



高等研究院

名古屋大学

# Cosmological imprints of string axions in plateau

---

Yuko Urakawa (Nagoya university, IAR)

*I.Soda & Y.U.(1710.00305)*

*N. Kitajima, I.Soda, & Y.U.(in progress)*

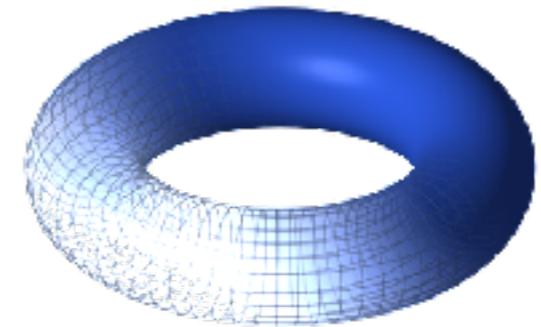
# String axiverse

---

10D string theory/supergravity

↓  
+ 6D compactification

Moduli fields ~ Geometrical DOFs



4D low energy EFT + String axions ....

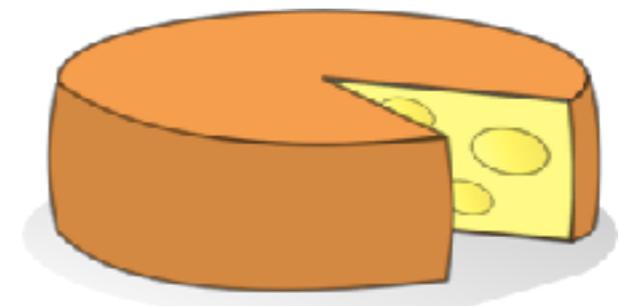
wide mass ranges → Probe of exDim

*Arvanitaki et al. (10)*

ex. Large Volume Scenario

*Conlon et al. (05)*

Predicts light mass axions

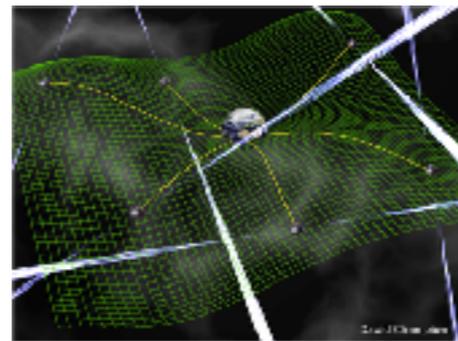
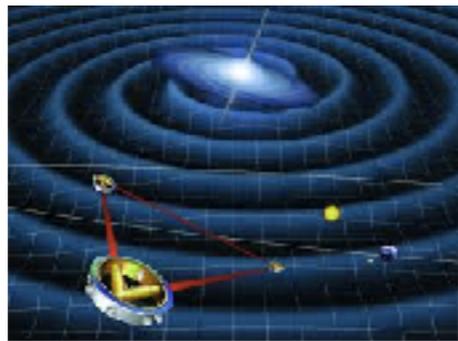


# Outline

---

## Targets

i) New window in string axiverse from GWs



ii) In particular, for Axion =DM, imprints on LSS

## Keywords

- Parametric resonance instability
- Turbulence

# String axions in plateau

---

Scalar potential  $V(a) = \Lambda^4 \left(1 - \cos \frac{a}{f}\right)$

under the dilute instanton gas approximation

In string theory constructions, potential tends to be flatten out.

ex. Monodromy, ....

having  $V'' < 0$

*Dubovski et al. (10), Nomura, Watari & Yamazaki (17)*

Axions w/flatten region

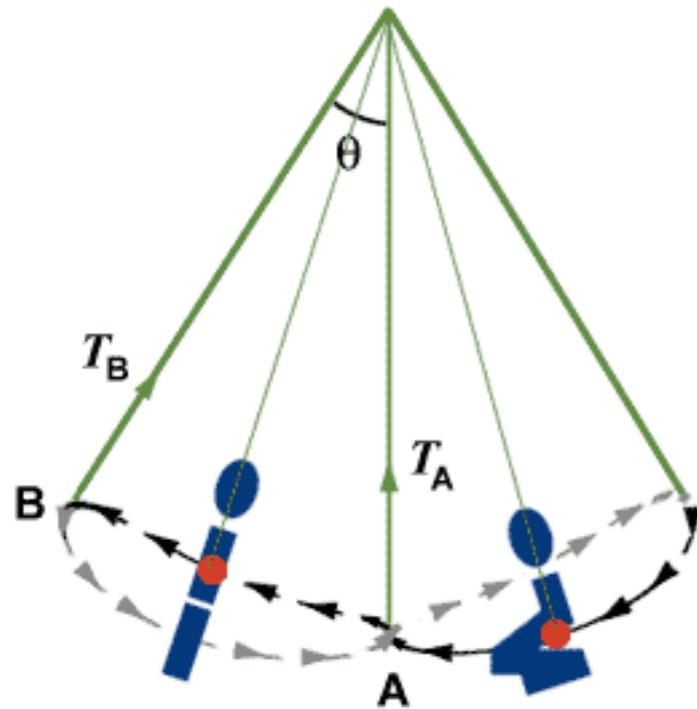
*Soda & Y.U. (17)*

→ Parametric resonance instability

New window in cosmological axion search

# Parametric resonance

---



Repeat: Up & Down in half period

→ Periodic ext. force (vs centrifugal force)

→ Enhancing the amplitude

“Parametric resonance instability”

## Mathieu equation

$$\frac{d^2}{dx^2} \tilde{\varphi} + (A - 2q \cos 2x) \tilde{\varphi} = 0$$

resonance band

$$A \sim n^2$$

ex. First band

$$\tilde{\varphi} \propto e^{\gamma x}$$

$$\gamma \simeq q/2$$

# Two enemies against PR

---

ex. Reheating after inflation  $H < m$ ,  $\varphi(t) \sim \varphi_* \cos mt$

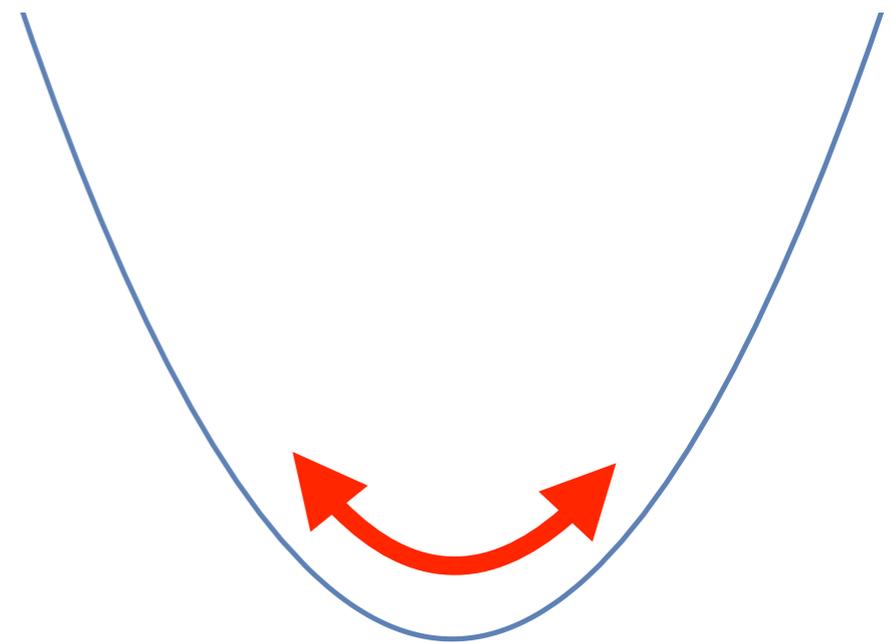
- Particle production through interaction w/SM sector
- Enhancement of inhomogeneity through self-interaction

