



高等研究院

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Cosmological imprints of string axions in plateau

Yuko Urakawa (Nagoya university, IAR)

I.Soda & Y.U.(1710.00305)

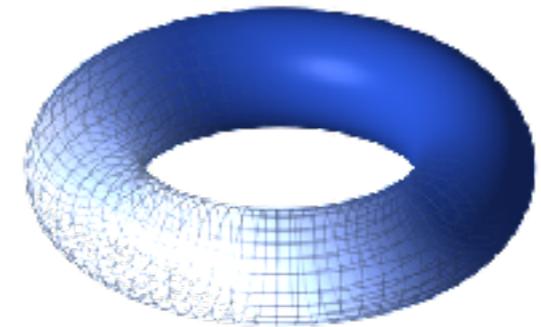
N. Kitajima, I.Soda, & Y.U.(in progress)

String axiverse

10D string theory/supergravity

+ 6D compactification

Moduli fields ~ Geometrical DOFs



4D low energy EFT + String axions

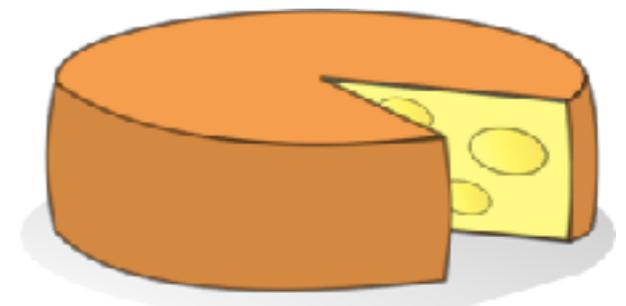
wide mass ranges → Probe of exDim

Arvanitaki et al. (10)

ex. Large Volume Scenario

Conlon et al. (05)

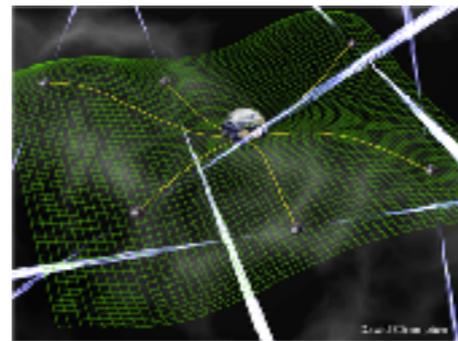
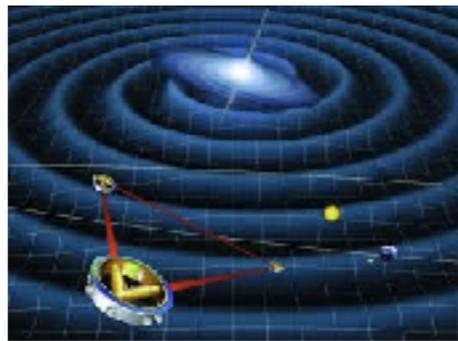
Predicts light mass axions



Outline

Targets

i) New window in string axiverse from GWs



ii) In particular, for Axion =DM, imprints on LSS

Keywords

- Parametric resonance instability
- Turbulence

String axions in plateau

Scalar potential $V(a) = \Lambda^4 \left(1 - \cos \frac{a}{f}\right)$

under the dilute instanton gas approximation

In string theory constructions, potential tends to be flatten out.

ex. Monodromy,

having $V'' < 0$

Dubovski et al. (10), Nomura, Watari & Yamazaki (17)

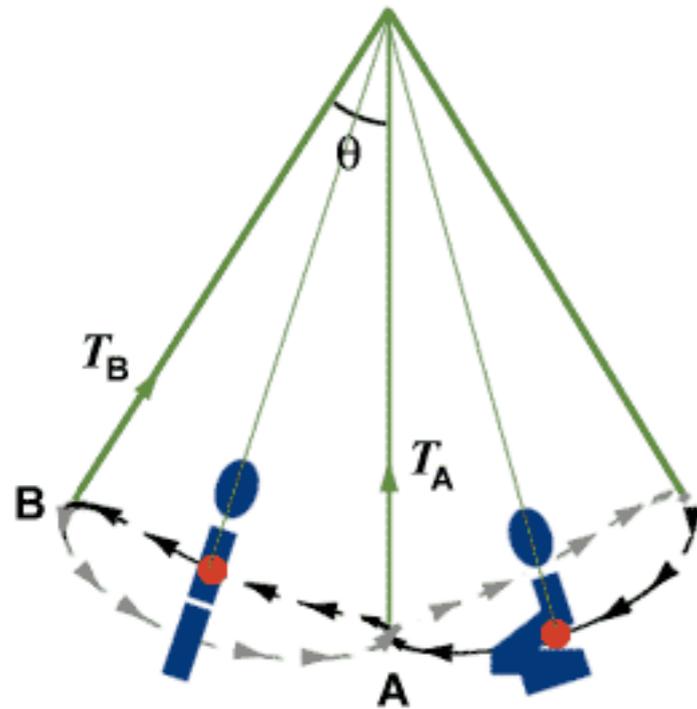
Axions w/flatten region

Soda & Y.U. (17)

→ Parametric resonance instability

New window in cosmological axion search

Parametric resonance



Repeat: Up & Down in half period

→ Periodic ext. force (vs centrifugal force)

→ Enhancing the amplitude

“Parametric resonance instability”

Mathieu equation

$$\frac{d^2}{dx^2} \tilde{\varphi} + (A - 2q \cos 2x) \tilde{\varphi} = 0$$

resonance band

$$A \sim n^2$$

ex. First band

$$\tilde{\varphi} \propto e^{\gamma x}$$

$$\gamma \simeq q/2$$

Two enemies against PR

ex. Reheating after inflation $H < m$, $\varphi(t) \sim \varphi_* \cos mt$

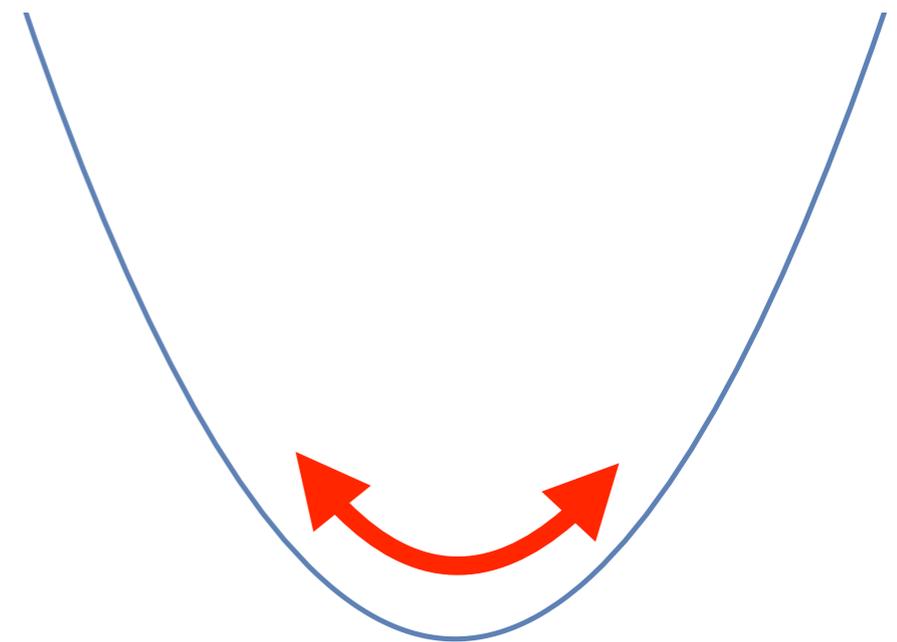
- Particle production through interaction w/SM sector
- Enhancement of inhomogeneity through self-interaction

