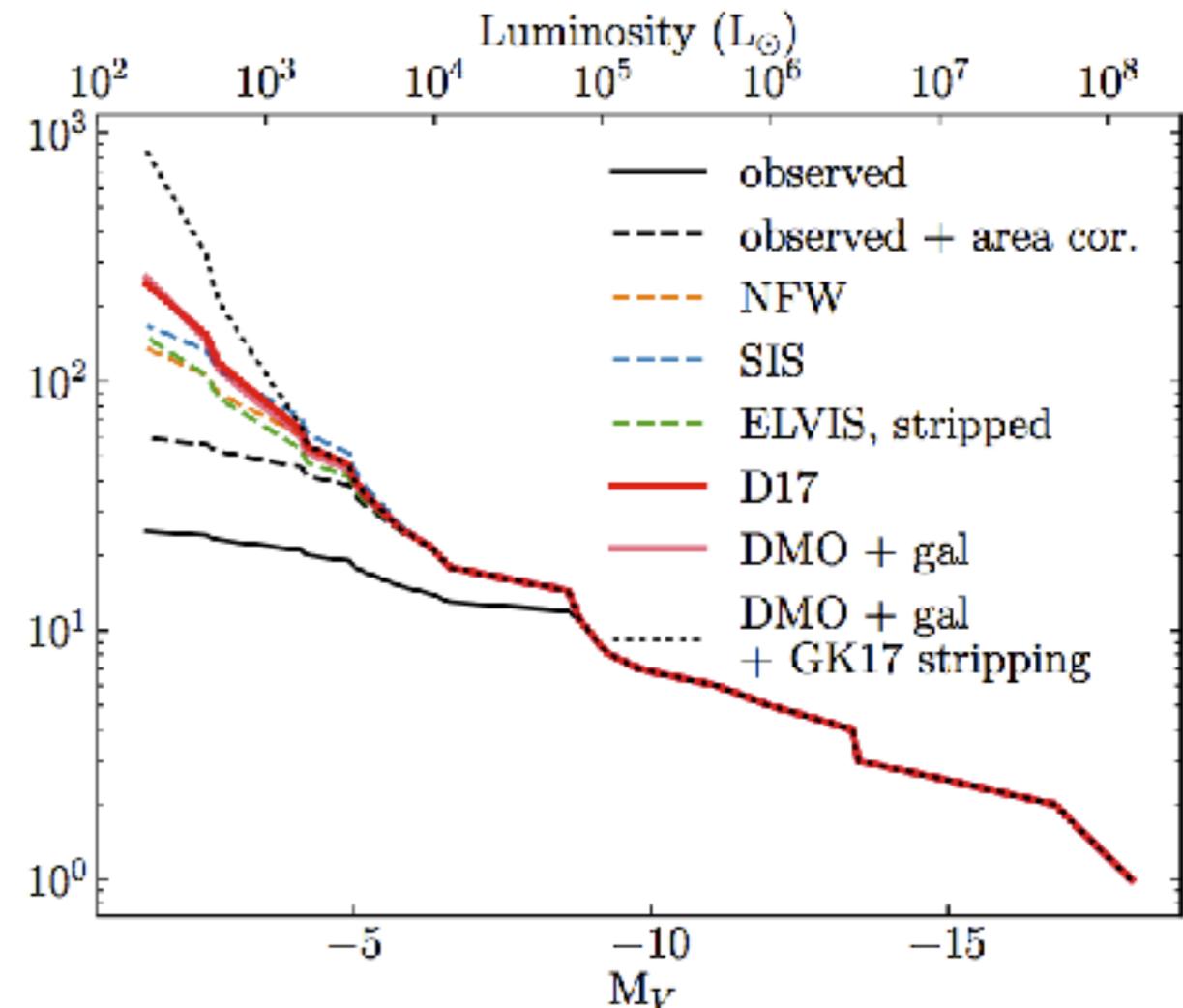
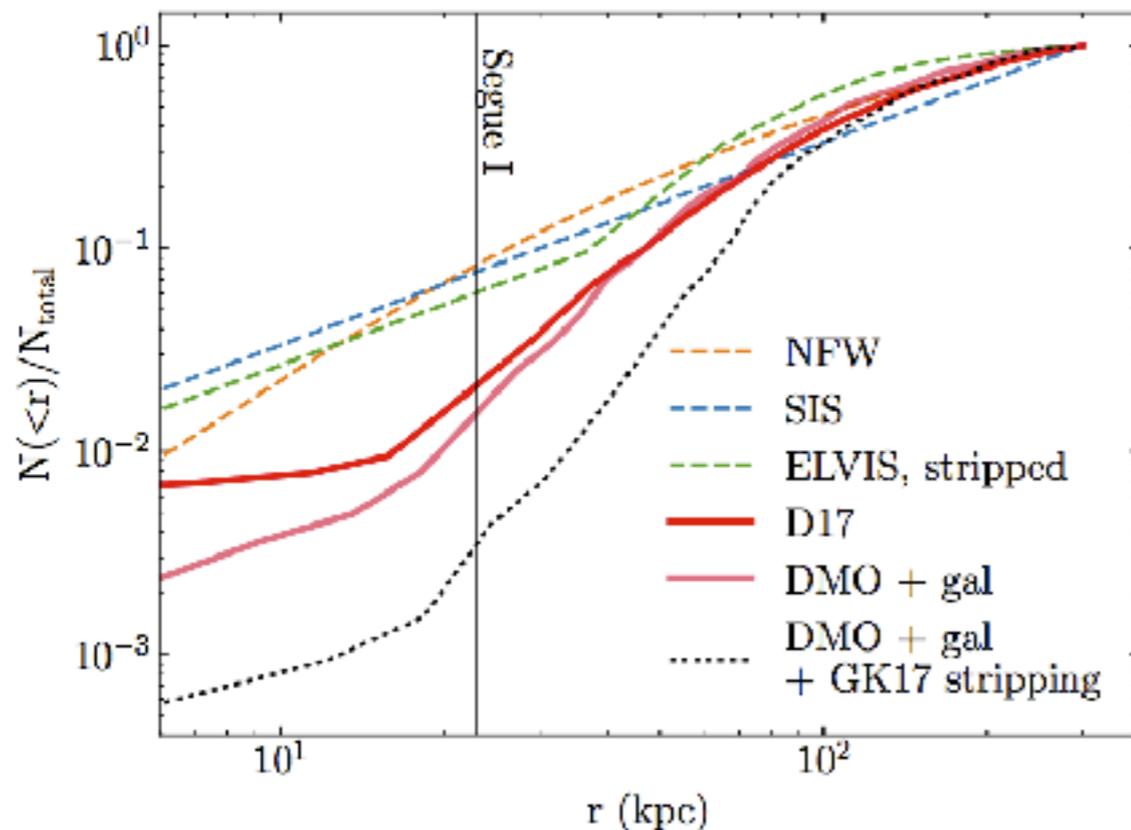
There is No Missing Satellites Problem

arXiv:1711.06267

Stacy Y. Kim<sup>1,2,\*</sup>, Annika H. G. Peter<sup>1,2,3</sup>, and Jonathan R. Hargis<sup>4</sup>

$$N_{\text{tot}} = \int c(L) \frac{dN_{\text{obs}}}{dL} dL \approx \sum_{i=1}^{N_{\text{obs}}} c(L_i), \quad c(L) = c_r(L) c_{\Omega}(L)$$

$$c_r(L) = \frac{\int_0^{R_{\text{vir}}} \frac{dN}{dr} dr}{\int_0^{r_c(L)} \frac{dN}{dr} dr} \quad \text{and} \quad c_{\Omega} = \frac{4\pi}{\int_0^{\Omega_c} d\Omega}$$



# Various Dark Matter

Cold Dark Matter  
(CDM):

$$m \sim 100 \text{ GeV},$$
$$v_{\text{th}}^{z=0} \approx 0 \text{ km s}^{-1}$$

***Thermal relic***

e.g. WIMP (weakly interacting massive ptcl)

Warm Dark Matter  
(WDM):

$$m \sim 1 \text{ keV},$$
$$v_{\text{th}}^{z=0} \sim 0.03 \text{ km s}^{-1}$$

becomes non-relativistic earlier, suppress  
perturbation at galactic or smaller scales.

(gravitino, steril neutrino,...)