## Cosmic expansion disturbs PR

i)  $\varphi_*$  damps due to Hubble friction

$$\text{Growth rate } \gamma \propto \varphi_*^n \quad (n > 0)$$

ii) Redshift away from resonance bands



# Two enemies against PR

---

ex. Reheating after inflation  $H < m$ ,  $\varphi(t) \sim \varphi_* \cos mt$

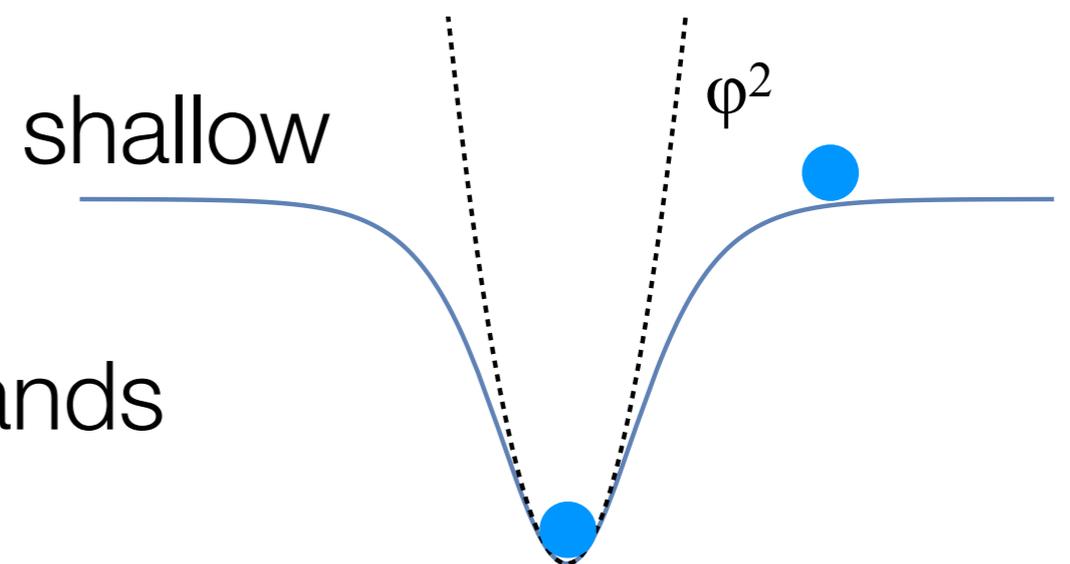
- Particle production through interaction w/SM sector
- Enhancement of inhomogeneity through self-interaction

## Cosmic expansion disturbs PR

i)  $\varphi_*$  damps due to Hubble friction

$$\text{Growth rate } \gamma \propto \varphi_*^n \quad (n > 0)$$

ii) Redshift away from resonance bands

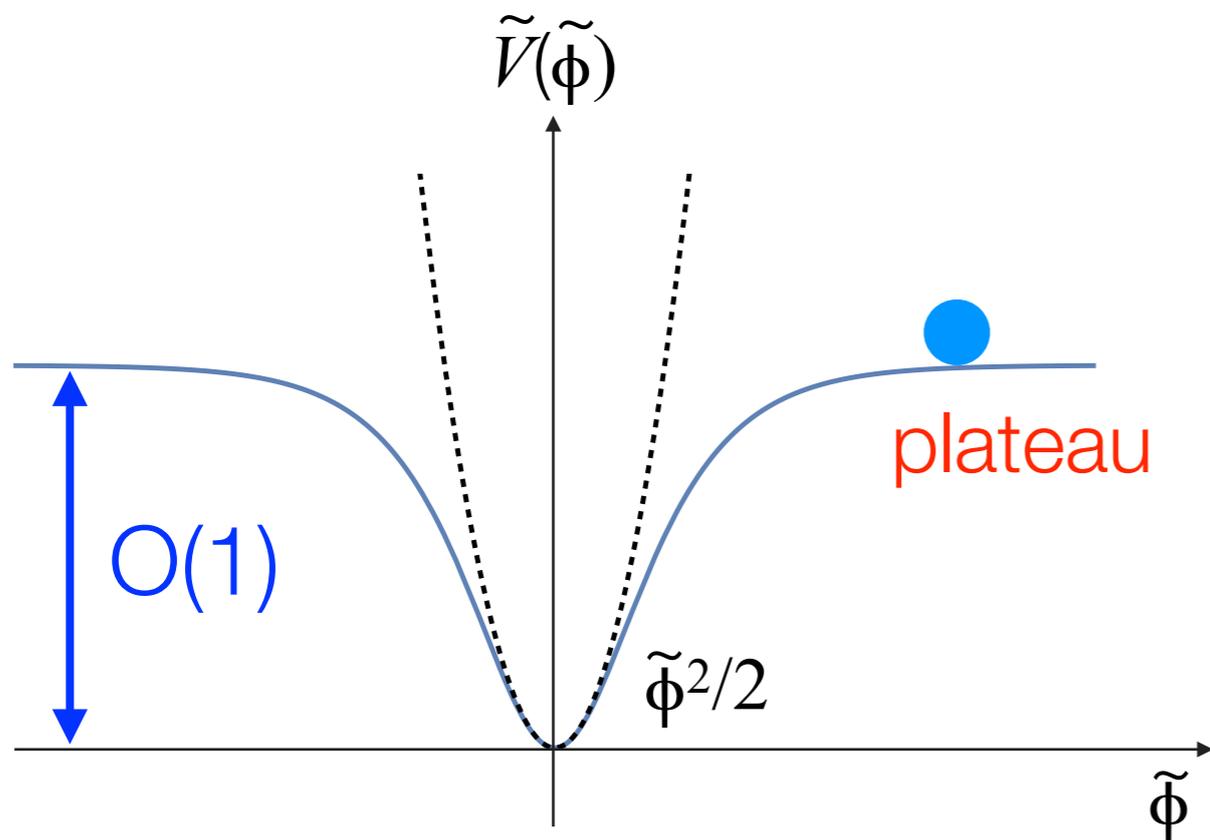


They can be overwhelmed if plateau exists!!