Cosmic expansion disturbs PR

i) φ_* damps due to Hubble friction

$$\text{Growth rate } \gamma \propto \varphi_*^n \quad (n > 0)$$

ii) Redshift away from resonance bands



Two enemies against PR

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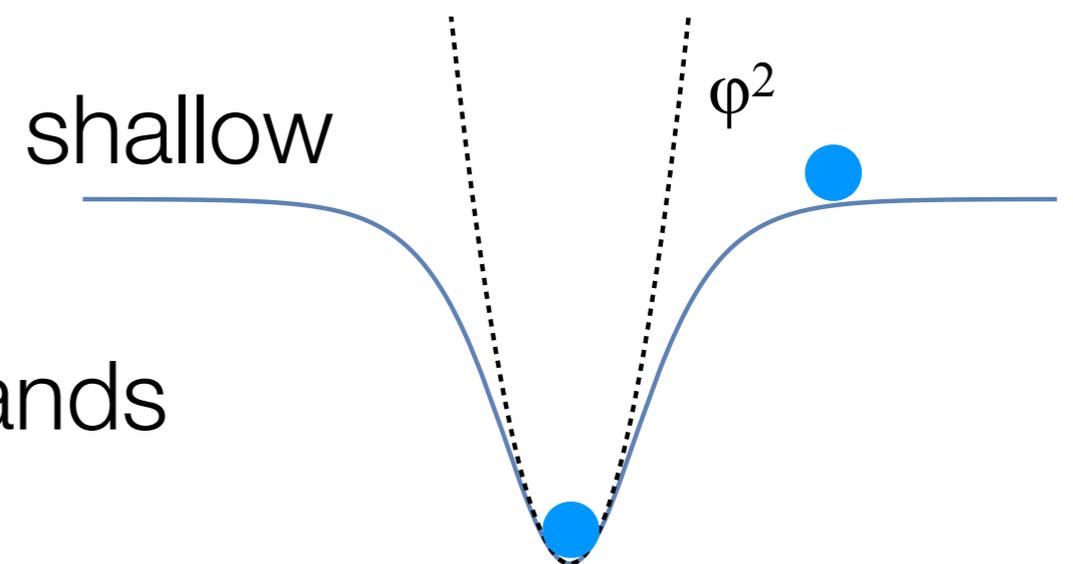
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Cosmic expansion disturbs PR

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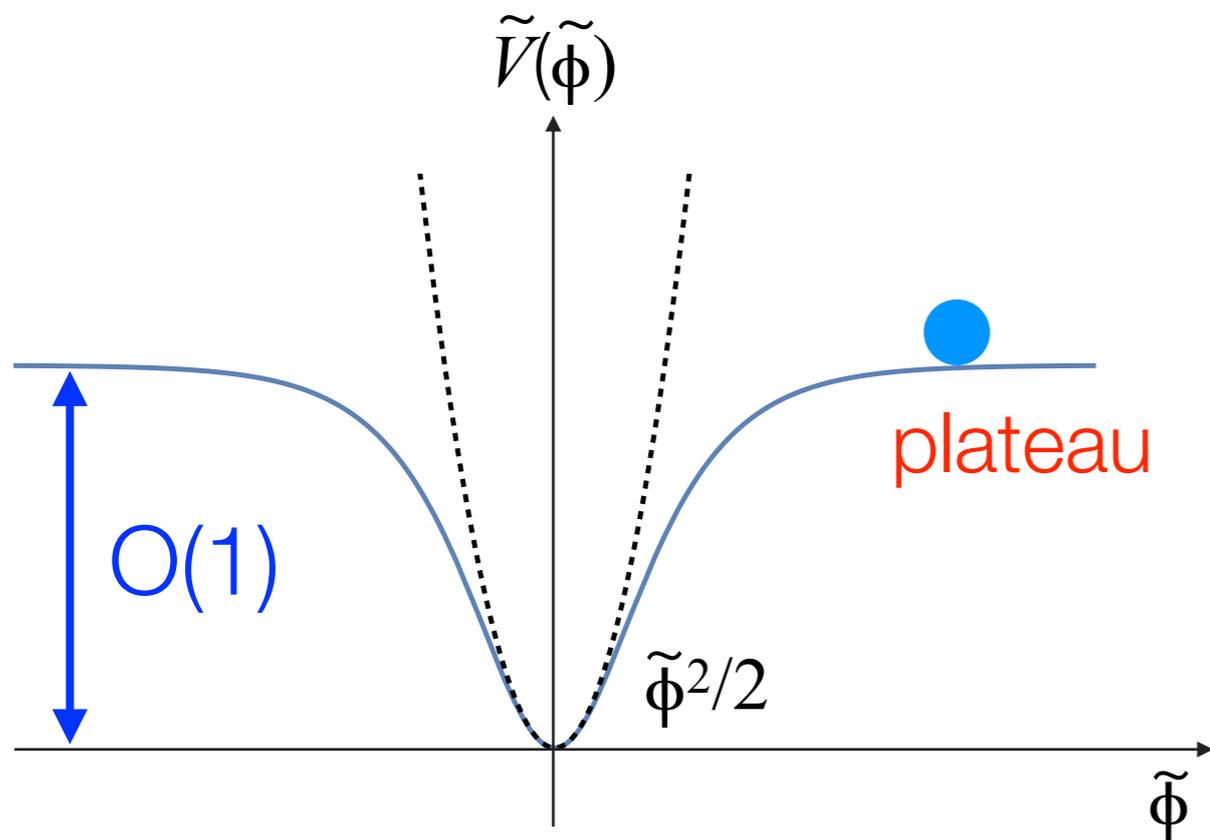


They can be overwhelmed if plateau exists!!