Hot Dark Matter  
(HDM):

$$m \sim 1 \text{ eV},$$
$$v_{\text{th}}^{z=0} \sim 30 \text{ km s}^{-1}$$

remains relativistic until late time, and  
erase structures at super-galactic scales.

**+FDM (axion-like)**

# So, how about WDM?

e.g., gravitino (Kawasaki+'97)  
sterile neutrino  $\sim$  keV (BoyarSKI+'09)

**Thermal relic; Streaming velocity  $v_s/c \sim T_x/m_x$**

$$R_s \approx 0.31 \left( \frac{\Omega_X}{0.3} \right)^{0.15} \left( \frac{h}{0.65} \right)^{1.3} \left( \frac{\text{keV}}{m_X} \right)^{1.15} h^{-1} \text{ Mpc}$$

$m \sim 1.5 \text{ keV} \Rightarrow R_s \sim 0.3 \text{ Mpc}/h$   
Bode+'01

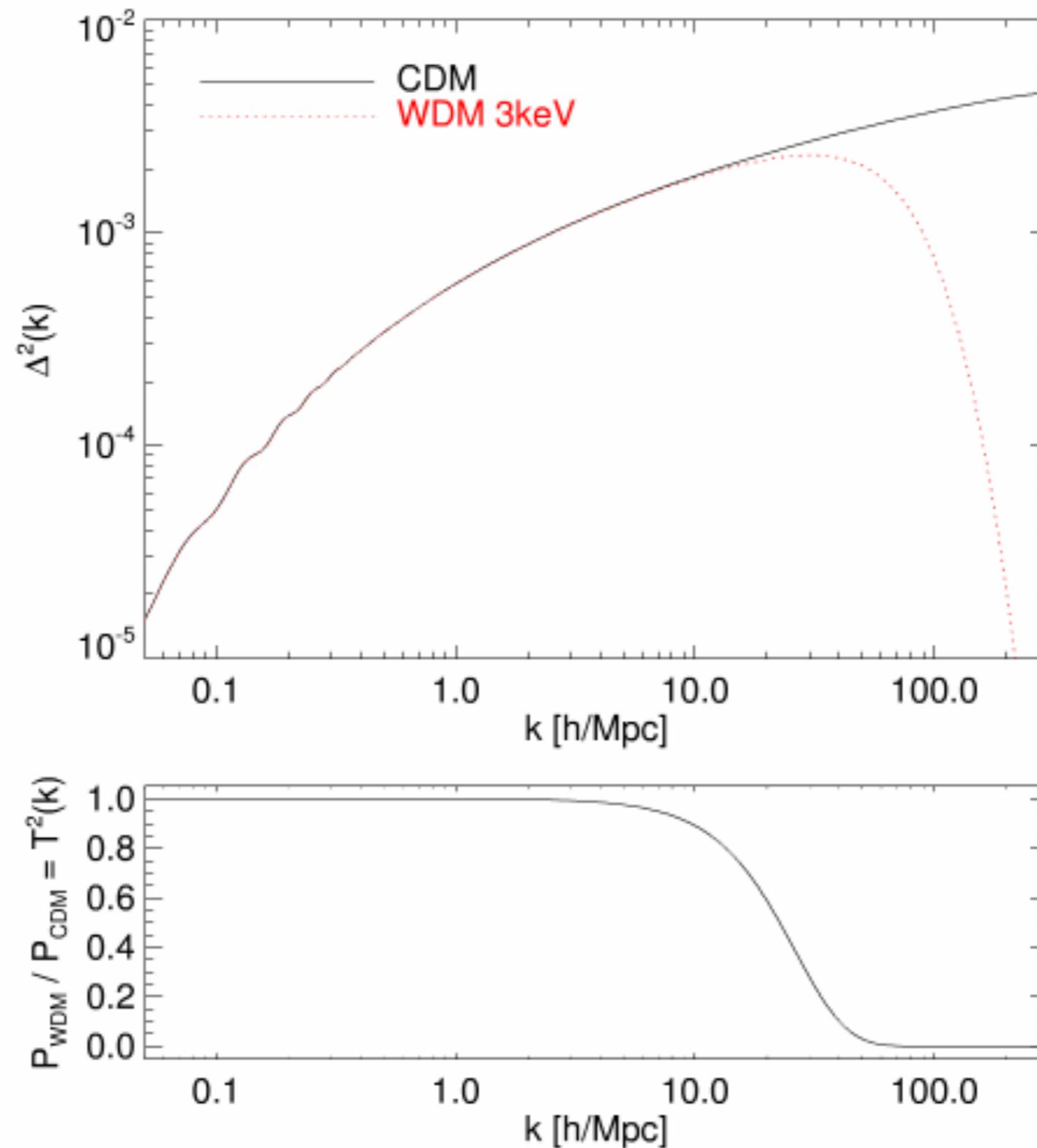
$$T_{\text{lin}}^2(k) \equiv P_{\text{WDM}}(k)/P_{\Lambda\text{CDM}}(k) = [1 + (\alpha k)^{2\nu}]^{-10/\nu},$$
$$\alpha(m_{\text{WDM}}) = 0.049 \left( \frac{1 \text{ keV}}{m_{\text{WDM}}} \right)^{1.11} \left( \frac{\Omega_{\text{WDM}}}{0.25} \right)^{0.11} \left( \frac{h}{0.7} \right)^{1.22}$$

Viel+'12

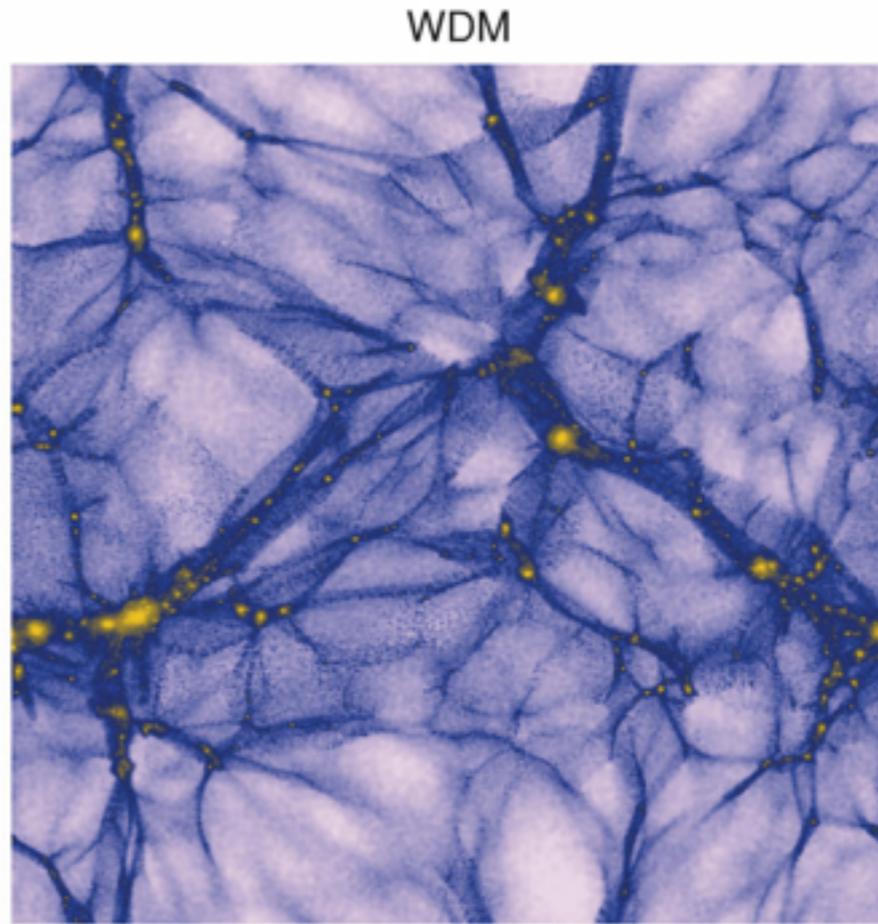
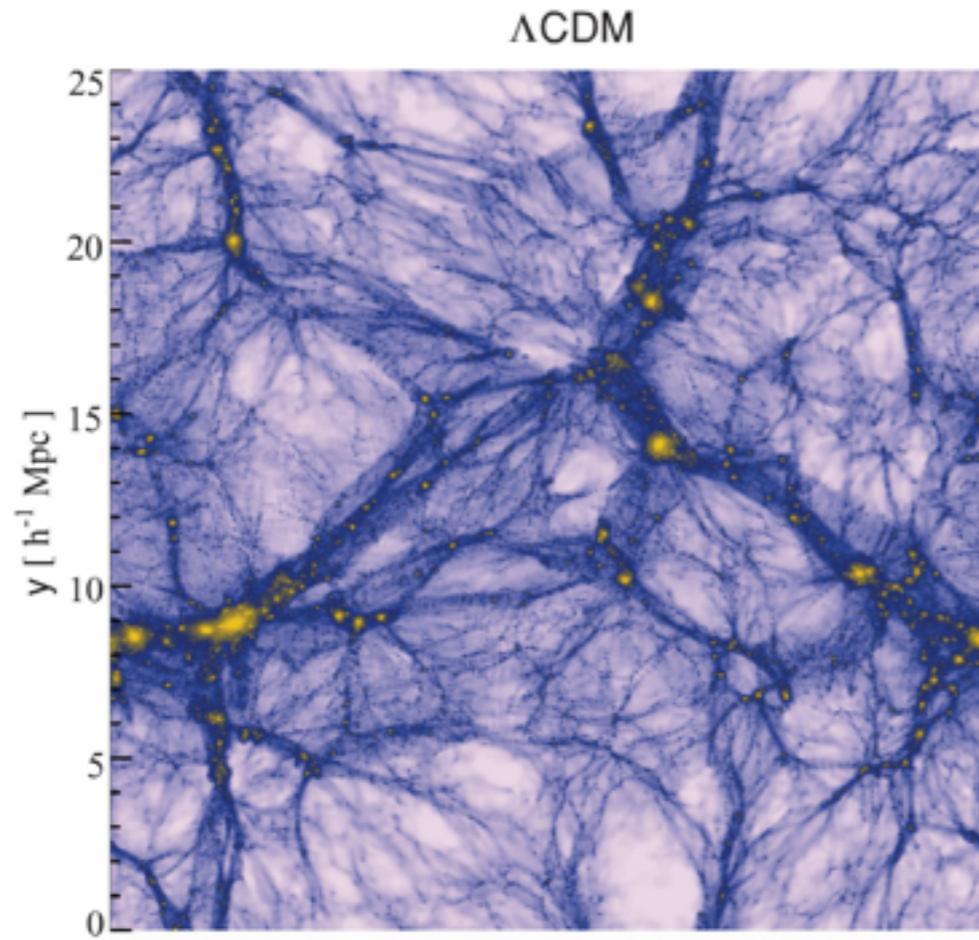
**half-mode mass**  $M_{\text{hm}} = 5.5 \times 10^{10} \left( \frac{m_{\text{WDM}}}{1 \text{ keV}} \right)^{-3.33} M_{\odot}$  Schneider+'12