# Setup of problem

*Soda & Y.U.(17)*

Given that there is a string axion (w/mass  $m$ ) whose potential has a plateau region, ...



scalar potential

$$V(\phi) = (mf)^2 \tilde{V}(\tilde{\phi}) \quad \tilde{\phi} \equiv \phi/f$$

$$\text{i) } \tilde{V}(\tilde{\phi}) \rightarrow \tilde{\phi}^2/2 \quad \tilde{\phi} \rightarrow 0$$

$$\text{ii) } \tilde{V}(\tilde{\phi})/\tilde{\phi}^2 \rightarrow 0 \quad \tilde{\phi} \rightarrow \infty$$

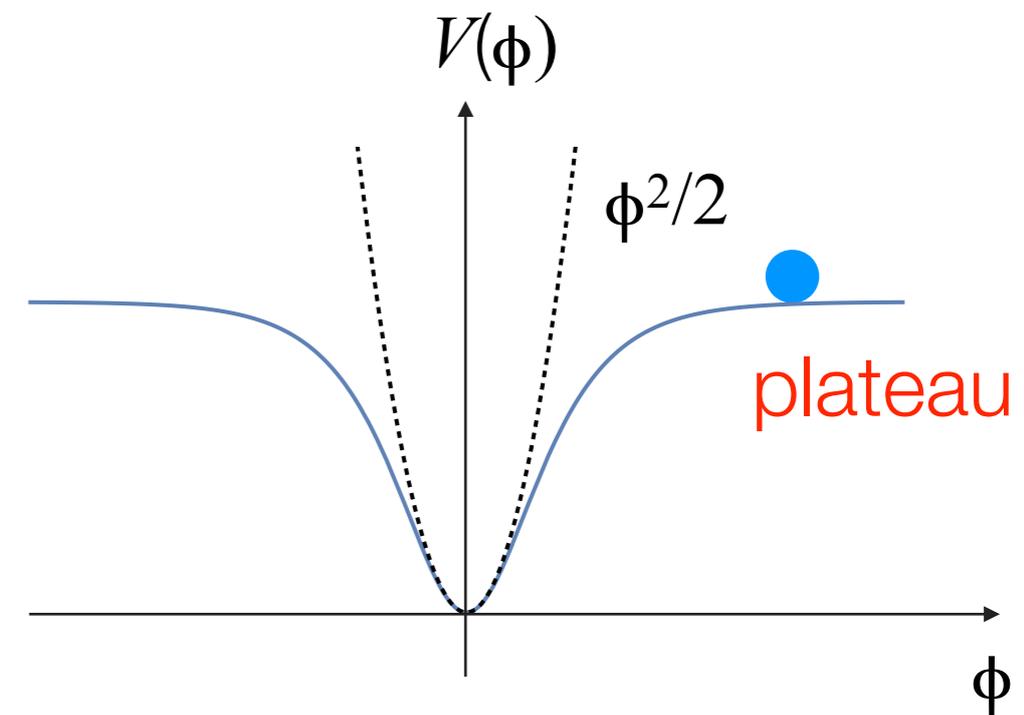
+  $Z_2$  symmetry

# Bottom-line story

1. Axion slowly rolls in plateau
2. Onset of oscillation  $H_{osc}/m < 1$
3. Exponential growth due to PR

if  $H_{osc}/m \ll 1$

No disturbance due to cosmic exp.



4. Rescattering  $\rightarrow$  PR becomes inefficient *eg. Kofman, Linde, Starobinsky*

5. Momentum transfer due to turbulence  $\rightarrow$  GW emission

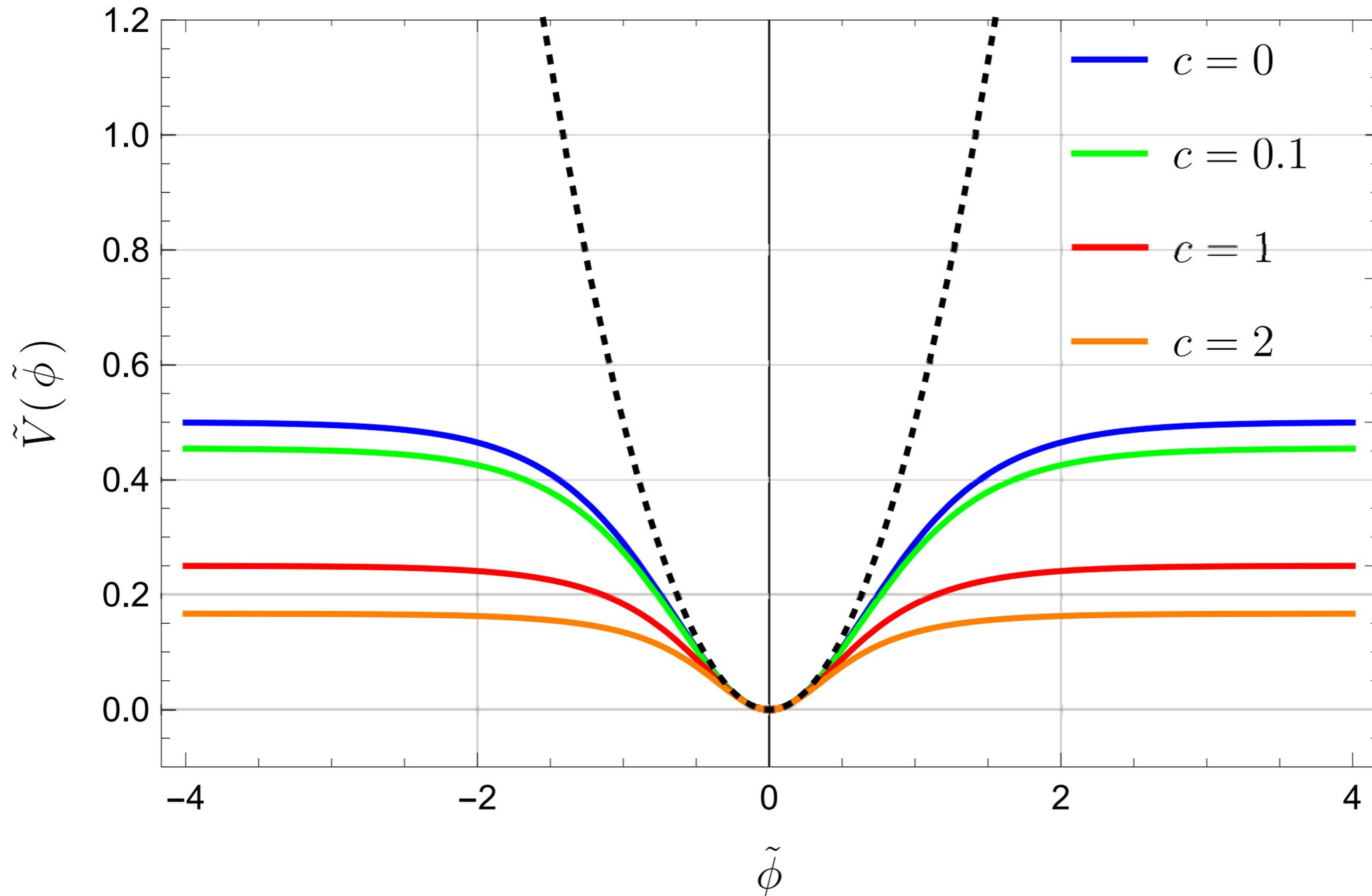
*Micha & Tkachev (02,04)*

6. Oscillon/I-ball formation

*Kasuya+(03), Amin + (10, 12, 17), Zhou(13), Antusch +(17), Kawasaki+(17), ...*

# Exercise: $\alpha$ -attractor

$$V(\phi) = \frac{(m_a f)^2}{2} \frac{(\tanh \frac{\phi}{f})^2}{1 + c(\tanh \frac{\phi}{f})^2}$$