Setup of problem

Soda & Y.U.(17)

Given that there is a string axion (w/mass m) whose potential has a plateau region, ...



scalar potential

$$V(\phi) = (mf)^2 \tilde{V}(\tilde{\phi}) \quad \tilde{\phi} \equiv \phi/f$$

$$\text{i) } \tilde{V}(\tilde{\phi}) \rightarrow \tilde{\phi}^2/2 \quad \tilde{\phi} \rightarrow 0$$

$$\text{ii) } \tilde{V}(\tilde{\phi})/\tilde{\phi}^2 \rightarrow 0 \quad \tilde{\phi} \rightarrow \infty$$

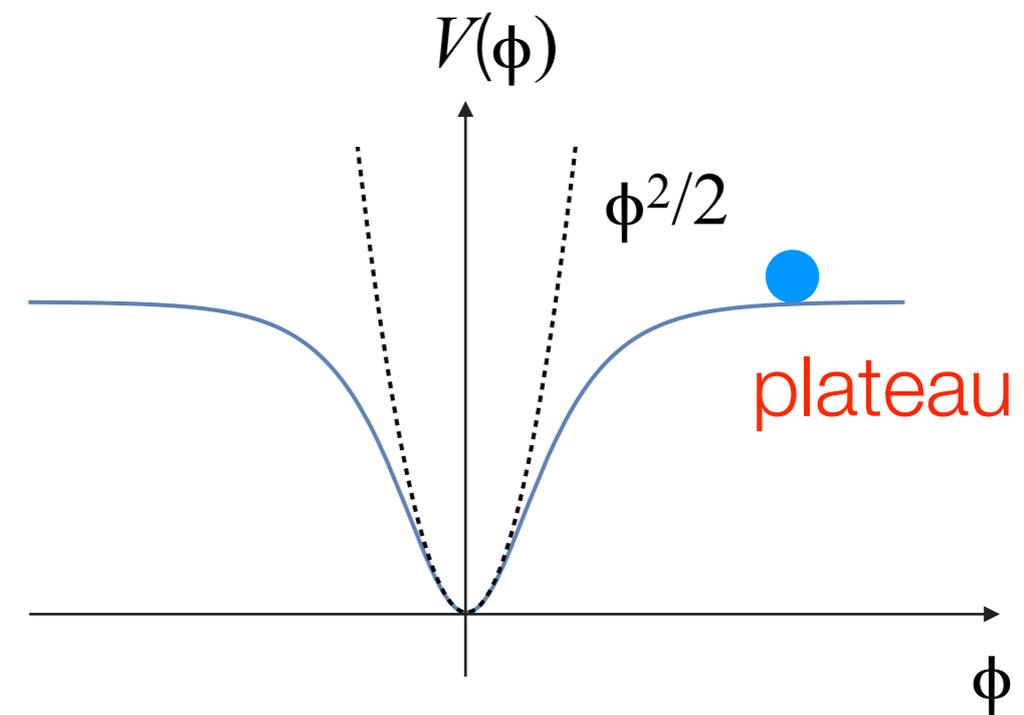
+ Z_2 symmetry

Bottom-line story

1. Axion slowly rolls in plateau
2. Onset of oscillation $H_{osc}/m < 1$
3. Exponential growth due to PR

if $H_{osc}/m \ll 1$

No disturbance due to cosmic exp.



4. Rescattering \rightarrow PR becomes inefficient *eg. Kofman, Linde, Starobinsky*

5. Momentum transfer due to turbulence \rightarrow GW emission

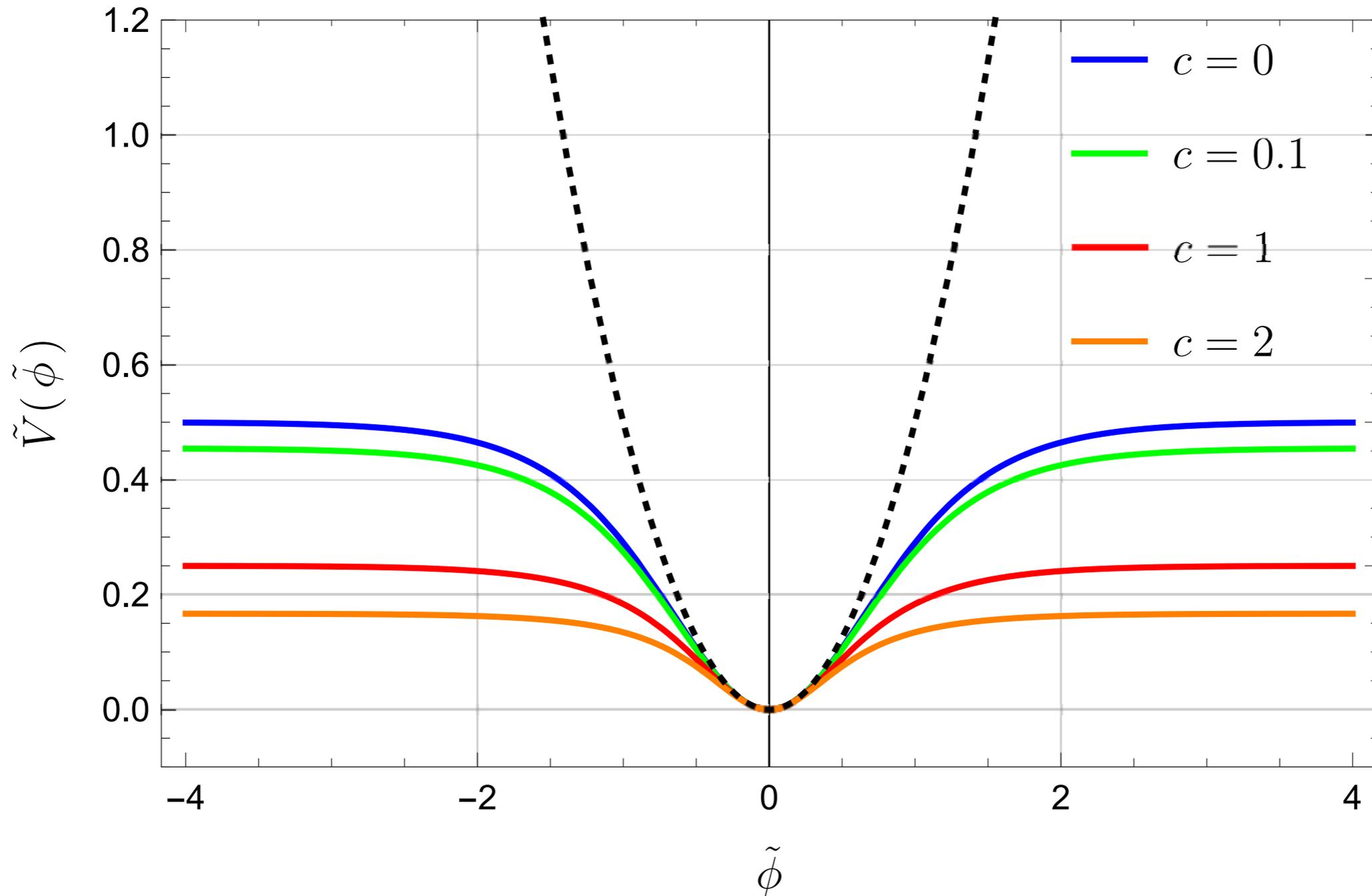
Micha & Tkachev (02,04)

6. Oscillon/I-ball formation

Kasuya+(03), Amin + (10, 12, 17), Zhou(13), Antusch +(17), Kawasaki+(17), ...