Colin+'00; Bode+'01; Viel+'05; Colin+'08; Colombi+'09; Viel+'12; Menci+'17

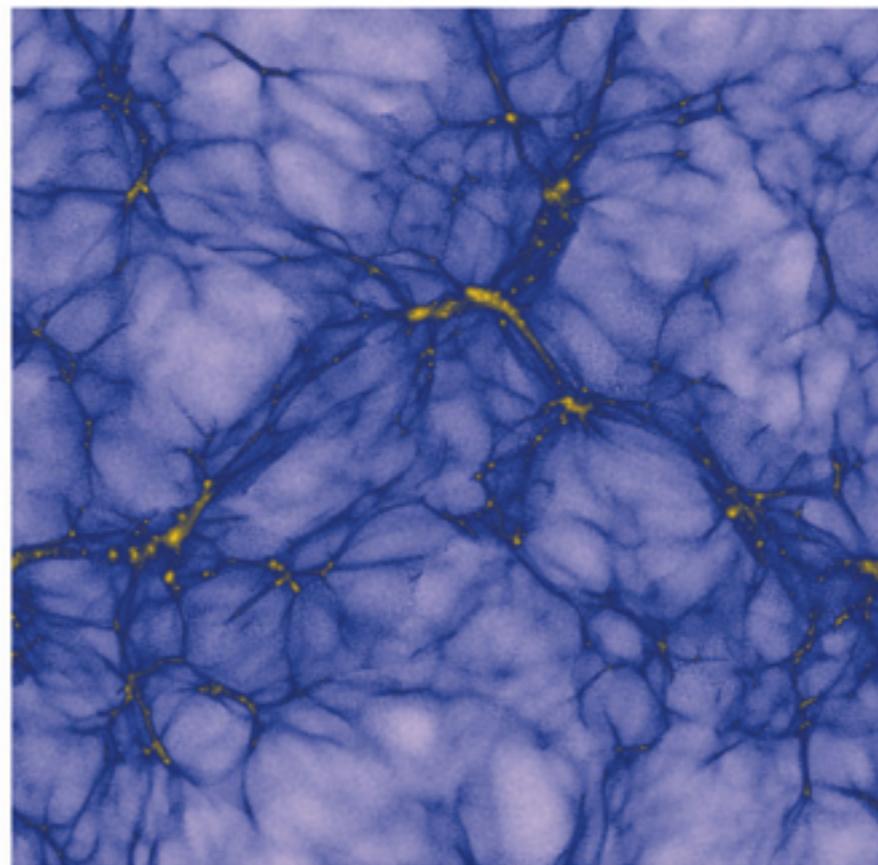
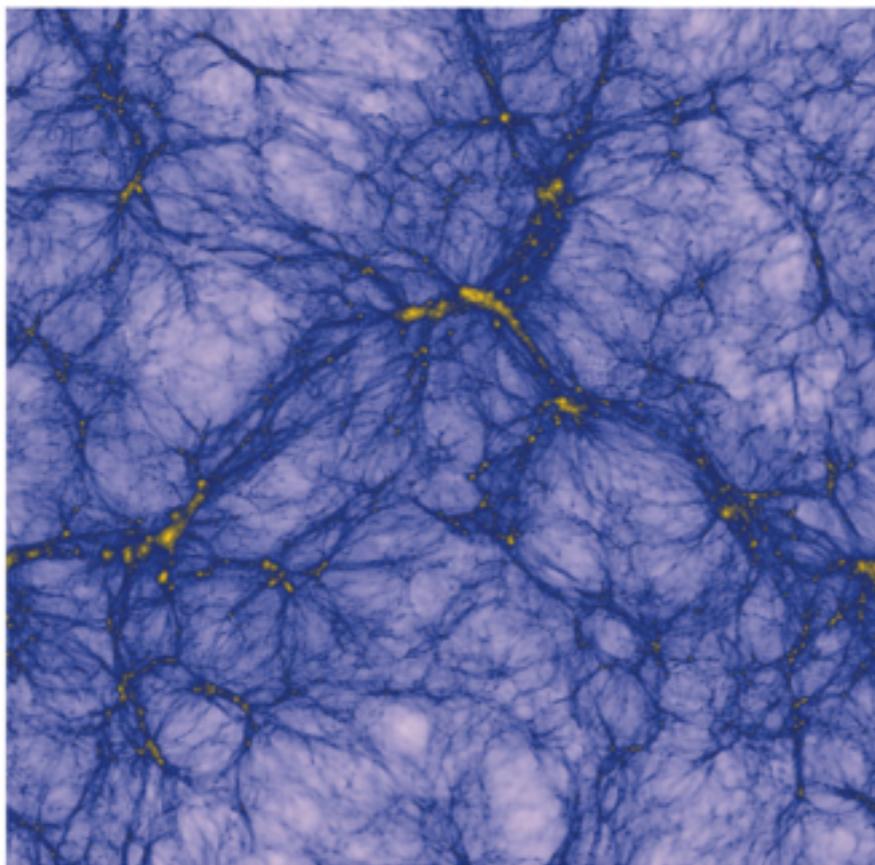
# Suppression of $P(k)$ @ small scales