Solving KG eq.

in cosmological spacetimes

---

Klein-Gordon eq.

$$\square\phi - V_\phi = 0$$

eg. Homogeneous mode

$$\frac{d^2\tilde{\phi}}{dx^2} + \frac{3p}{x} \frac{d\tilde{\phi}}{dx} + p^2 \frac{d\tilde{V}}{d\tilde{\phi}} = 0$$

Dimensionless form

$$\tilde{\phi} = \phi/f \quad x = m/H = mt/p \quad a \propto tp$$

$$(IC) \tilde{\phi}(x_i), d\tilde{\phi}/dx(x_i) \longrightarrow x_{osc} = O(1) - O(10^4)$$

$$- m \rightarrow H_{osc} = m/x_{osc}$$

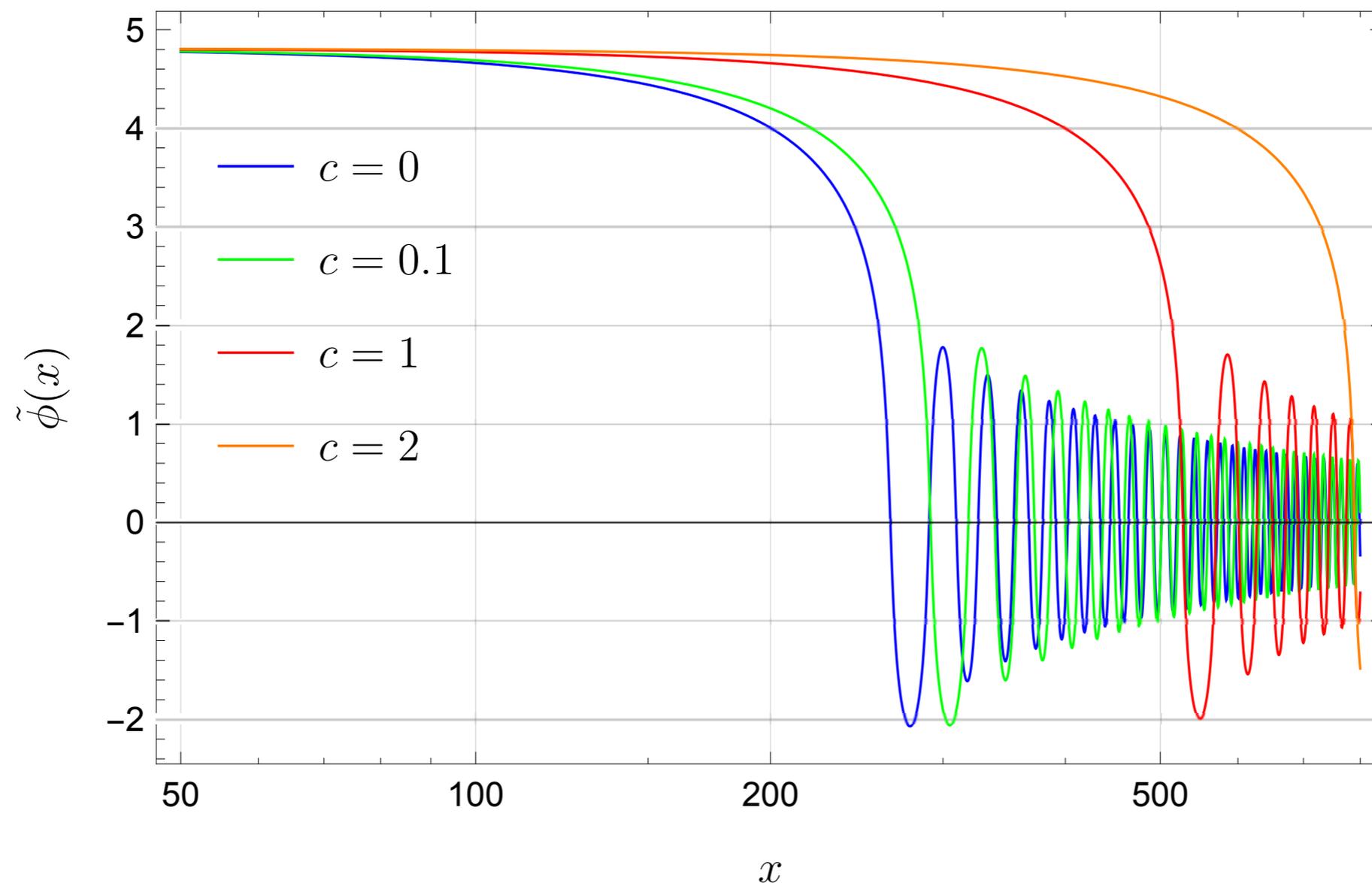
$$- f \rightarrow \text{Abundance}$$

# Background evolution

$\tilde{\phi}_i=5$

RD

*Soda & Y.U.(17)*



$x = m/H$

Onset of oscillation is not  $m \sim H$ , but delayed!

# Linear perturbation

in Newtonian gauge

---

$$\ddot{\varphi} + 3H\dot{\varphi} + \frac{k^2}{a^2}\varphi + V_{\phi\phi}\varphi - 2V_{\phi}\Phi + \dot{\phi}\dot{\Phi} = 0$$