Exercise: α -attractor

$$V(\phi) = \frac{(m_a f)^2}{2} \frac{(\tanh \frac{\phi}{f})^2}{1 + c(\tanh \frac{\phi}{f})^2}$$



Solving KG eq.

in cosmological spacetimes

Klein-Gordon eq.

$$\square\phi - V_\phi = 0$$

eg. Homogeneous mode

$$\frac{d^2\tilde{\phi}}{dx^2} + \frac{3p}{x} \frac{d\tilde{\phi}}{dx} + p^2 \frac{d\tilde{V}}{d\tilde{\phi}} = 0$$

Dimensionless form

$$\tilde{\phi} = \phi/f \quad x = m/H = mt/p \quad a \propto tp$$

$$(IC) \tilde{\phi}(x_i), d\tilde{\phi}/dx(x_i) \longrightarrow x_{osc} = O(1) - O(10^4)$$

$$- m \rightarrow H_{osc} = m/x_{osc}$$

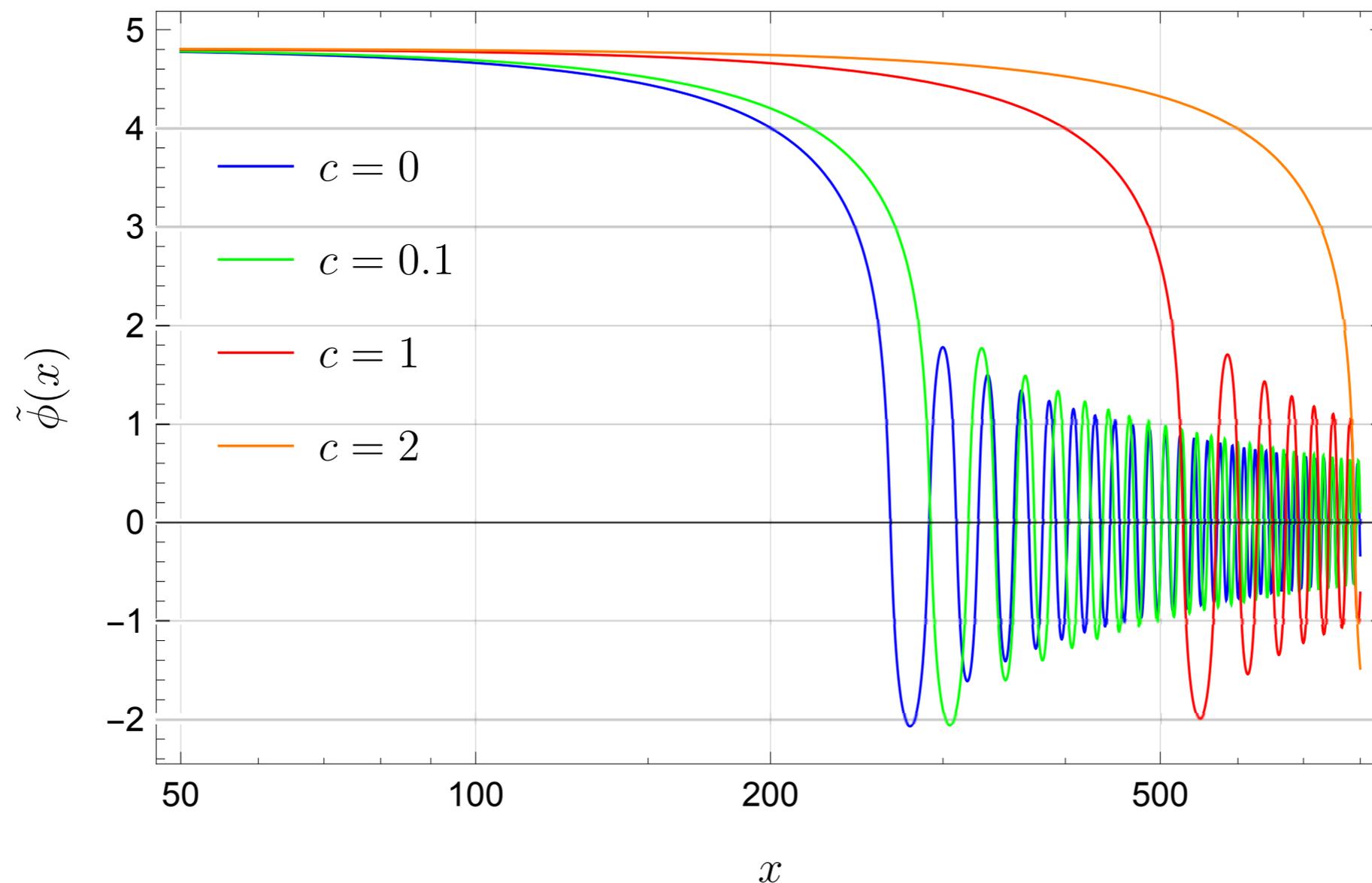
$$- f \rightarrow \text{Abundance}$$

Background evolution

$\tilde{\phi}_i=5$

RD

Soda & Y.U.(17)



$x = m/H$

Onset of oscillation is not $m \sim H$, but delayed!

Linear perturbation

in Newtonian gauge

$$\ddot{\varphi} + 3H\dot{\varphi} + \frac{k^2}{a^2}\varphi + V_{\phi\phi}\varphi - 2V_{\phi}\Phi + \dot{\phi}\dot{\Phi} = 0$$