**z=0**



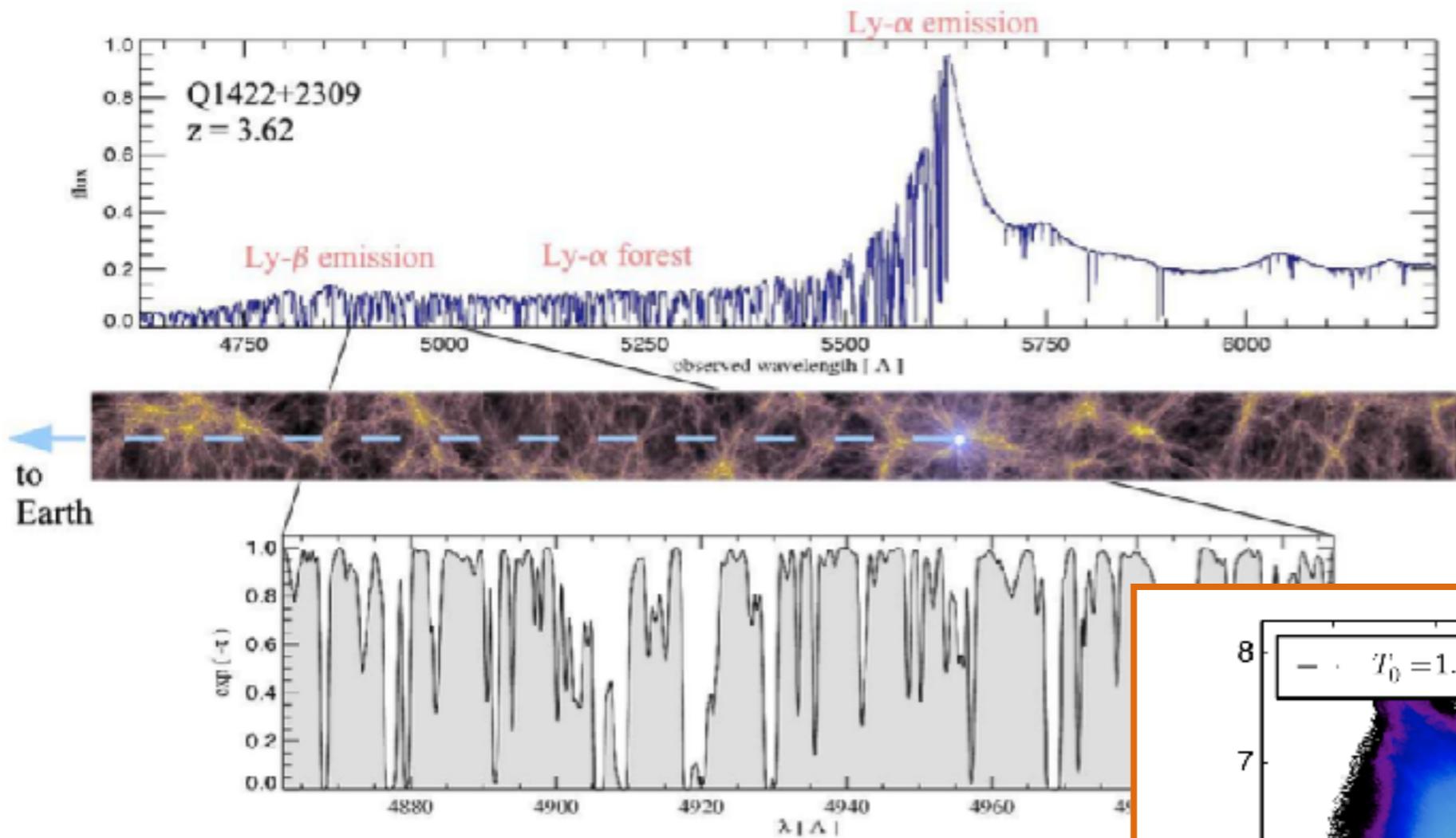
**z=2**



**m=1 keV**

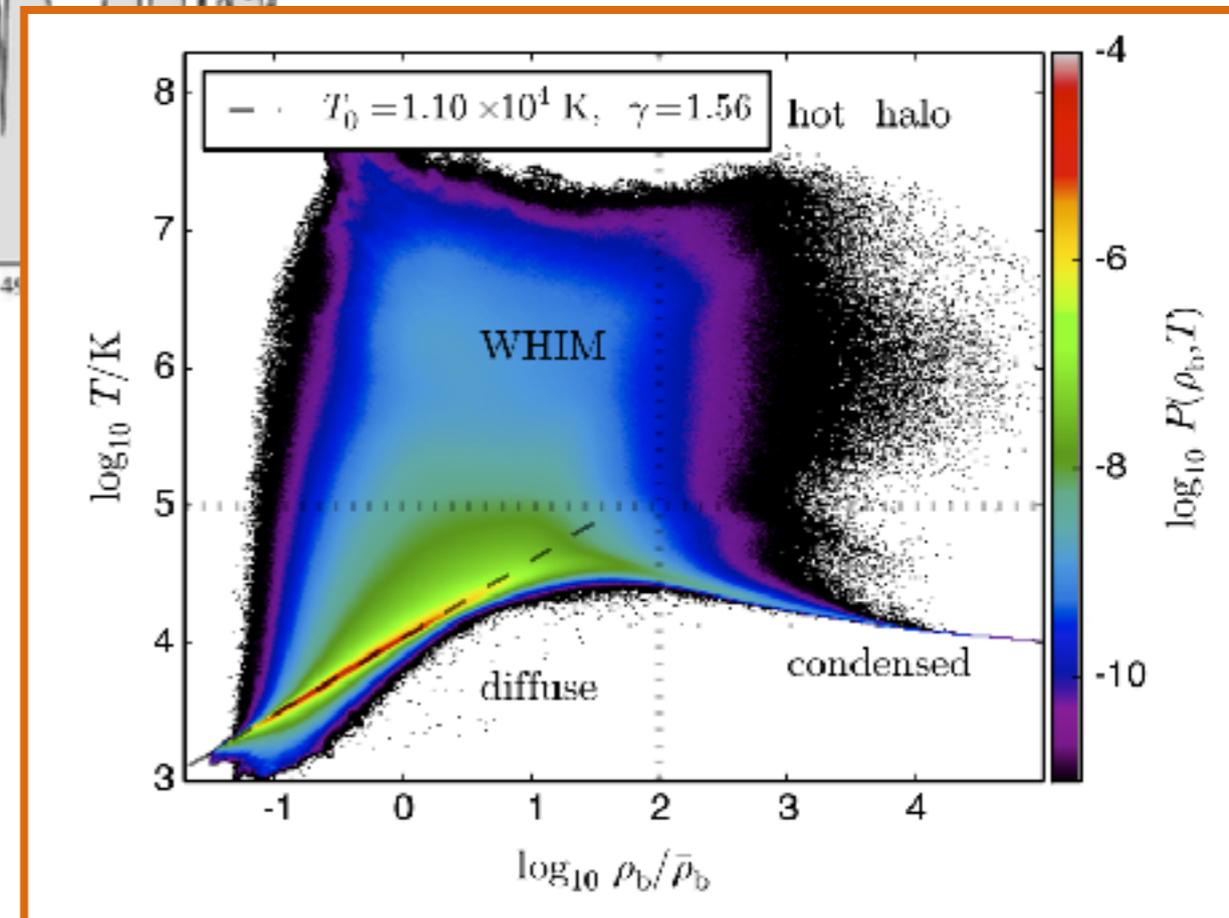
**Viel+'12**

# Quasars (QSOs) and Ly- $\alpha$ forest

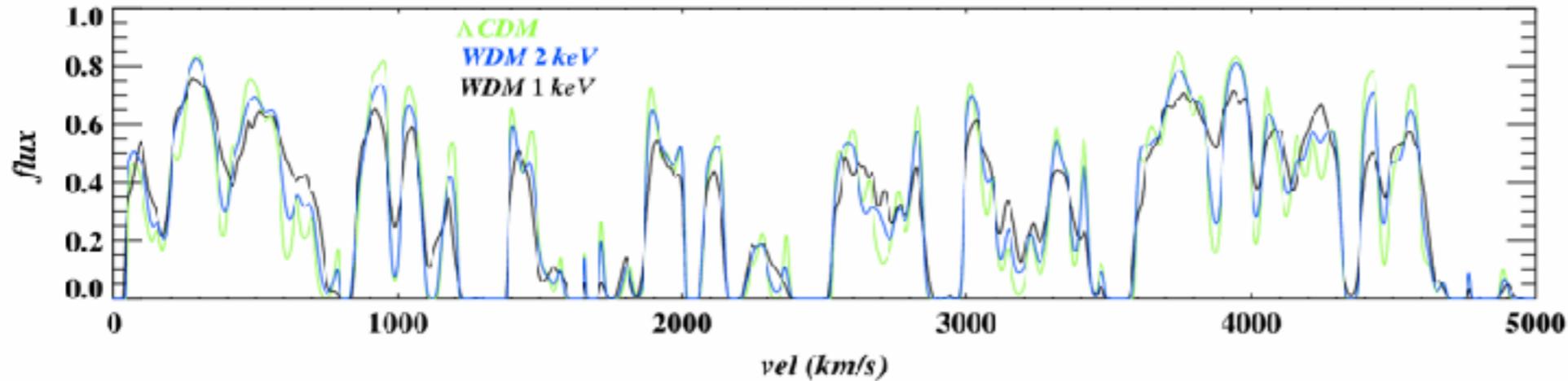


Springel+'05  
(cf. Cen+'94)