$\Phi$ : Bardeen potential

## 2 possible instabilities

i) Parametric resonance instability

Non-linear potential

$$V_{\phi\phi} \supset \phi^n \sim (\phi^* \cos mt)^n$$

$$\longrightarrow \cos(nmt)$$

ii) Tachyonic instability

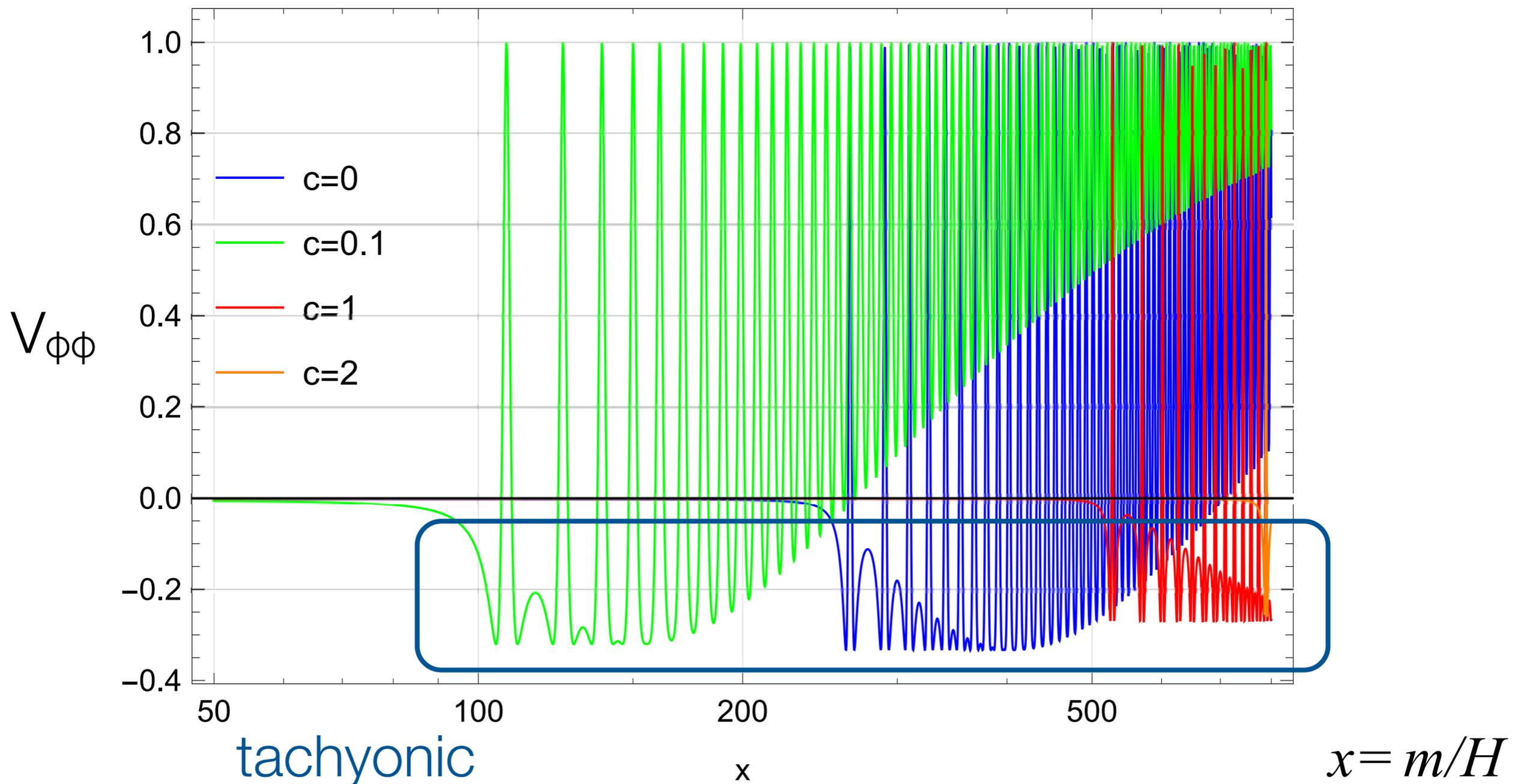
Region w/  $V_{\phi\phi} < 0$

\* Backreaction of ULA on  $\Phi$  was neglected.

# Tachyonic instability?

Time evolution of mass term

$\tilde{\varphi}_i=5$  RD ( $p=1/2$ )

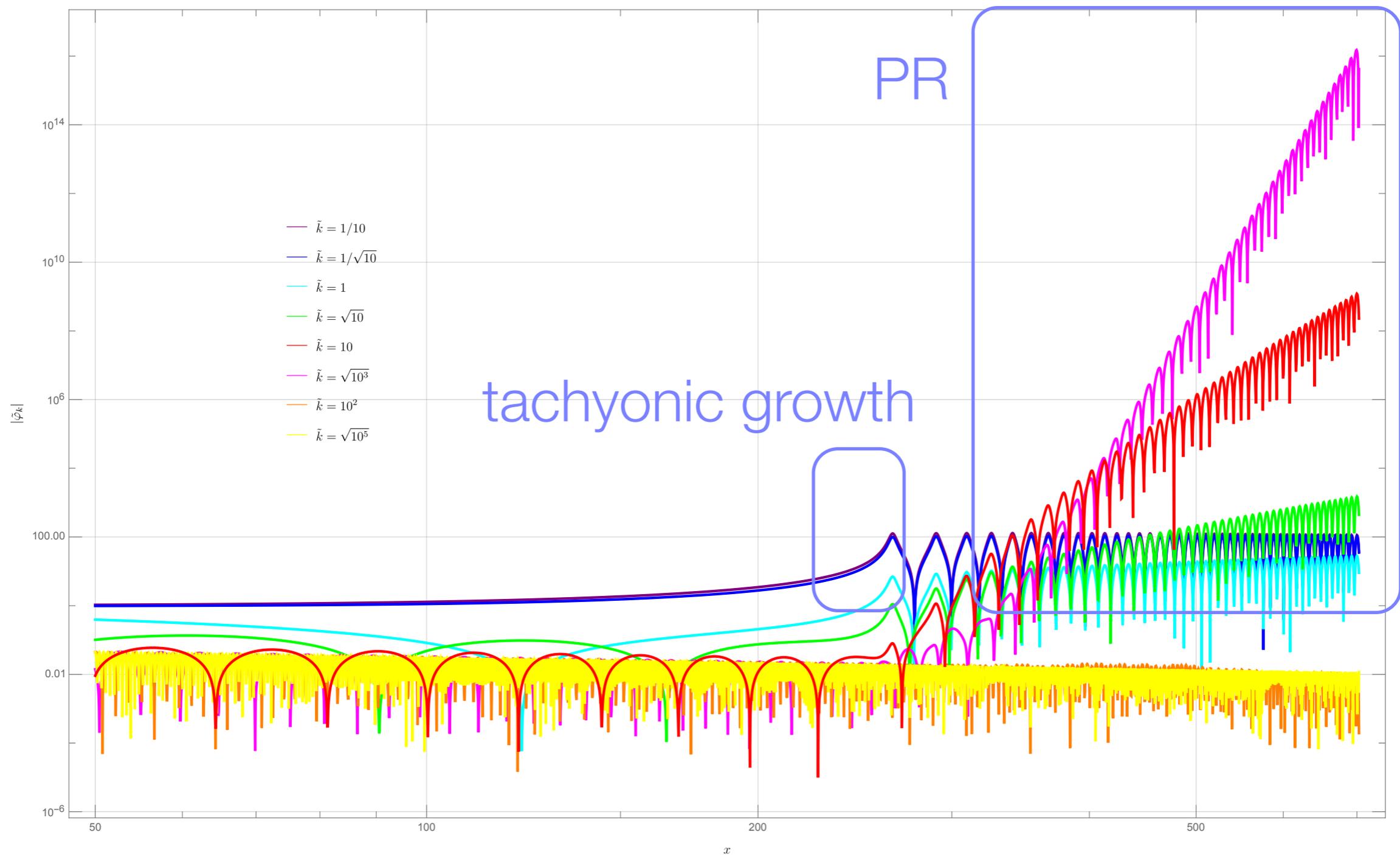


# Linear perturbation

Soda & Y.U.(17)