Φ : Bardeen potential

2 possible instabilities

i) Parametric resonance instability

Non-linear potential

$$V_{\phi\phi} \supset \phi^n \sim (\phi^* \cos mt)^n$$

$$\longrightarrow \cos(nmt)$$

ii) Tachyonic instability

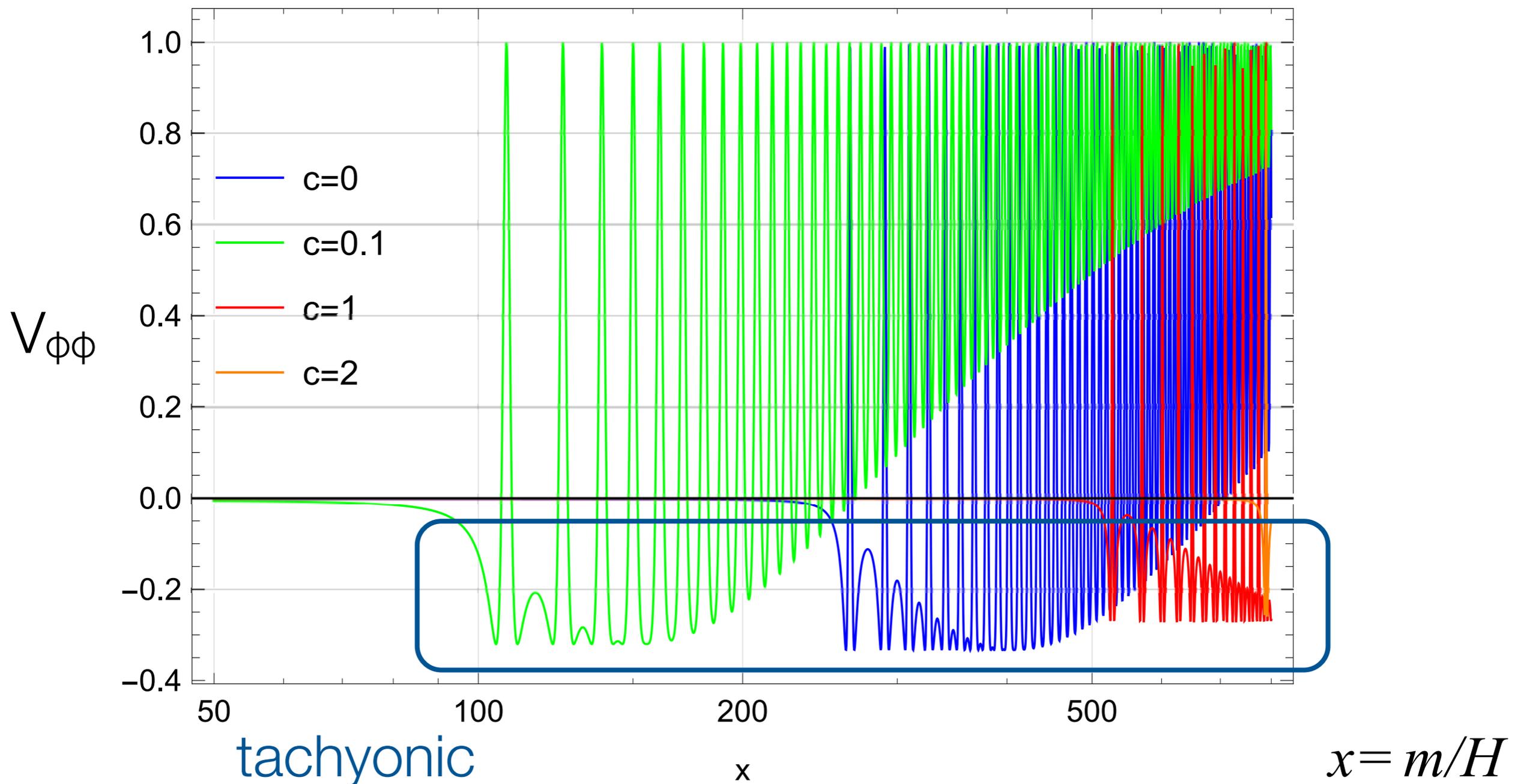
Region w/ $V_{\phi\phi} < 0$

* Backreaction of ULA on Φ was neglected.

Tachyonic instability?

Time evolution of mass term

$\tilde{\varphi}_i=5$ RD ($p=1/2$)

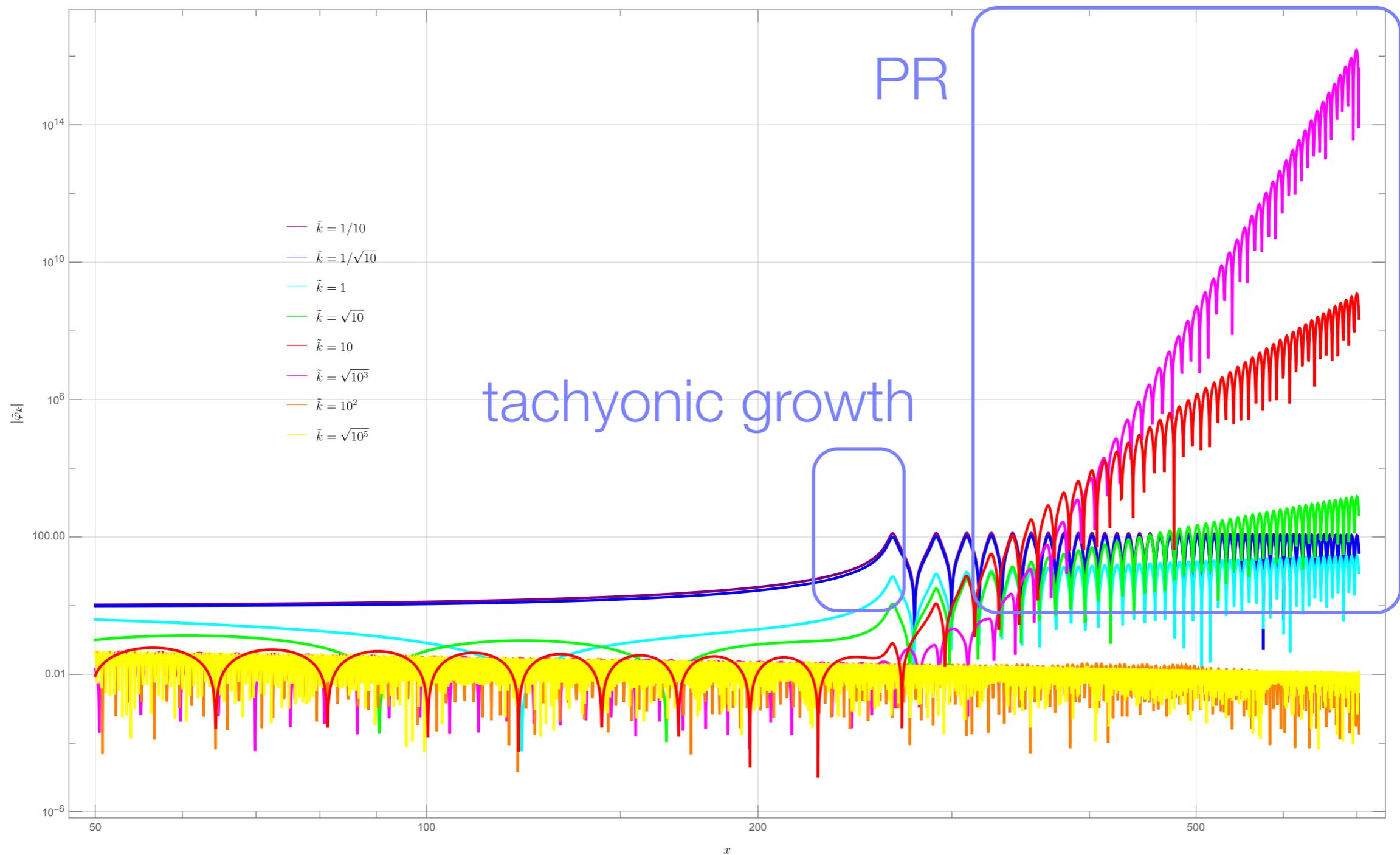


Linear perturbation

Soda & Y.U.(17)