Lukic+16



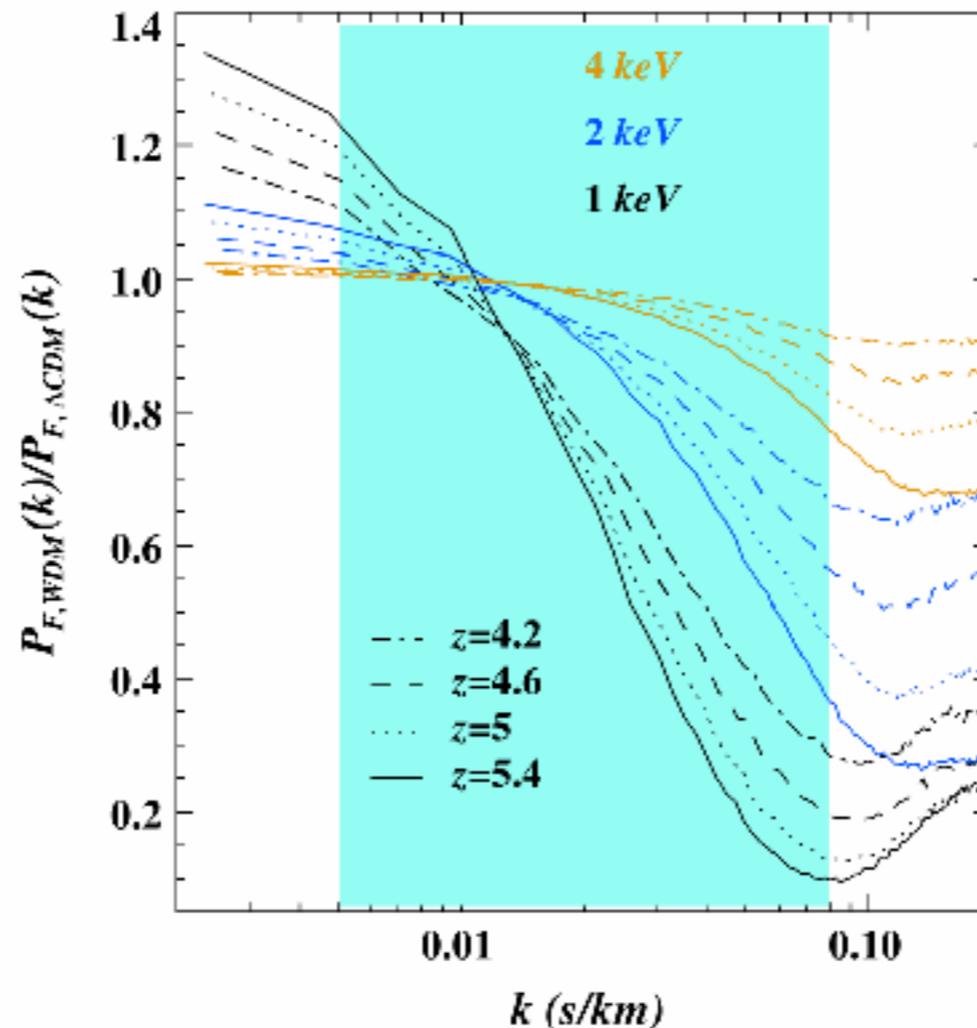
# Ly- $\alpha$ forest constraint



$$T = T_0(1 + \delta)^{\gamma-1}$$

**1D flux  
power spec**

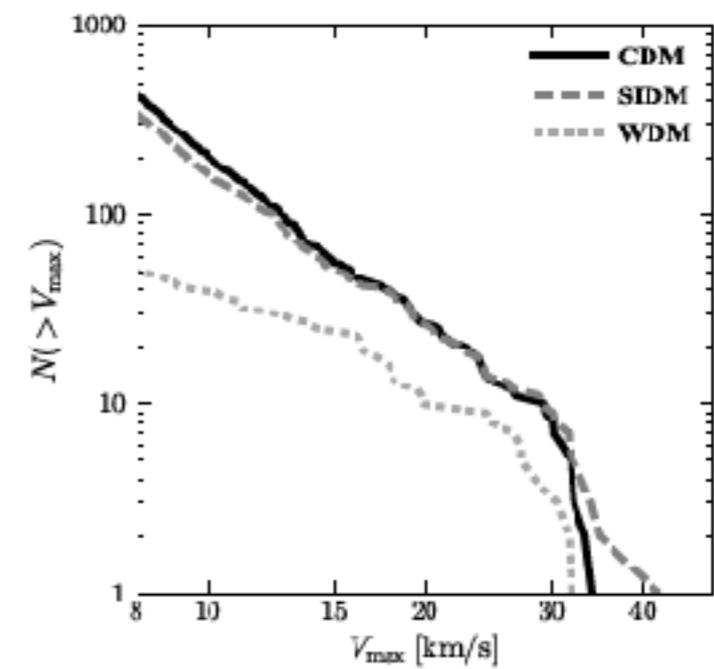
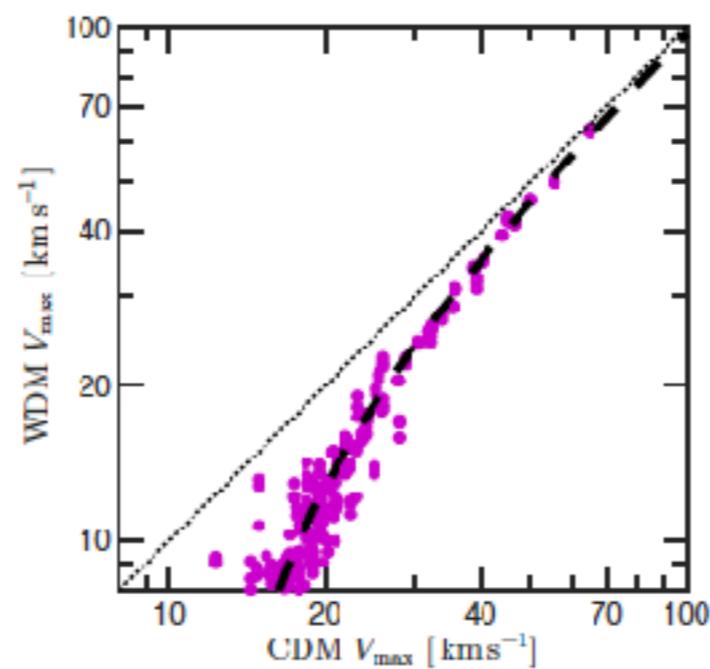
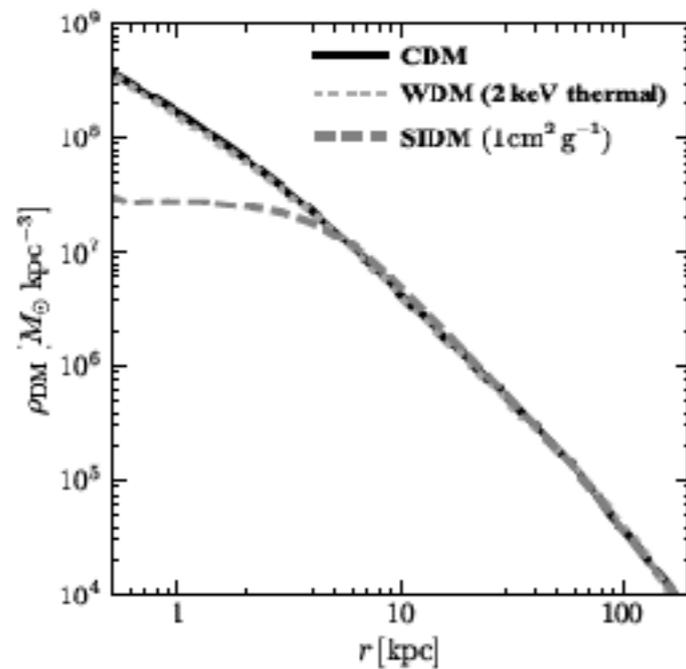
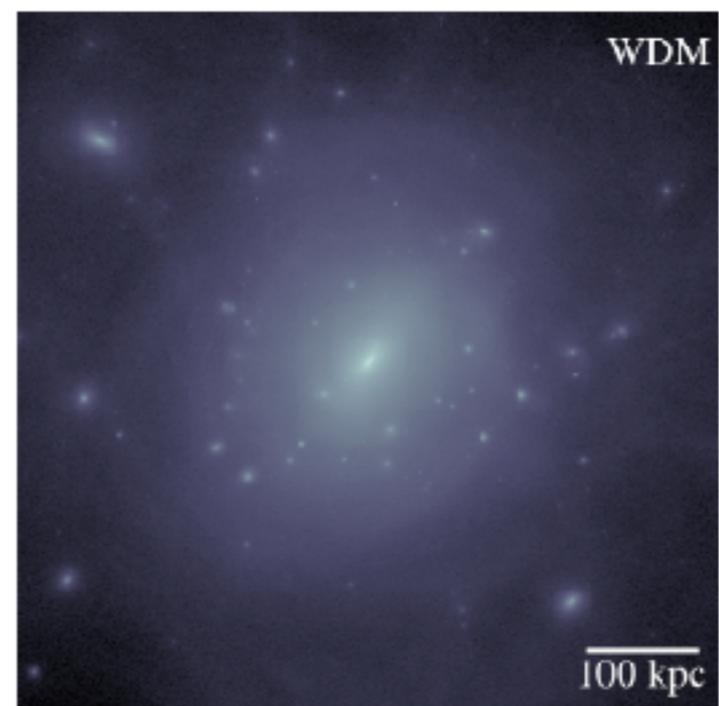
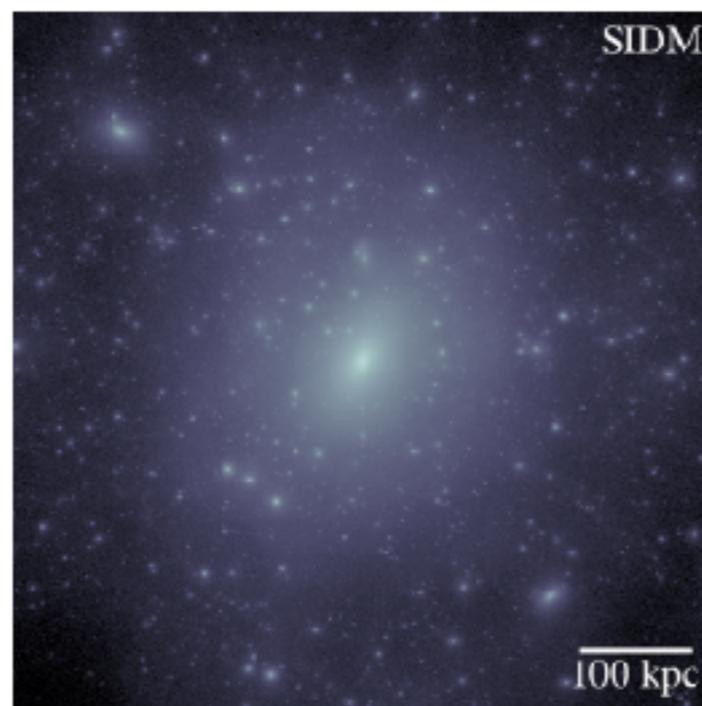
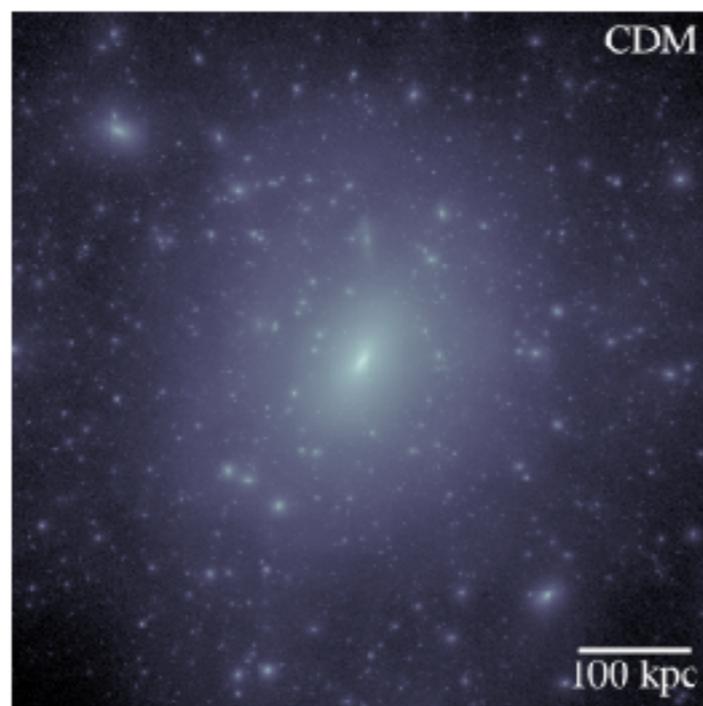
$$\delta_F = F / \langle F \rangle - 1$$



marginalize over  
6 cosmo param  
&  $T_0, \gamma$   
using COSMOMC  
against real obs data

# WDM conclusions

- **WDM** models w/  $\approx 3\text{keV}$  have been explored — strong alternative candidate to CDM
- $m_{\text{dm}} \gtrsim \text{a few keV}$  seems more likely than  $< 1\text{keV}$ .
- Viel+13, **Ly-a forest**:  $m > 3.3\text{ keV}$  ( $2\text{-}\sigma$ ),  $M_{\text{h,min}} \sim 2e8 M_{\odot}$
- Further study is needed with high-resolution and realistic SF & feedback models — **e.g. impact of AGN feedback on small-scale power** (van Daahlen+'11; Semboloni+'11)



- **WDM** reduces the substructure, but **keeps the cusp**.
- **SIDM** **doesn't reduce the abundance of substructure, but produces large const-density core**

# SIDM (self-interacting DM)

— as a generic consequence of hidden sector extensions to Standard Model

- no couplings to SM particles
- possibly strong self-interaction via dark gauge bosons

(Feng '10; Peter '12 for reviews)

$$\sigma/m \sim 0.1 - 100 \text{ cm}^2/\text{g} \quad \text{Spergel \& Steinhart '00}$$

$$\sigma/m \simeq 0.1 \text{ cm}^2/\text{g} \simeq 0.2 \text{ barn}/\text{GeV} \quad \text{Rocha+'13}$$

can produce results consistent w/ current obs.