## Onset of oscillation in RD

$$\tilde{k} = k/(a_i m)$$



# Parametric resonance instability

---

Neglect cosmic exp. and  $\Phi$

$$\frac{d^2}{dx^2} \tilde{\varphi} + (A - 2a \cos 2x) \tilde{\varphi} = 0$$

BG axion  $\tilde{\phi} = \tilde{\phi}_* e^{if}$

Band width  $(q/A)^n$

$$A \equiv \frac{1}{4} \left[ \left( \frac{k}{m a_{osc}} \right)^2 + 1 - (2 + 3c) \tilde{\phi}_*^2 \right] \quad q \equiv \frac{2 + 3c}{8} \tilde{\phi}_*^2$$

## Mathieu equation

Resonance band

$$A \simeq n^2$$

First resonance band

$$\tilde{\varphi} \propto e^{\gamma x}$$

$$\gamma \simeq \frac{q}{2} = \frac{2 + 3c}{16} \tilde{\phi}_*^2$$

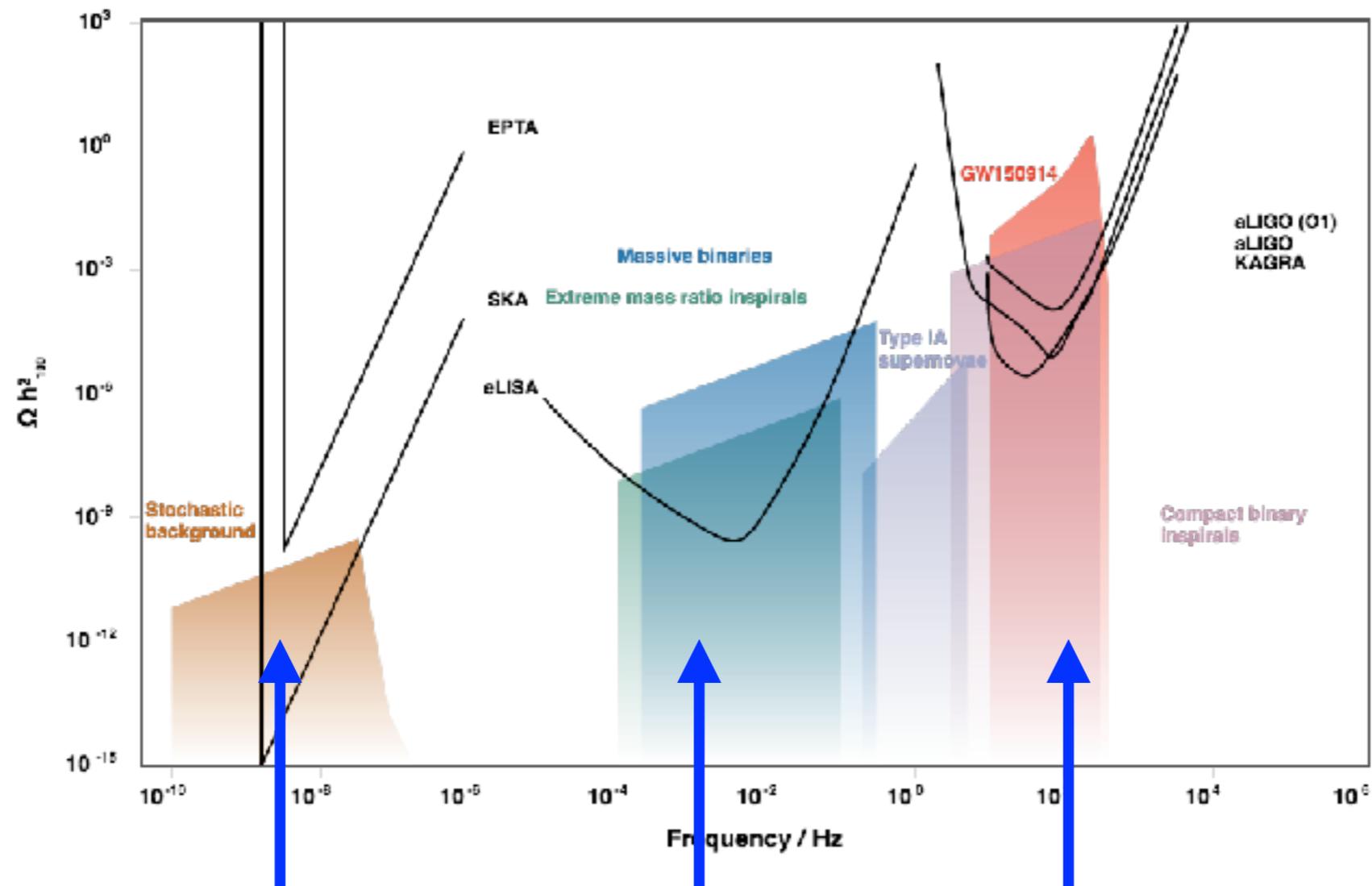
# GWs from PR of axion

## Frequency at present

$$f_0 \simeq m / (1 + z_*)$$

$z_*$ : Redshift at emission

$$z_{\text{osc}} \sim z_*$$



$$m \sim 10^{-16} \text{eV}$$

$$m \sim 10^{-6} \text{eV}$$

$$m \sim 10^3 \text{eV}$$

# Bottom-line story of Axion's excursion

1. Axion slowly rolls in plateau

2. Onset of oscillation  $H_{osc}/m < 1$

3. Exponential growth due to PR

if  $H_{osc}/m \ll 1$

*J.S&Y.U(07)*

.....