Onset of oscillation in RD

$$\tilde{k} = k/(a_i m)$$



Parametric resonance instability

Neglect cosmic exp. and Φ

$$\frac{d^2}{dx^2} \tilde{\varphi} + (A - 2a \cos 2x) \tilde{\varphi} = 0$$

BG axion $\tilde{\phi} = \tilde{\phi}_* e^{if}$

Band width $(q/A)^n$

$$A \equiv \frac{1}{4} \left[\left(\frac{k}{m a_{osc}} \right)^2 + 1 - (2 + 3c) \tilde{\phi}_*^2 \right] \quad q \equiv \frac{2 + 3c}{8} \tilde{\phi}_*^2$$

Mathieu equation

Resonance band

$$A \simeq n^2$$

First resonance band

$$\tilde{\varphi} \propto e^{\gamma x}$$

$$\gamma \simeq \frac{q}{2} = \frac{2 + 3c}{16} \tilde{\phi}_*^2$$

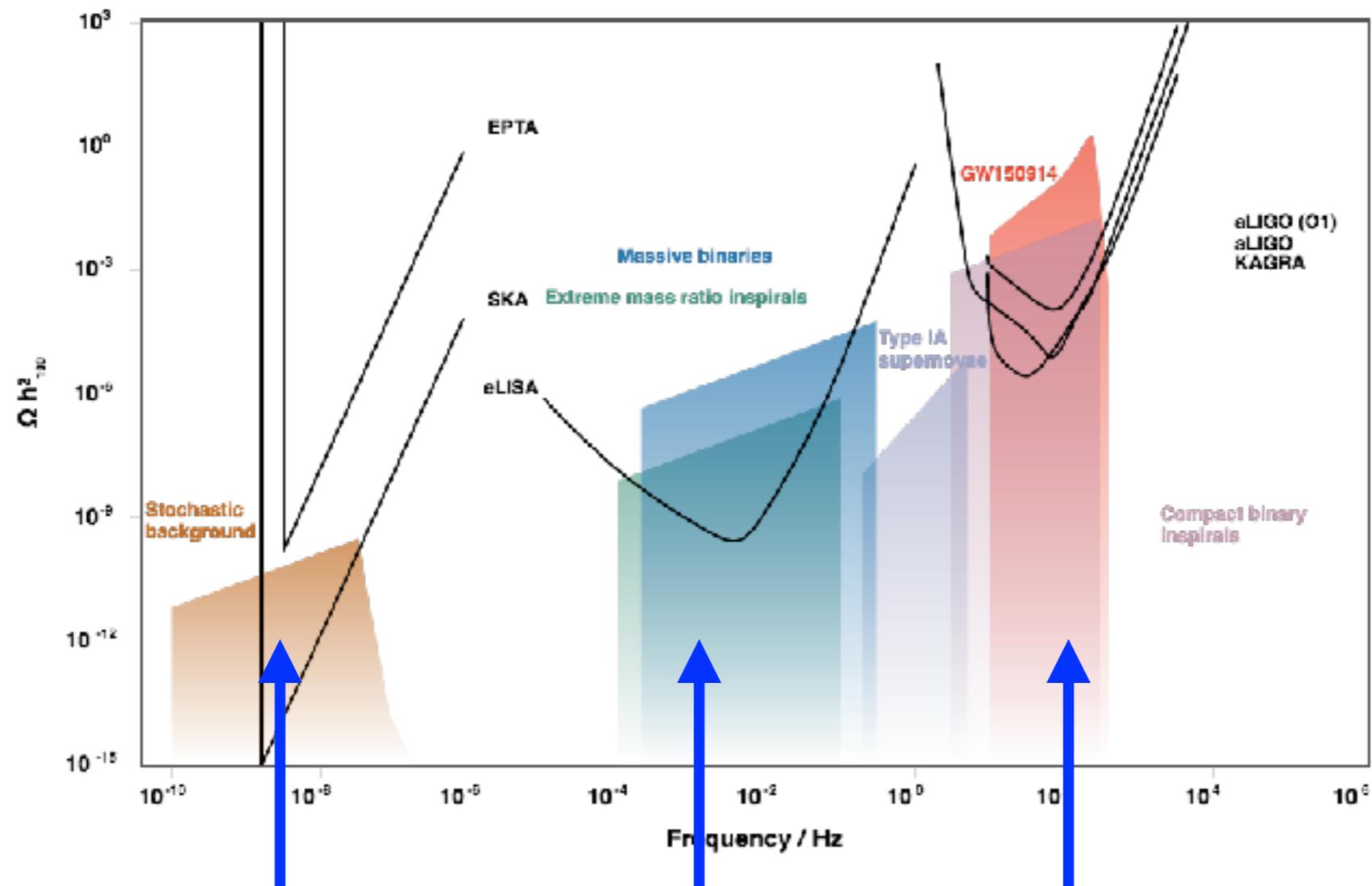
GWs from PR of axion

Frequency at present