**LSS & sub halos unchanged.**

# Fuzzy Dark Matter (FDM)

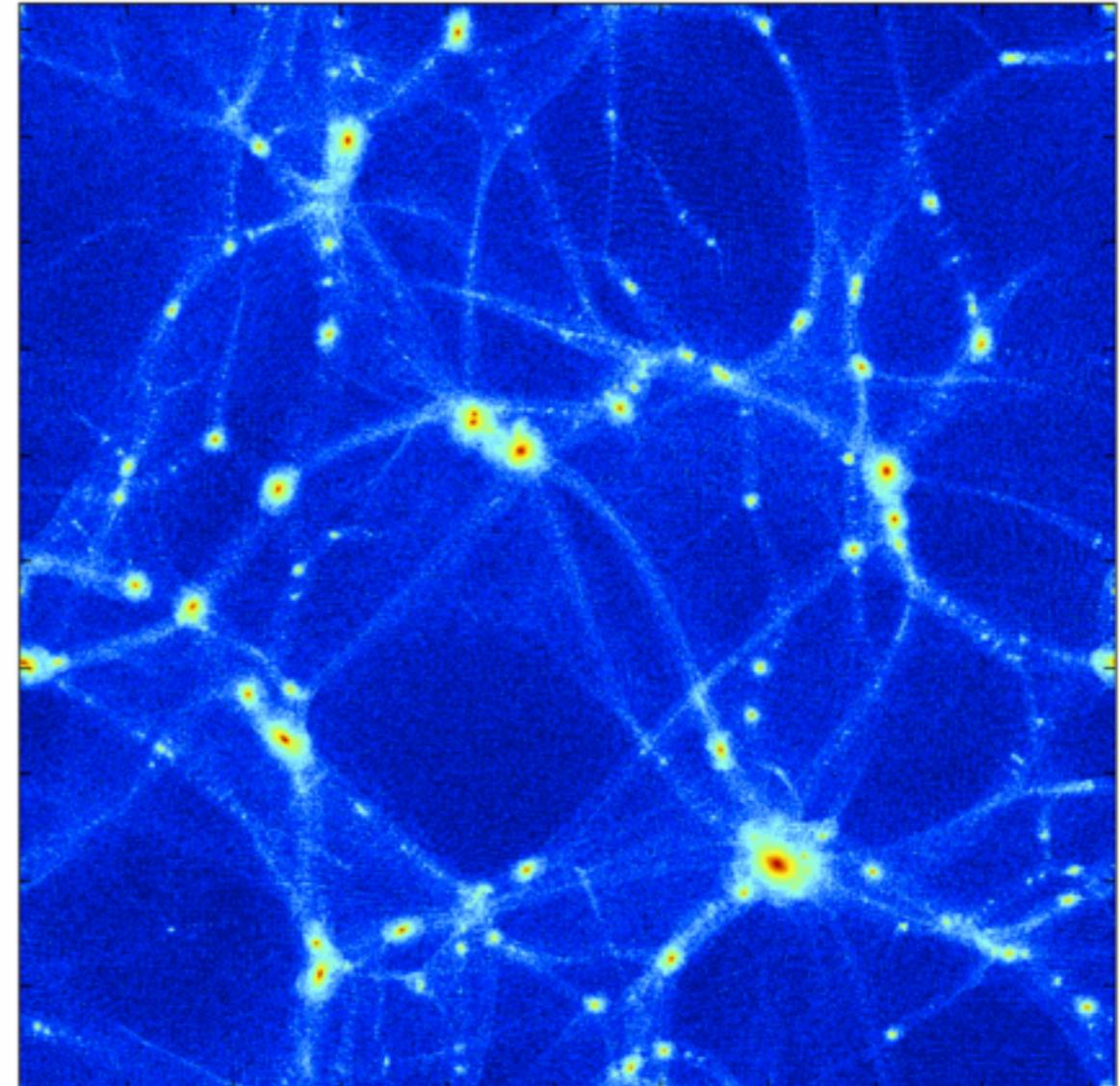
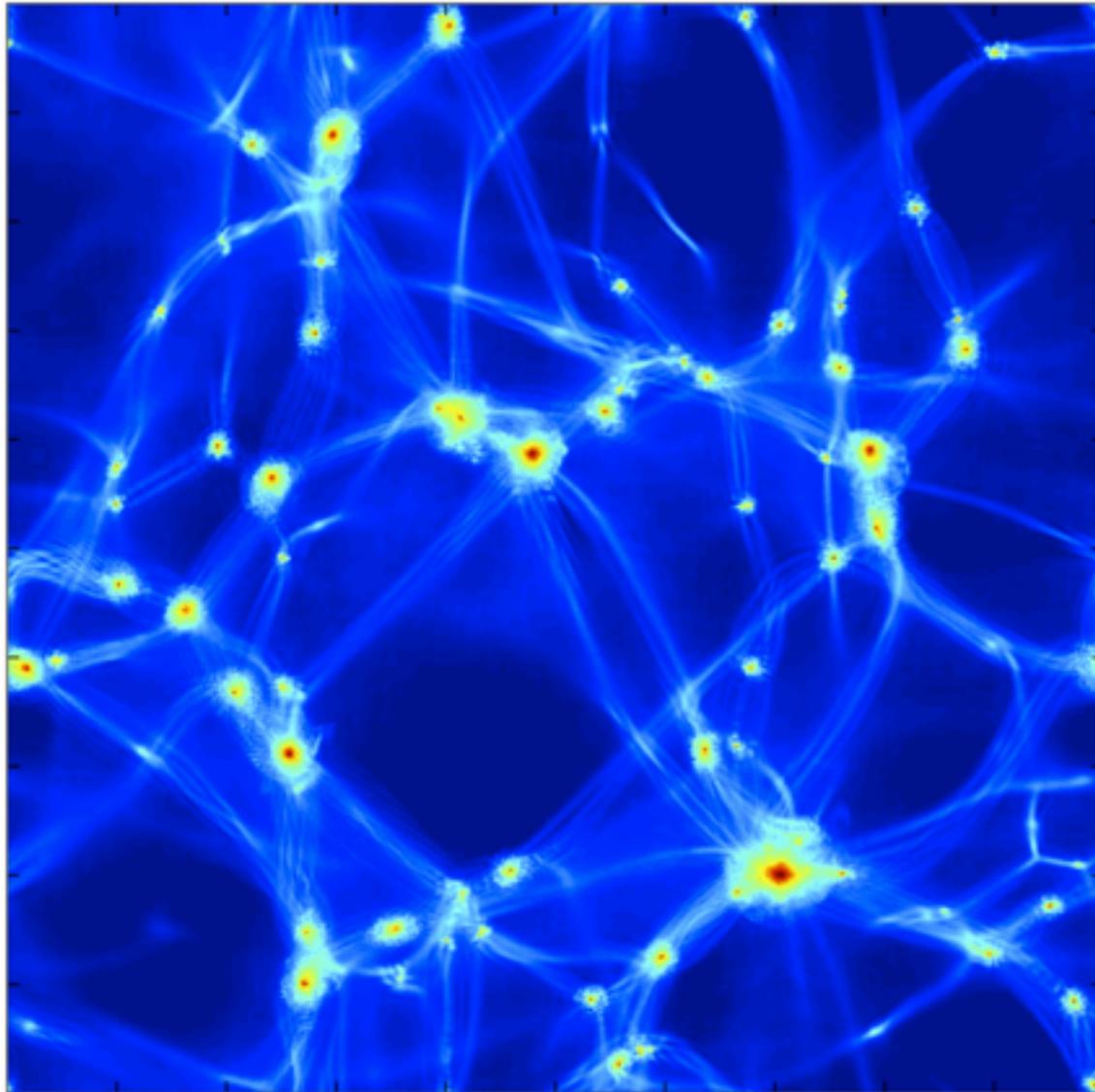
## Ultra Light Bosons, Wave-like, Axion-like

- non-thermal boson field (particularly scalar), non-rela, low-momentum state as a cold BEC
- $m \sim 10^{-22}$  eV,  $\lambda_{\text{de Broglie}} \sim 1 \text{ kpc}$ ,  $< 10^7 \left( \frac{m}{10^{-22} \text{ eV}} \right)^{-3/2} M_{\odot}$
- suppresses halo formation @  $< 10^{10} \left( \frac{m}{10^{-22} \text{ eV}} \right)^{-4/3} M_{\odot}$
- halo abundance reduced at
- forms a central core as a “**soliton**” (Schrödinger-Poisson eq.)
- on large-scales,  $\approx$  CDM

..., Baldeschi+83; Kim '87; Sin+94; Hu+00;  
Marsh+14; Schive+14; Hui+17; Mocz+17; ....

**FDM**

$\approx$  **CDM** (more like WDM)