4. Rescattering  $\rightarrow$  PR becomes inefficient

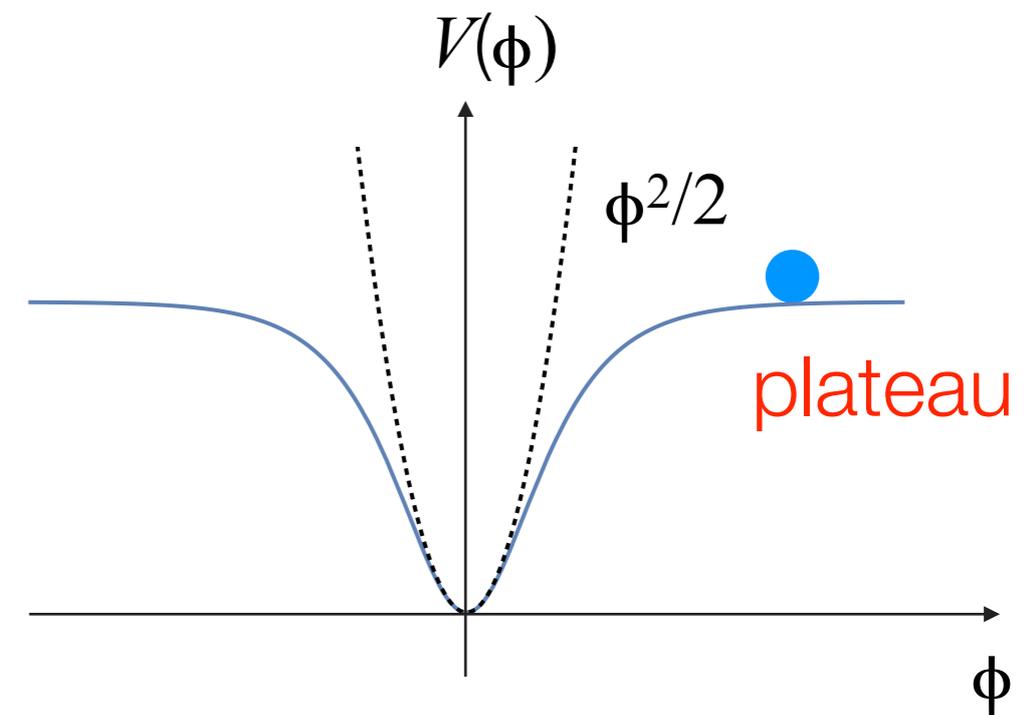
$+N.K$

5. Momentum transfer due to turbulence  $\rightarrow$  GW emission

*Micha & Tkachev (02,04)*

6. Oscillon/I-ball formation

*Kasuya+(03), Amin + (10, 12, 17), Zhou(13), Antusch +(17), Kawasaki+(17), ...*

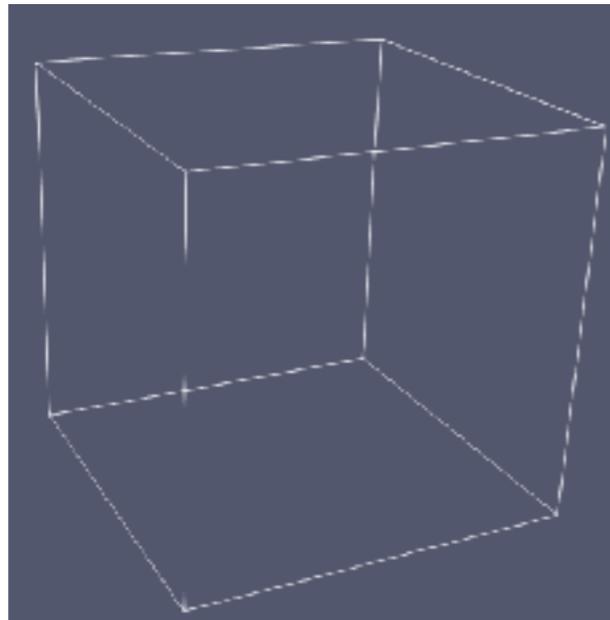


*eg. Kofman, Linde, Starobinsky*

# Oscillon formation

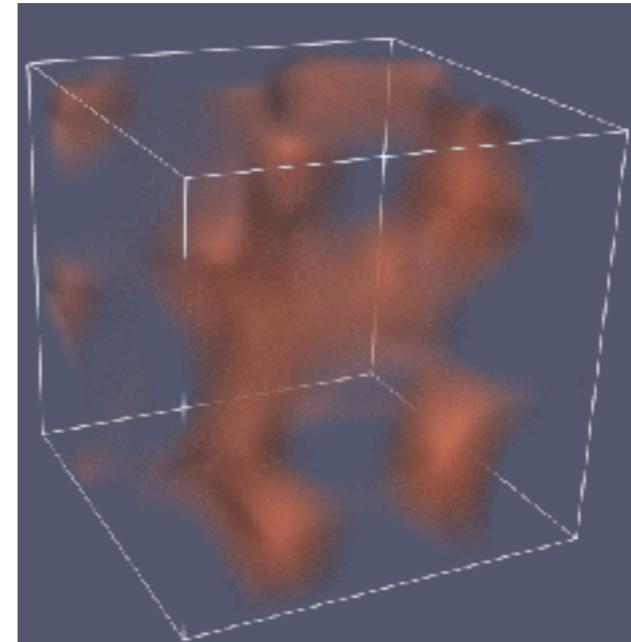
*Kitajima, Soda, Y.U. (in preparation)*

$a \sim a_0$



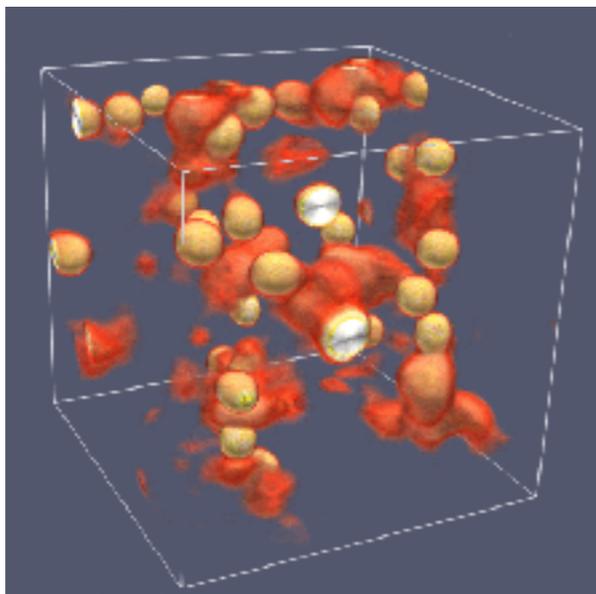
$a \sim 20 a_0$

rescattering



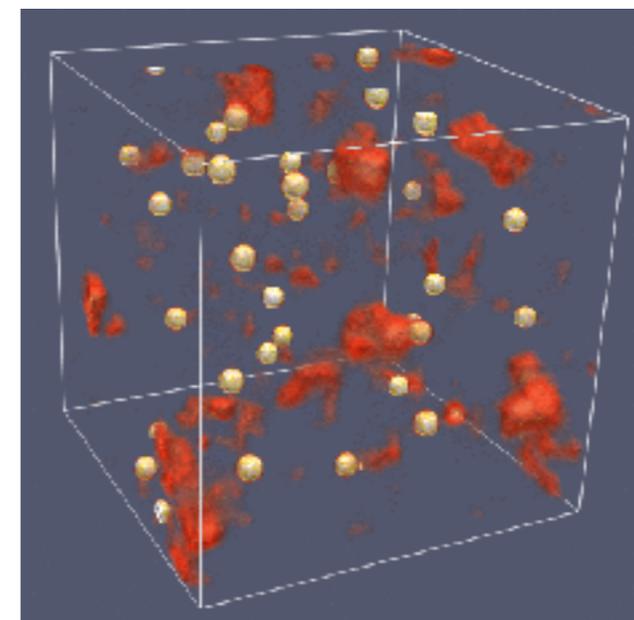
$a \sim 35 a_0$

turbulence



$a \sim 90 a_0$

oscillon



$N_{\text{grid}}=(128)^3$

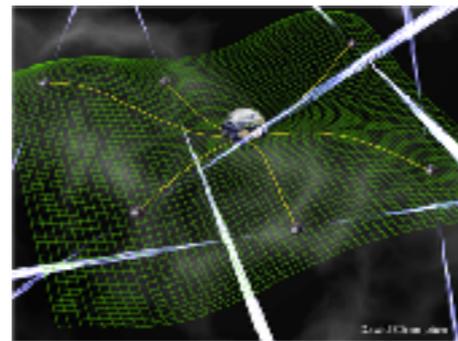
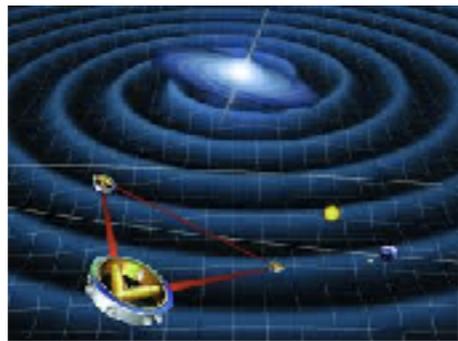
$f \sim 10^{-4} M_{\text{P}}, c=5, \phi_i=5 \rightarrow \Omega_{\text{GW}} \sim 10^{-15}$  in PTA band

# Outline

---

## Targets

i) New window in string axiverse from GWs



ii) In particular, for Axion =DM, imprints on LSS

## Keywords

- Parametric resonance instability
- Turbulence

# Bottom-line story of Axion's excursion

---

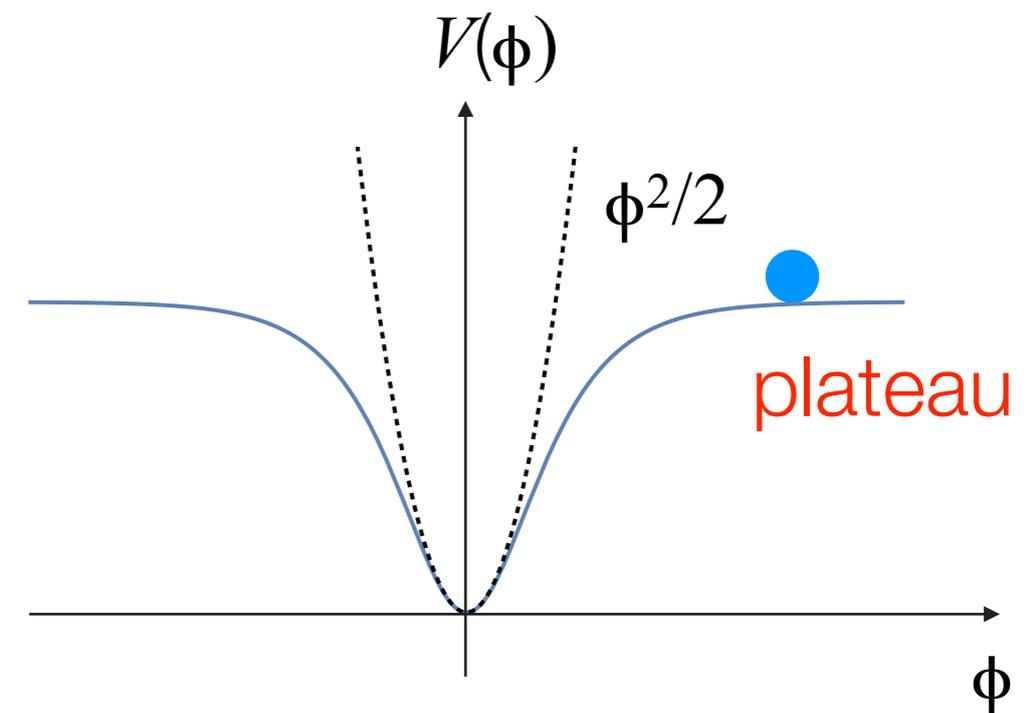
1. Axion slowly rolls in plateau
2. Onset of oscillation  $H_{osc}/m < 1$
3. Exponential growth due to PR