$$f_0 \simeq m / (1 + z_*)$$

z_* : Redshift at emission

$$z_{\text{osc}} \sim z_*$$



$$m \sim 10^{-16} \text{eV}$$

$$m \sim 10^{-6} \text{eV}$$

$$m \sim 10^3 \text{eV}$$

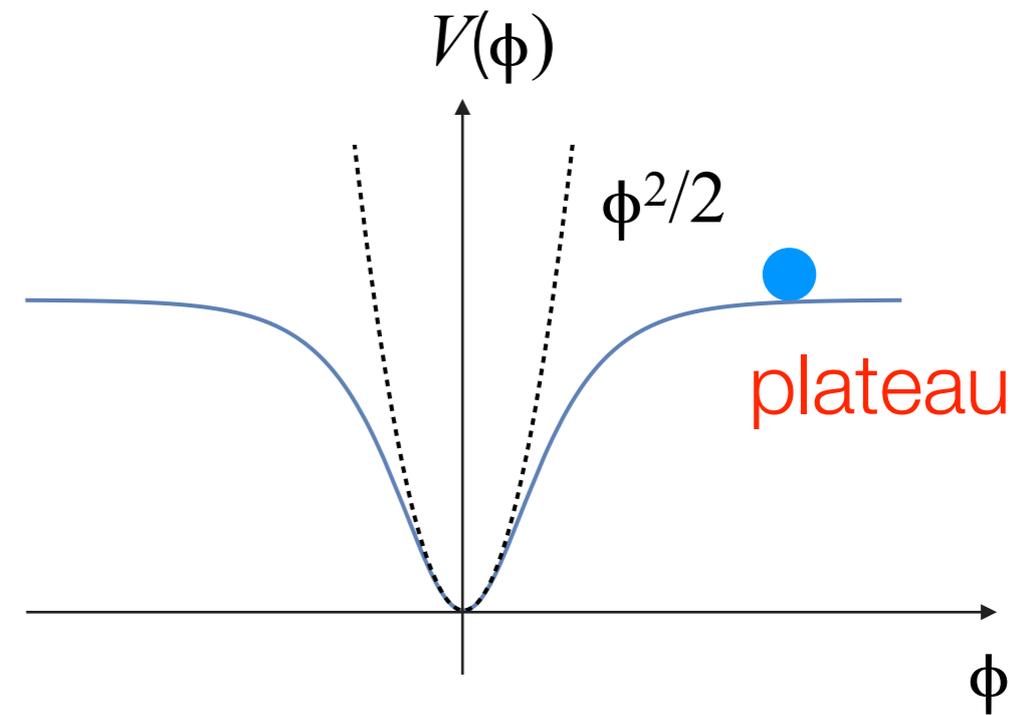
Bottom-line story of Axion's excursion

1. Axion slowly rolls in plateau

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eg. Kofman, Linde, Starobinsky

J.S&Y.U(07)
.....



+N.K

4. Rescattering → PR becomes inefficient

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Micha & Tkachev (02,04)

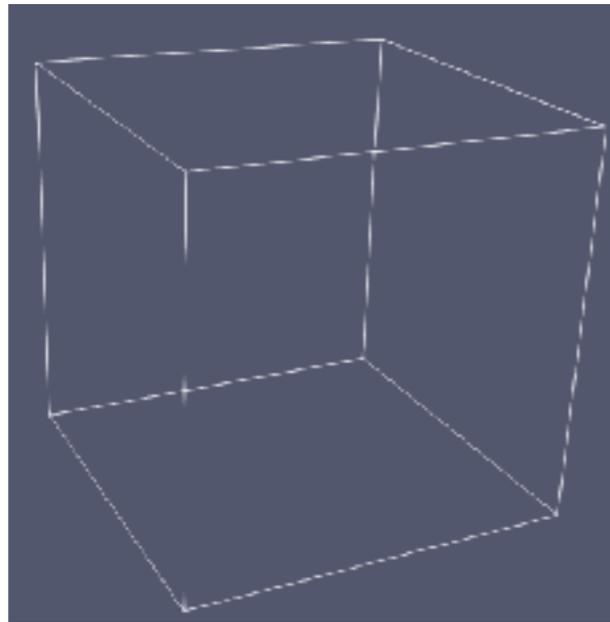
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Oscillon formation

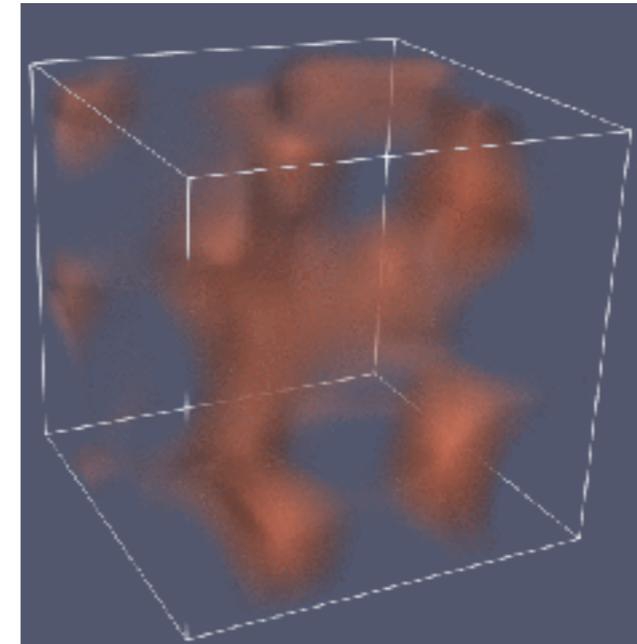
Kitajima, Soda, Y.U. (in preparation)