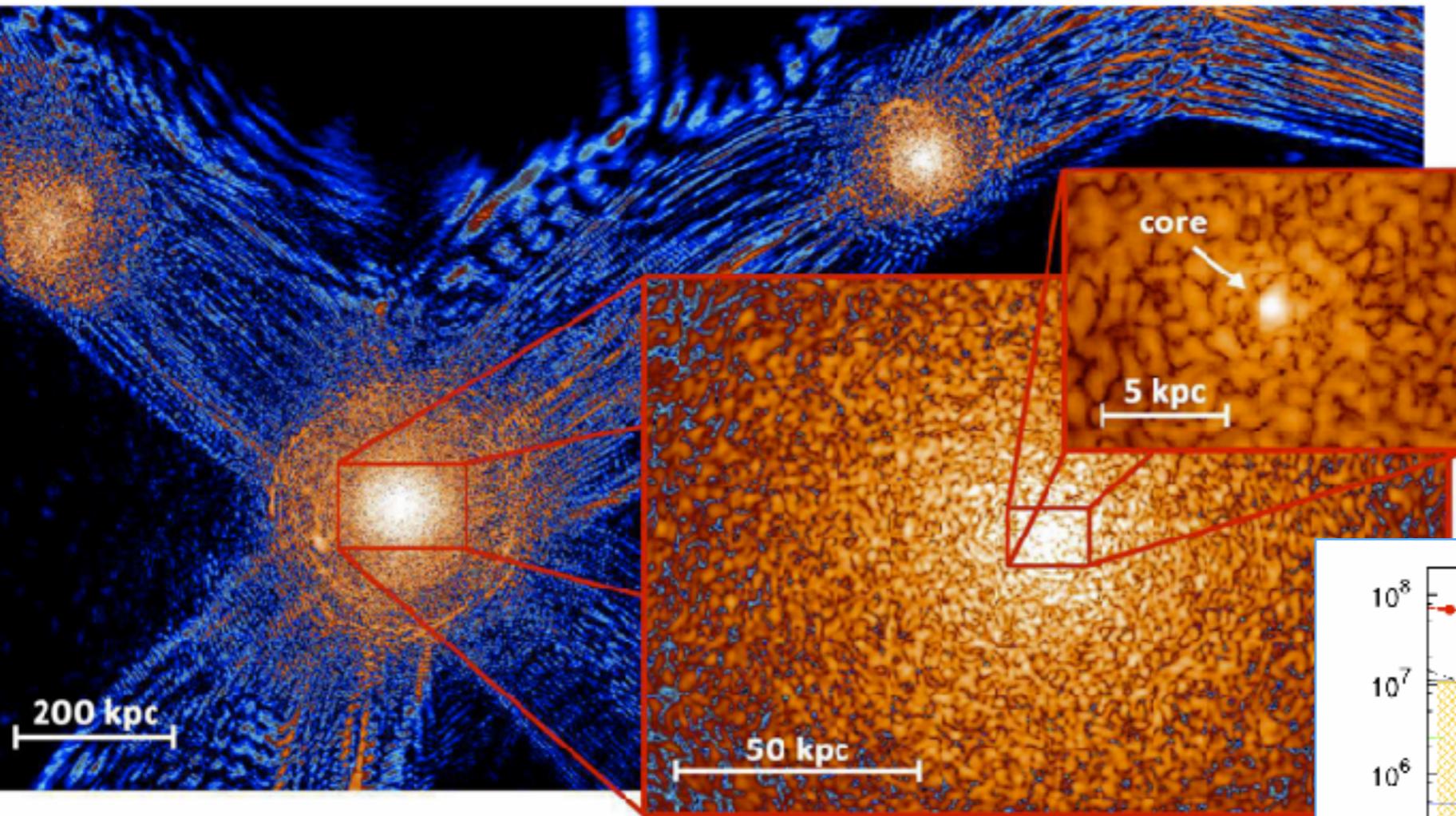


**Uncertainty principle counteracts gravity  
below Jeans scale**

Schive+14

- adds new form of quantum pressure from uncertainty
- comoving Jeans length:  $\lambda_J \propto (1+z)^{1/4} m_B^{-1/2}$

# Solitonic Core of FDM simulation



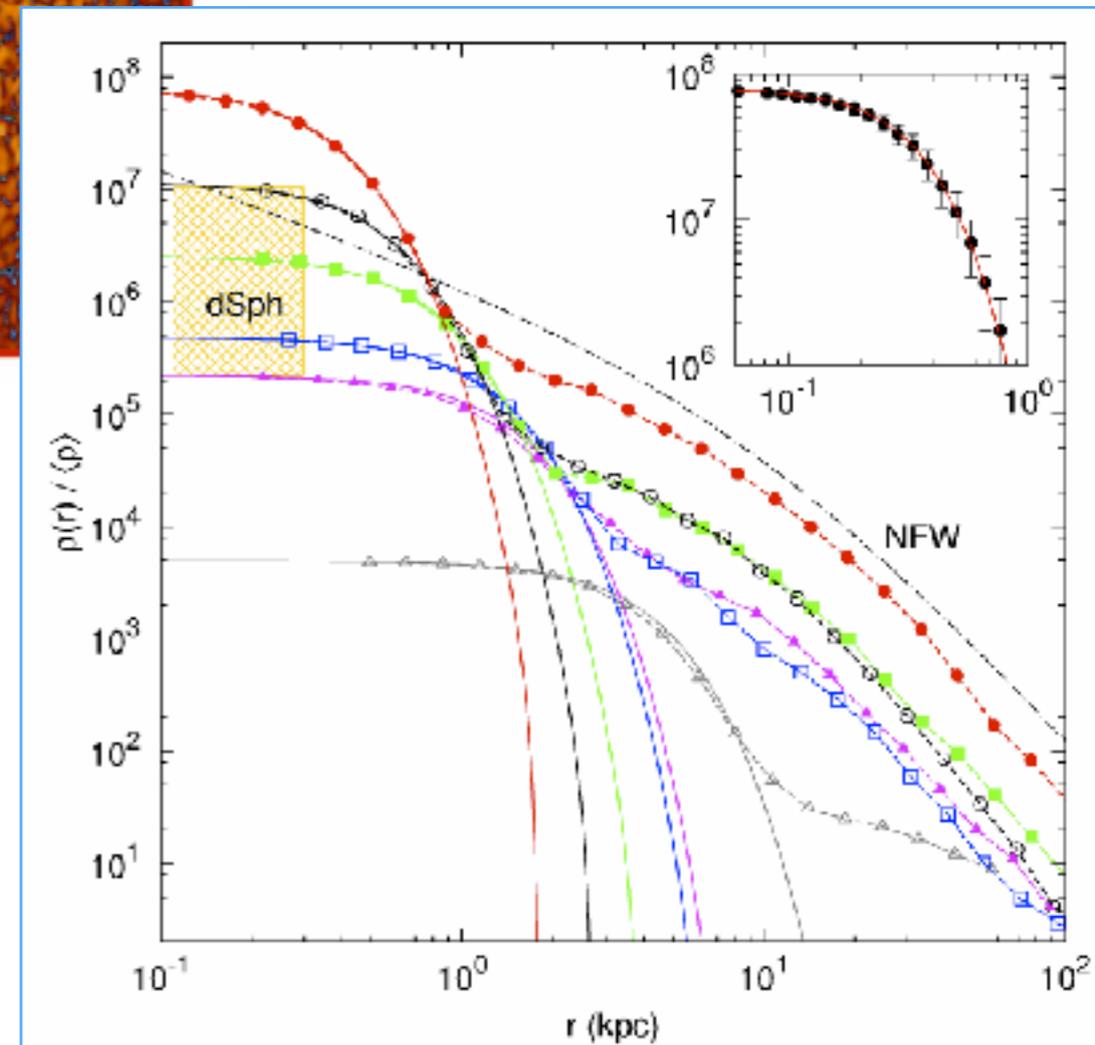
Schive+14

gravitationally bound  
solitonic core

e.g.  $m_B = (8.1^{+1.6}_{-1.7}) \times 10^{-23} \text{ eV}$   
for Fornax dSph gal.

$$M_s \propto M_{gal}^{1/3}$$

$M_s \simeq 2 \times 10^9 M_\odot$  for MW core



# The impact of ultra-light axion self-interactions on the large scale structure of the Universe

Desjacques+'17 arXiv:1709.07946

- constraints from Ly $\alpha$  P(k):  $m > 2 \times 10^{-21}$  eV

cf. Irsic+17; Armengaud+17; but Zhang+17

- **But, attractive force due to self-interaction btw ULA**

- semi-analytic linear stability analysis

- **cosmic web can be influenced.**

- **needs further numerical simulation studies**

reconsider Schive+14; Calabrese+16; Zhang+16; Mocz+17; ....

$$\Omega \sim 10^{-1} \left( \frac{f}{10^{17} \text{ GeV}} \right)^2 \left( \frac{m}{10^{-22} \text{ eV}} \right)^{1/2}$$

f: decay const (symmetry-breaking scale)

extremely tiny quartic coupling:  $\lambda = \frac{m^2}{f^2} \sim 10^{-96}$ ,

# Various Dark Matter

## & Astrophysics

**Cold Dark Matter (CDM):**

$$m \sim 100 \text{ GeV},$$
$$v_{\text{th}}^{z=0} \approx 0 \text{ km s}^{-1}$$

**Warm Dark Matter (WDM):**

$$m \sim 1 \text{ keV},$$
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**Hot Dark Matter (HDM):**

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***Thermal relic***

e.g. WIMP (weakly interacting massive ptcl)

becomes non-relativistic earlier, suppress perturbation at galactic or smaller scales.

(gravitino, steril neutrino,...)

remains relativistic until late time, and erase structures at super-galactic scales.

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