if not  $H_{osc}/m \ll 1$

4. PR finished due to red-shift

Yet, for DM= axion, imprints on structure formation

Resonance peak in spectrum



# Imprints for axion DM

---

## Alternative solution to small scale issues of $\Lambda$ CDM??

ULA w/  $m \sim 10^{-22} eV$

Recall Nagamine-san's

→ Emergent pressure smooths at  $k > k_J$

$k_J$ : Jeans scale

→ Tension with small scale observations?

*Irsic et al. (17), Kim et al. (17), ...*

Note!! Resonance scale  $k_r > k_J \propto a^{1/4}$

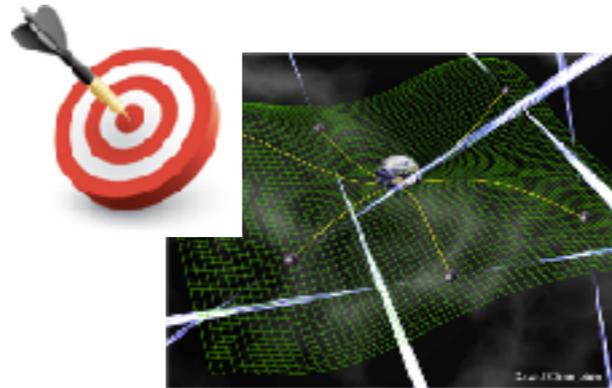
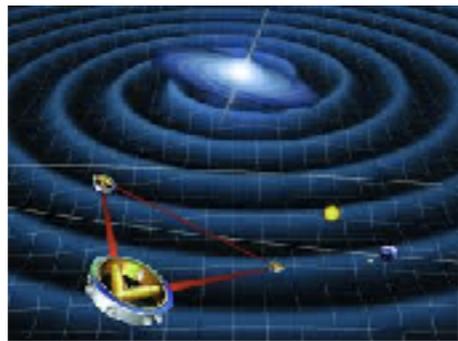
Evade tension? (in progress)

# Summary

---

## Targets: Axions in plateau

i) New window in string axiverse



ii) For Axion DM, enhancement of power spectrum at the scale determined by  $\sim$  the mass scale.

Remedy for tension of ULA w/small scale observations?

in progress

# Ultralight axion (ULA)

---

What is often said.....

$m > H_{eq} \sim 10^{-27}$  eV, ULA is quiet in cosmological scales.

 Not ULA in plateau!

## Jeans scale

ULA has pressure  $\rightarrow$  Jeans scale  $k_J(a) \simeq \sqrt{mH} a$

$k > k_J$       fluctuations are smoothed out

$\longrightarrow$  Tension with Lyman  $\alpha$  forest observation

at equal time  $k_r \simeq \sqrt{x_{osc}} k_J(a_{eq})$       Relaxing the tension?