$a \sim a_0$



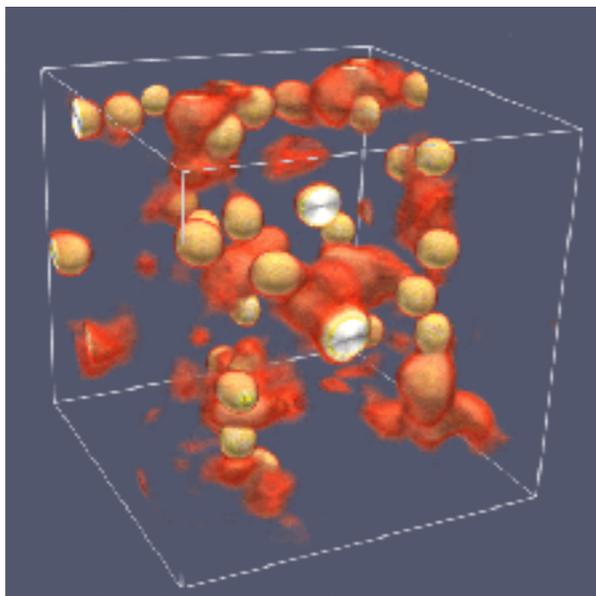
$a \sim 20 a_0$

rescattering



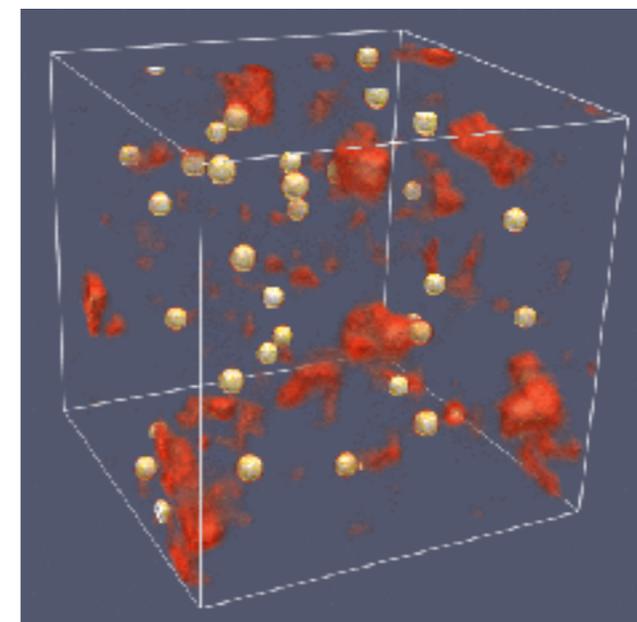
$a \sim 35 a_0$

turbulence



$a \sim 90 a_0$

oscillon



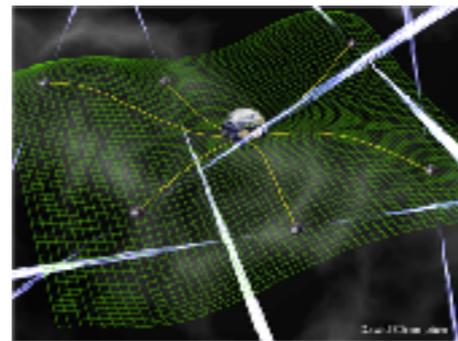
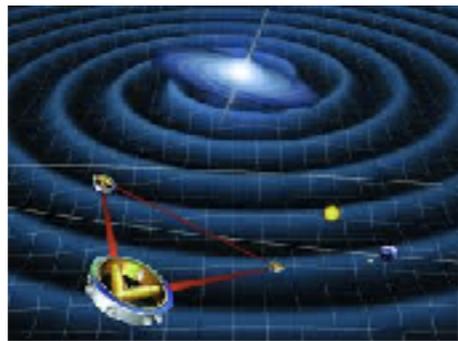
$N_{\text{grid}}=(128)^3$

$f \sim 10^{-4} M_{\text{P}}, c=5, \phi_i=5 \rightarrow \Omega_{\text{GW}} \sim 10^{-15}$ in PTA band

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Bottom-line story of Axion's excursion

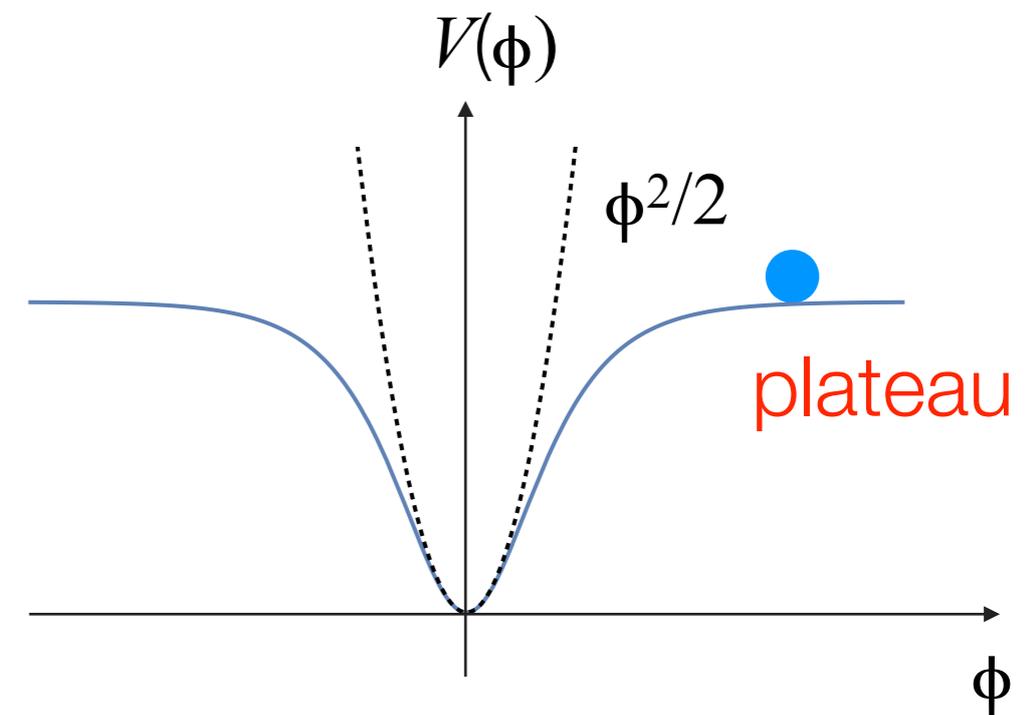
1. Axion slowly rolls in plateau
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3. Exponential growth due to PR

if not $H_{osc}/m \ll 1$

4. PR finished due to red-shift

Yet, for DM= axion, imprints on structure formation

Resonance peak in spectrum



Imprints for axion DM

Alternative solution to small scale issues of Λ CDM??

ULA w/ $m \sim 10^{-22} eV$

Recall Nagamine-san's

→ Emergent pressure smooths at $k > k_J$

k_J : Jeans scale

→ Tension with small scale observations?

Irsic et al. (17), Kim et al. (17), ...

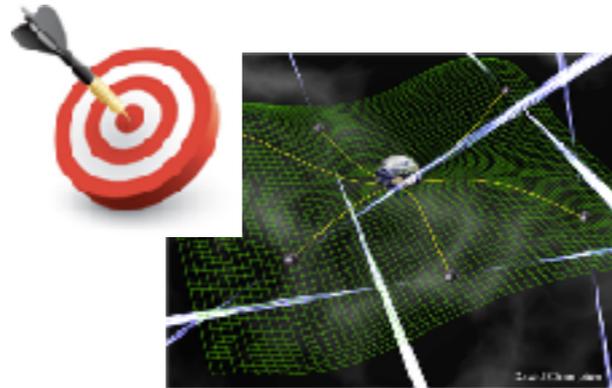
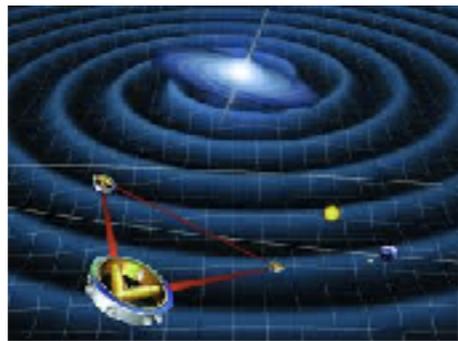
Note!! Resonance scale $k_r > k_J \propto a^{1/4}$

Evade tension? (in progress)

Summary

Targets: Axions in plateau

i) New window in string axiverse



ii) For Axion DM, enhancement of power spectrum at the scale determined by \sim the mass scale.

Remedy for tension of ULA w/small scale observations?

in progress

Ultralight axion (ULA)

What is often said.....

$m > H_{eq} \sim 10^{-27}$ eV, ULA is quiet in cosmological scales.

 Not ULA in plateau!

Jeans scale

ULA has pressure \rightarrow Jeans scale $k_J(a) \simeq \sqrt{mH} a$

$k > k_J$ fluctuations are smoothed out

\longrightarrow Tension with Lyman α forest observation

at equal time $k_r \simeq \sqrt{x_{osc}} k_J(a_{eq})$ Relaxing the tension?